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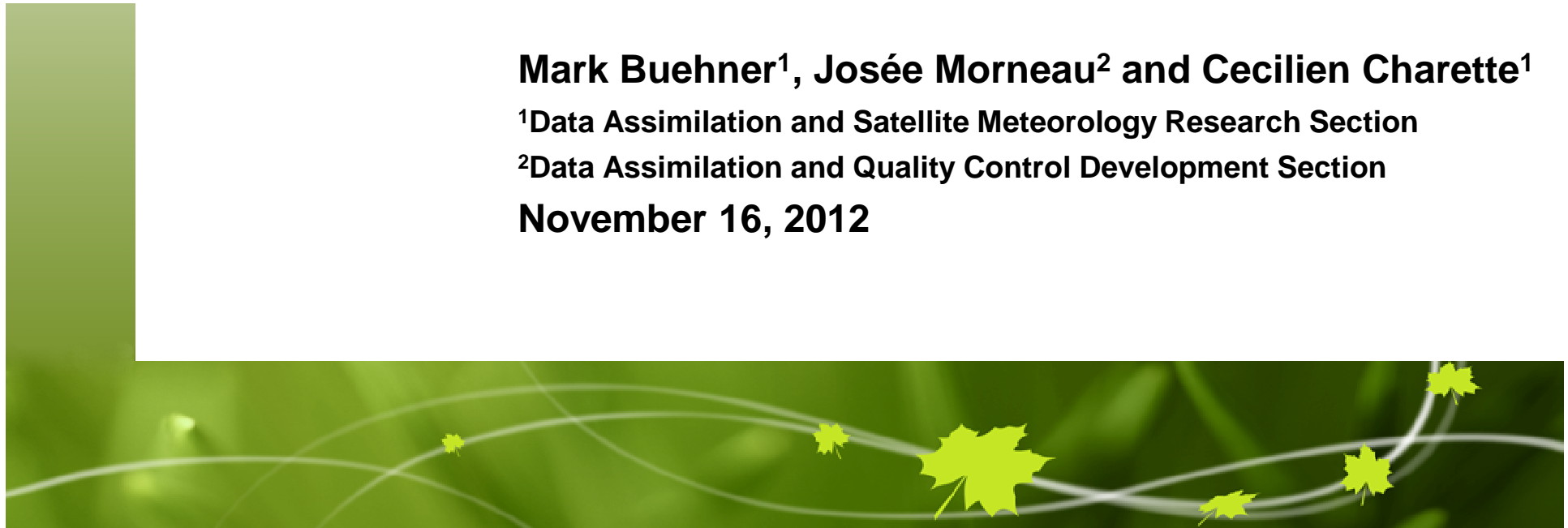
A comparison of Ensemble-Variational (EnVar) data assimilation and 4D-Var for global deterministic weather prediction

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Contents

- Background
- The ensemble-variational (EnVar) data assimilation approach
- Recent results from using EnVar compared with standard 3D-Var and 4D-Var (but NO comparisons with 4D-Var-Ben or EnKF)
- Conclusions and next steps



Background

- Environment Canada currently has 2 relatively independent state-of-the-art global data assimilation systems
- **4D-Var** (Gauthier et al 2007) and **EnKF** (Houtekamer et al 2009):
 - both operational since 2005
 - both use GEM forecast model and assimilate similar set of observations
 - current effort towards unifying code of the two systems
- 4D-Var is used to initialize medium range global deterministic forecasts (GDPS)
- EnKF is used to initialize global ensemble forecasts (GEPS)
- Intercomparison of approaches and various hybrid configurations was performed in **carefully controlled context**: similar medium-range forecast quality from EnKF and 4D-Var analyses, 4D-Var-Ben best
- Results presented at WMO workshop on intercomparison of 4D-Var and EnKF, Buenos Aires, November 2008 (Buehner et al 2010)



Ensemble-Variational assimilation: EnVar

- EnVar approach is currently being tested in the context of replacing 4D-Var in the operational Global Deterministic Prediction System
- EnVar uses a **variational assimilation approach** in combination with the already available **4D ensemble covariances** from the EnKF
- By making use of the 4D ensembles, EnVar performs a 4D analysis without the need of the tangent-linear and adjoint of forecast model
- Consequently, it is more computationally efficient and easier to maintain/adapt than 4D-Var
- Hybrid covariances can be used in EnVar by averaging the ensemble covariances with the static NMC-method covariances
- Like 4D-Var, EnVar uses an incremental approach with:
 - analysis increment at the horizontal/temporal resolution of EnKF ensembles
 - background state and analysis at the horizontal/temporal resolution of the higher-resolution deterministic forecast model

Page 4 – January 14, 2013



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EnVar formulation

- In 4D-Var the 3D analysis increment is evolved in time using the TL/AD forecast model (here included in \mathbf{H}_{4D}):

$$J(\Delta\mathbf{x}) = \frac{1}{2} (H_{4D}[\mathbf{x}_b] + \mathbf{H}_{4D}\Delta\mathbf{x} - \mathbf{y})^T \mathbf{R}^{-1} (H_{4D}[\mathbf{x}_b] + \mathbf{H}_{4D}\Delta\mathbf{x} - \mathbf{y}) + \frac{1}{2} \Delta\mathbf{x}^T \mathbf{B}^{-1} \Delta\mathbf{x}$$

- In EnVar the background-error covariances and analysed state are explicitly 4-dimensional, resulting in cost function:

$$J(\Delta\mathbf{x}_{4D}) = \frac{1}{2} (H_{4D}[\mathbf{x}_b] + \mathbf{H}\Delta\mathbf{x}_{4D} - \mathbf{y})^T \mathbf{R}^{-1} (H_{4D}[\mathbf{x}_b] + \mathbf{H}\Delta\mathbf{x}_{4D} - \mathbf{y}) + \frac{1}{2} \Delta\mathbf{x}_{4D}^T \mathbf{B}_{4D}^{-1} \Delta\mathbf{x}_{4D}$$

- Computations involving ensemble-based \mathbf{B}_{4D} can be more expensive than with \mathbf{B}_{nmc} depending on ensemble size and spatial/temporal resolution, but significant parallelization is possible

EnVar formulation: Preconditioning

- Preconditioned cost function formulation at Environment Canada:

$$J(\xi) = \frac{1}{2} \xi^T \xi + \frac{1}{2} (H_{4D}(\mathbf{x}_b) + \mathbf{H} \Delta \mathbf{x}(\xi) - \mathbf{y})^T \mathbf{R}^{-1} (H_{4D}(\mathbf{x}_b) + \mathbf{H} \Delta \mathbf{x}(\xi) - \mathbf{y})$$

- In EnVar with hybrid covariances, the control vector (ξ) is composed of 2 vectors:

$$\begin{bmatrix} \xi \end{bmatrix} = \begin{bmatrix} \xi_{\text{nmc}} \\ \xi_{\text{ens}} \end{bmatrix} \rightarrow \begin{bmatrix} \xi_{\text{ens}} \end{bmatrix} = \begin{bmatrix} \xi_{\text{ens}}^1 \\ \vdots \\ \xi_{\text{ens}}^{N_{\text{ens}}} \end{bmatrix}$$

- The analysis increment is computed as (\mathbf{e}_k is k 'th ensemble perturbation divided by $\text{sqrt}(N_{\text{ens}}-1)$):

$$\Delta \mathbf{x}(\xi) = \beta_{\text{nmc}}^{1/2} \mathbf{B}_{\text{nmc}}^{1/2} \xi_{\text{nmc}} + \beta_{\text{ens}}^{1/2} \sum_{k=1}^{N_{\text{ens}}} \mathbf{e}_k \circ (\mathbf{L}^{1/2} \xi_{\text{ens}}^k) \rightarrow \mathbf{B} = \beta_{\text{nmc}} \mathbf{B}_{\text{nmc}} + \beta_{\text{ens}} \sum_{k=1}^{N_{\text{ens}}} (\mathbf{e}_k \mathbf{e}_k^T) \circ \mathbf{L}$$

- Better preconditioned than original “alpha control vector” formulation (with \mathbf{L}^{-1} and $1/\beta$ in background term of J)
- Most, but maybe not all, applications of the approach use the better preconditioned formulation

Experimental results:

Configuration

EnVar tested in comparison with new version of forecast system currently being implemented in operations:

- model top at 0.1hPa, 80 levels
- ~25km grid spacing
- 4D-Var analysis increments with ~100km grid spacing

EnVar experiments use ensemble members from new configuration of EnKF:

- 192 members every 60min in 6-hour window
- model top at 2hPa, 75 levels
- ~66km grid spacing → EnVar increments ~66km grid spacing



Experimental results:

Computational cost

Overall, EnVar analysis ~3X faster than 4D-Var on half as many cpus, even though higher resolution increments

Wall-clock time of 4D-Var already close to allowable time limit; increasing number of processors has negligible impact

To progress with 4D-Var, significant work would be required to improve scalability of TL/AD versions of forecast model at resolutions and grid configuration used in 4D-Var

Current focus for model is on development of higher-resolution global Yin-Yang configuration that scales well

Decision made to try to replace 4D-Var with more efficient EnVar → if EnVar is at least as good as current 4D-Var



EnVar uses Hybrid Covariance Matrix

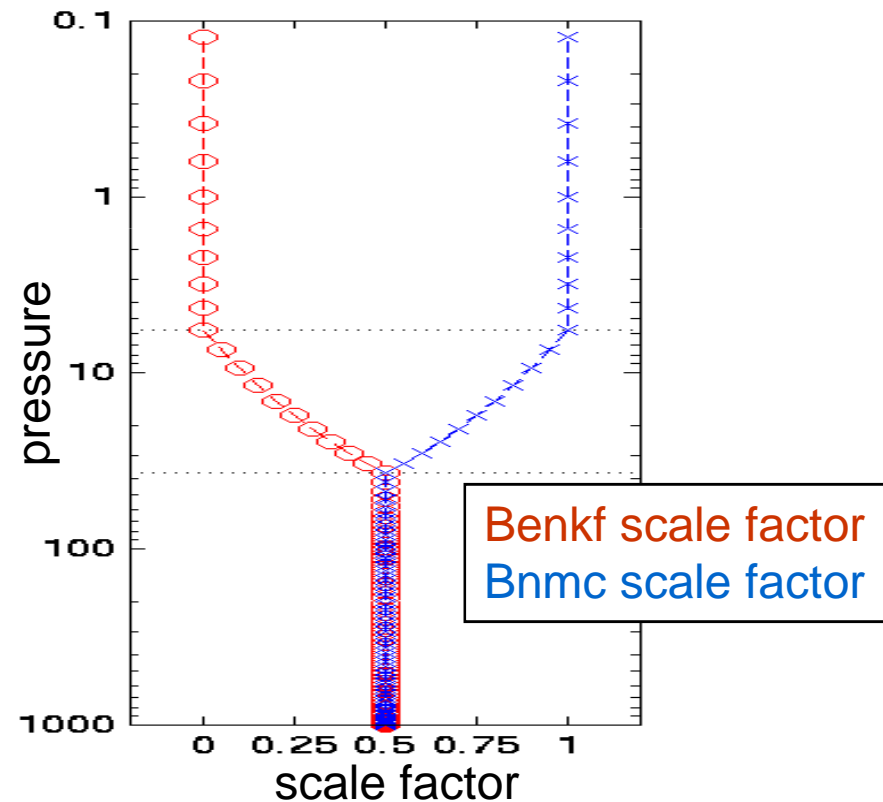
Model top of EnKF is lower than GDPS

Benkf and Bnmc are averaged in troposphere $\frac{1}{2}$ & $\frac{1}{2}$, tapering to 100% Bnmc at and above 6hPa (EnKF model top at 2hPa)

Therefore, EnVar not expected to be better than 3D-Var above $\sim 10\text{-}20\text{hPa}$

Also tested 75% Benkf and 25% Bnmc in troposphere, but results slightly worse

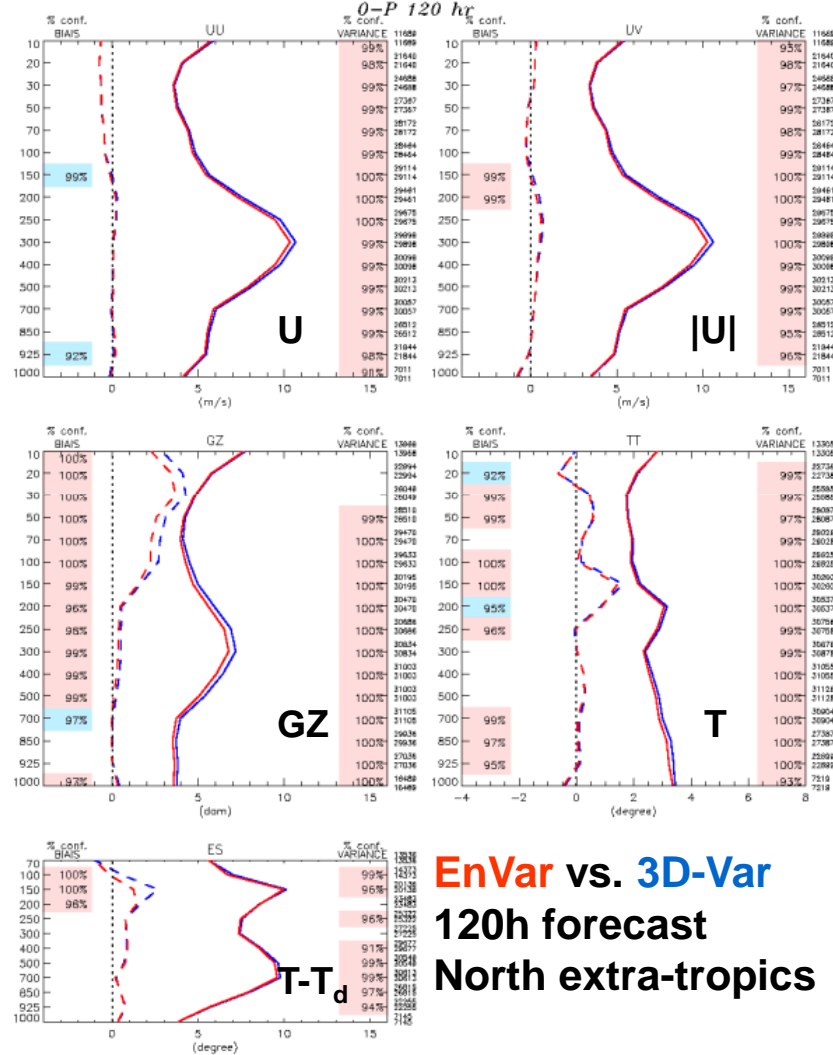
Also did preliminary tests with a full outer loop, but degraded the results



Forecast Results: EnVar vs. 3D-Var and 4D-Var

Radiosonde verification scores – 6 weeks, Feb/Mar 2011

keh125_g contre k3h125_j (hiver 2011)



EnVar vs. 3D-Var
120h forecast
North extra-tropics

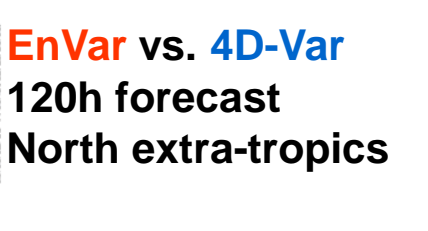
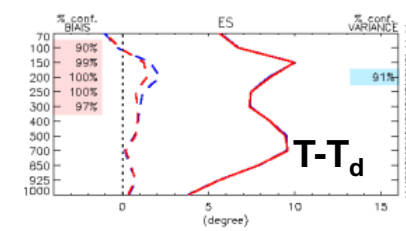
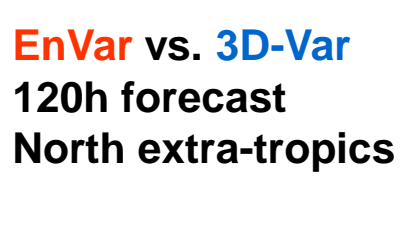
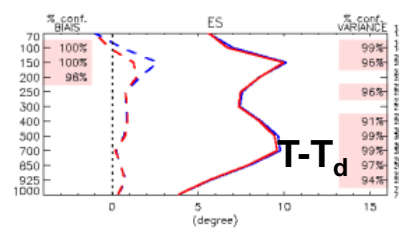
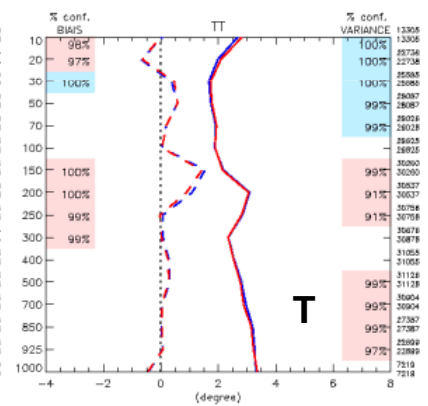
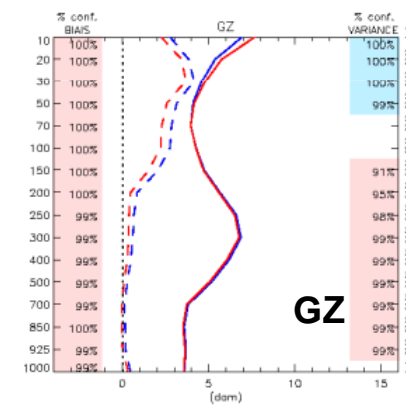
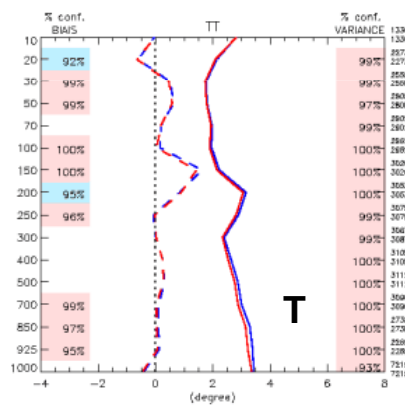
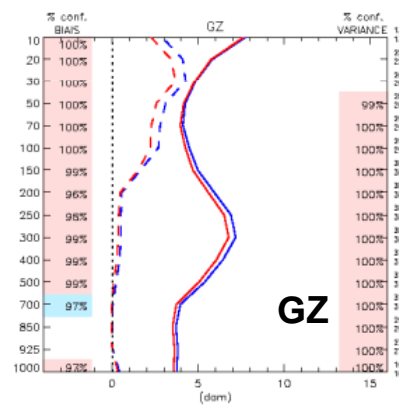
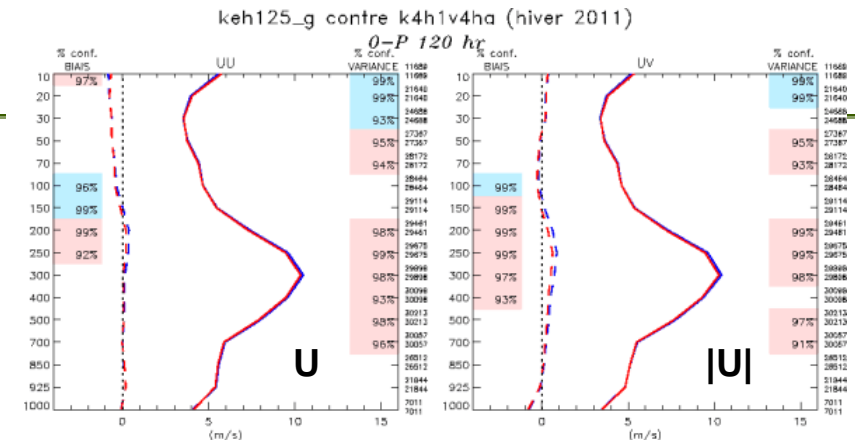
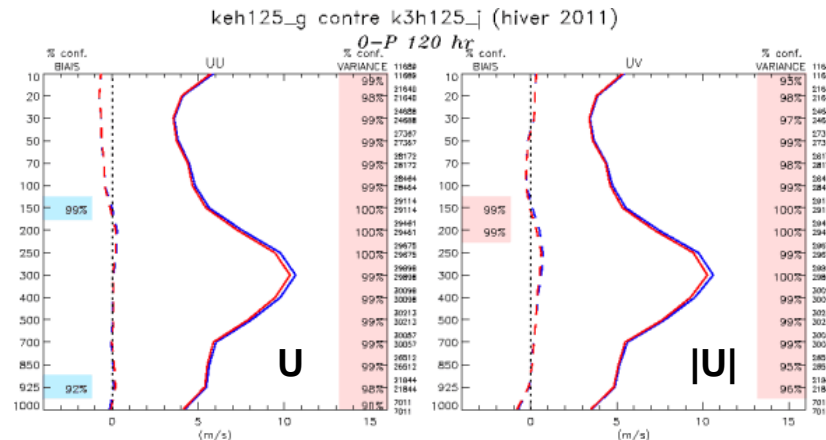
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January 14, 2013



Forecast Results: EnVar vs. 3D-Var and 4D-Var

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EnVar vs. 3D-Var
120h forecast
North extra-tropics

EnVar vs. 4D-Var
120h forecast
North extra-tropics

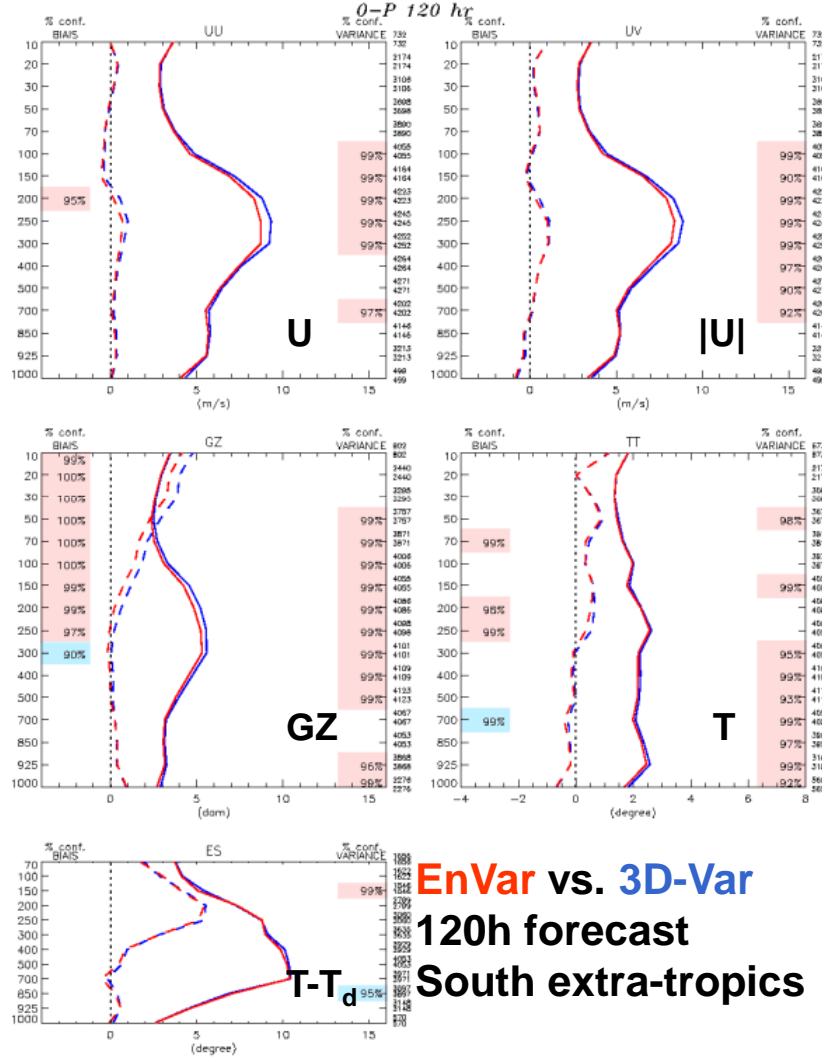
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keh125_g contre k3h125_j (hiver 2011)



EnVar vs. 3D-Var
120h forecast
South extra-tropics

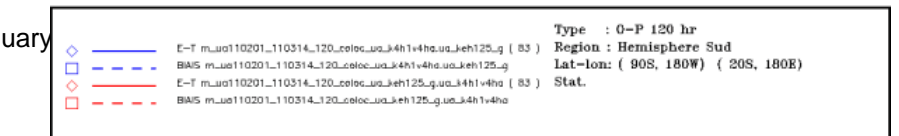
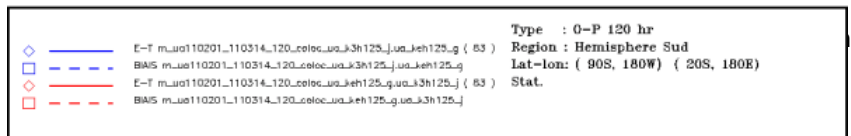
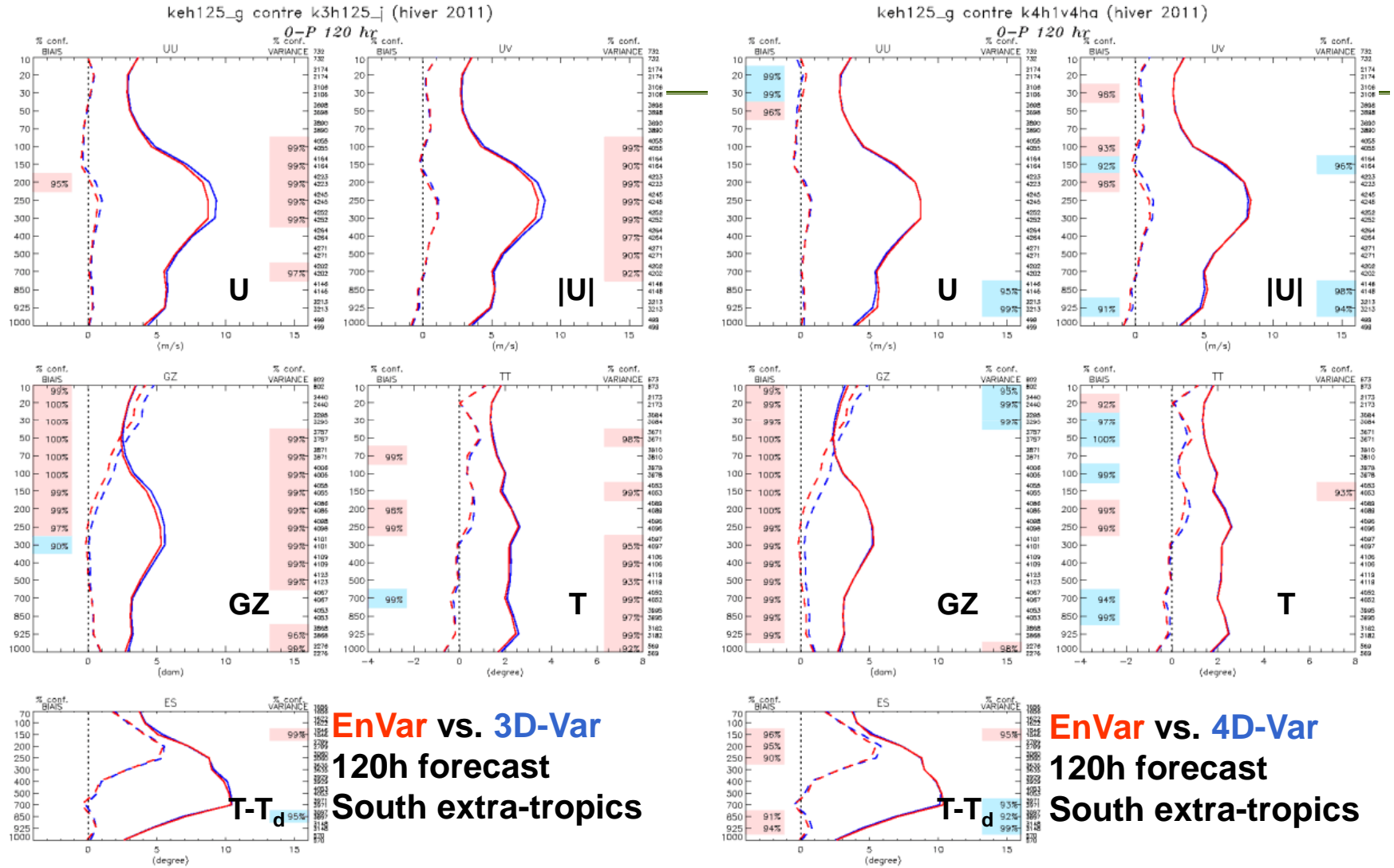
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January 14, 2013



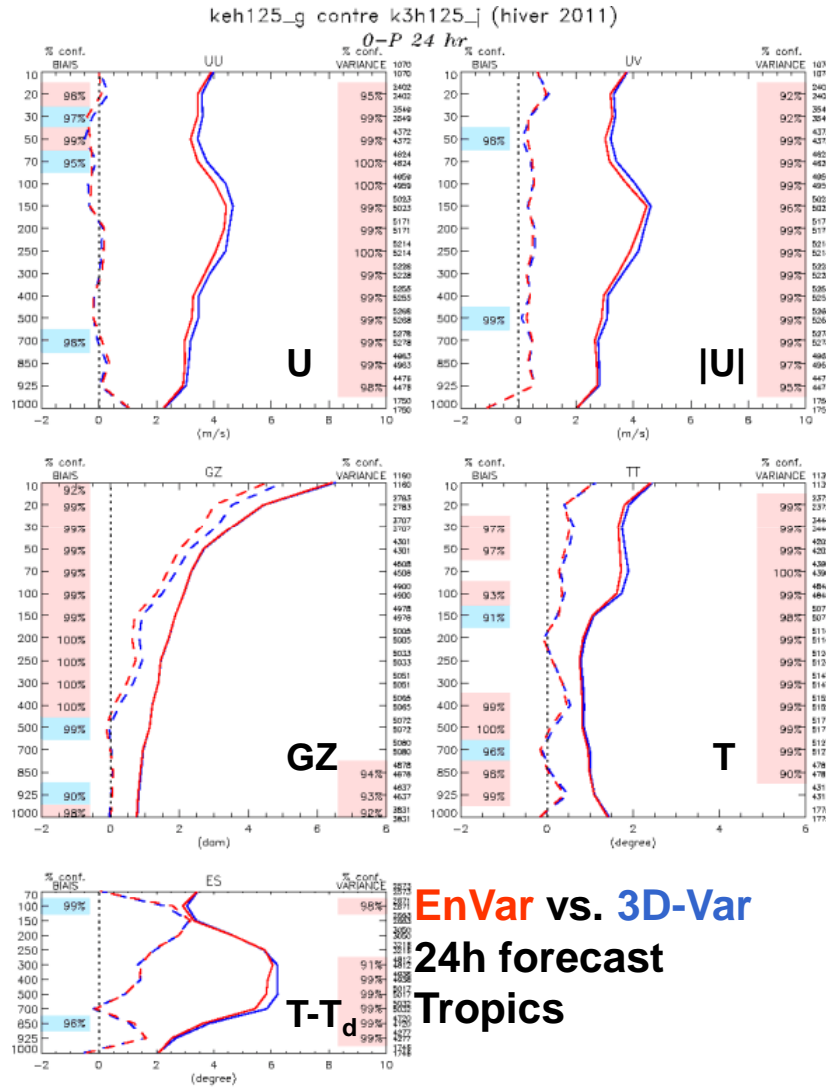
Forecast Results: EnVar vs. 3D-Var and 4D-Var

Radiosonde verification scores – 6 weeks, Feb/Mar 2011



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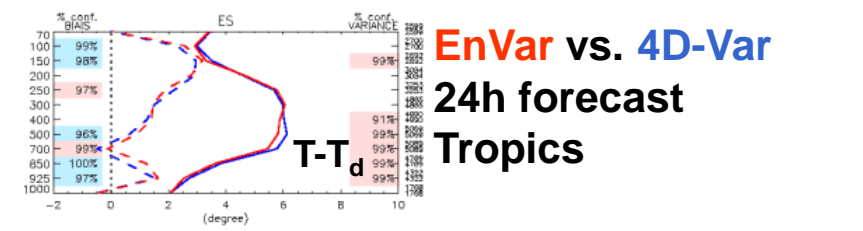
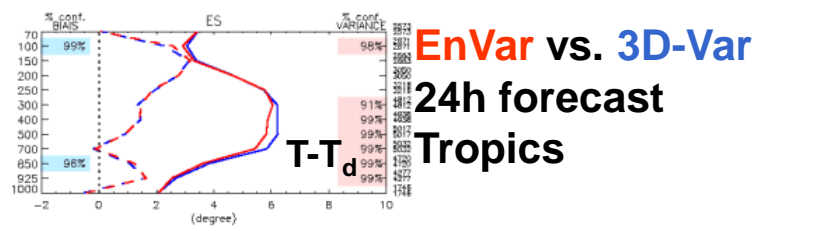
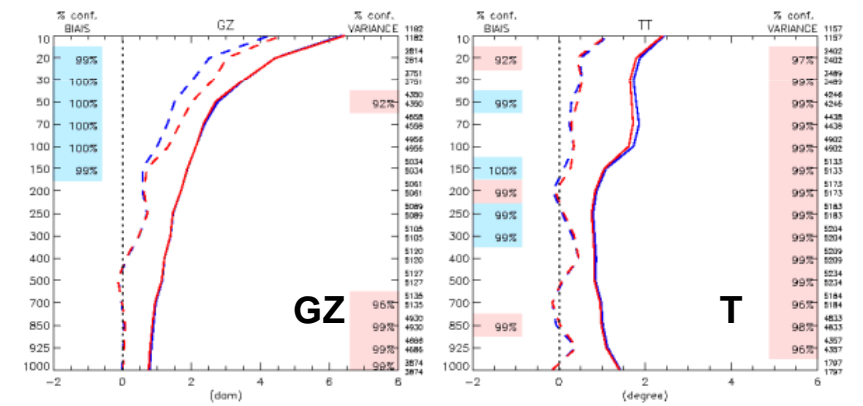
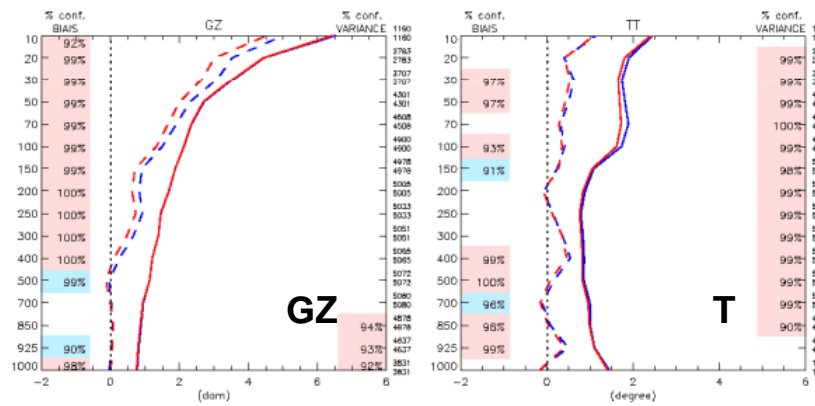
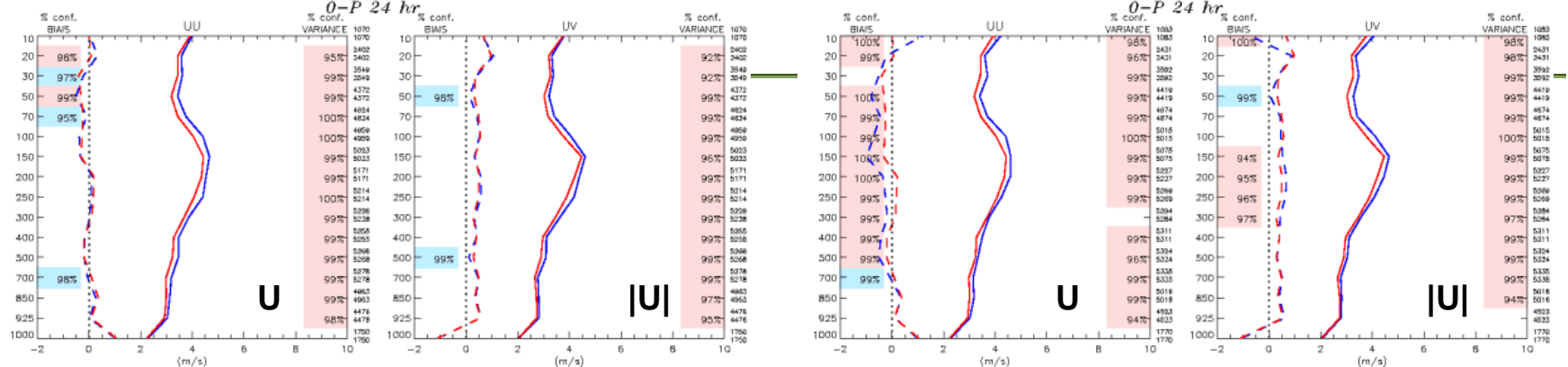
January 14, 2013

Forecast Results: EnVar vs. 3D-Var and 4D-Var

Radiosonde verification scores – 6 weeks, Feb/Mar 2011

keh125_g contre k3h125_j (hiver 2011)

keh125_g contre k4h1v4ha (hiver 2011)



Type : 0-P 24 hr
Region : Tropiques
Lat-lon : (20S, 180W) (20N, 180E)
Stat.

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Lat-lon : (20S, 180W) (20N, 180E)
Stat.

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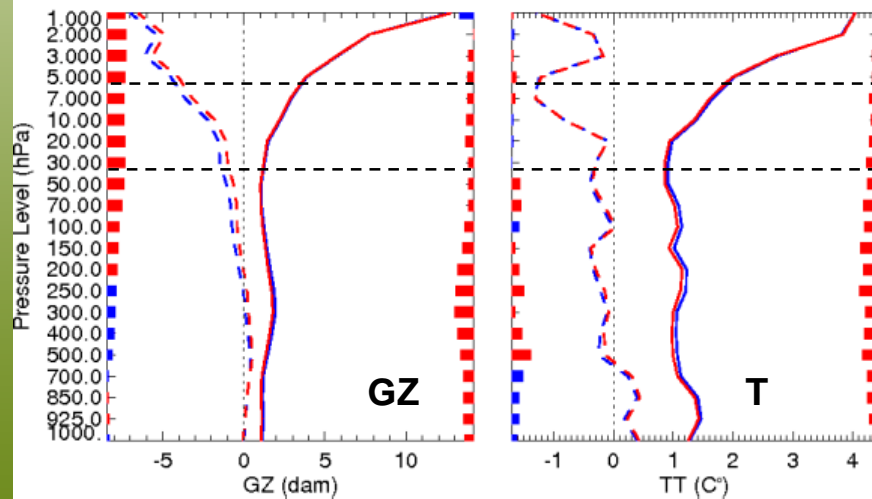
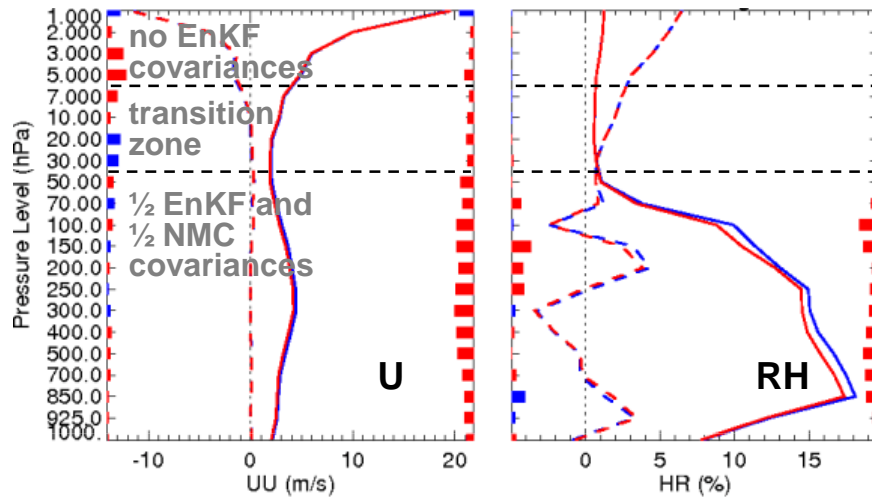


Forecast Results: EnVar vs. 3D-Var and 4D-Var

Verification against ERA-Interim analyses – 6 weeks, Feb/Mar 2011

EnVar vs. 3D-Var

48h forecast, global domain



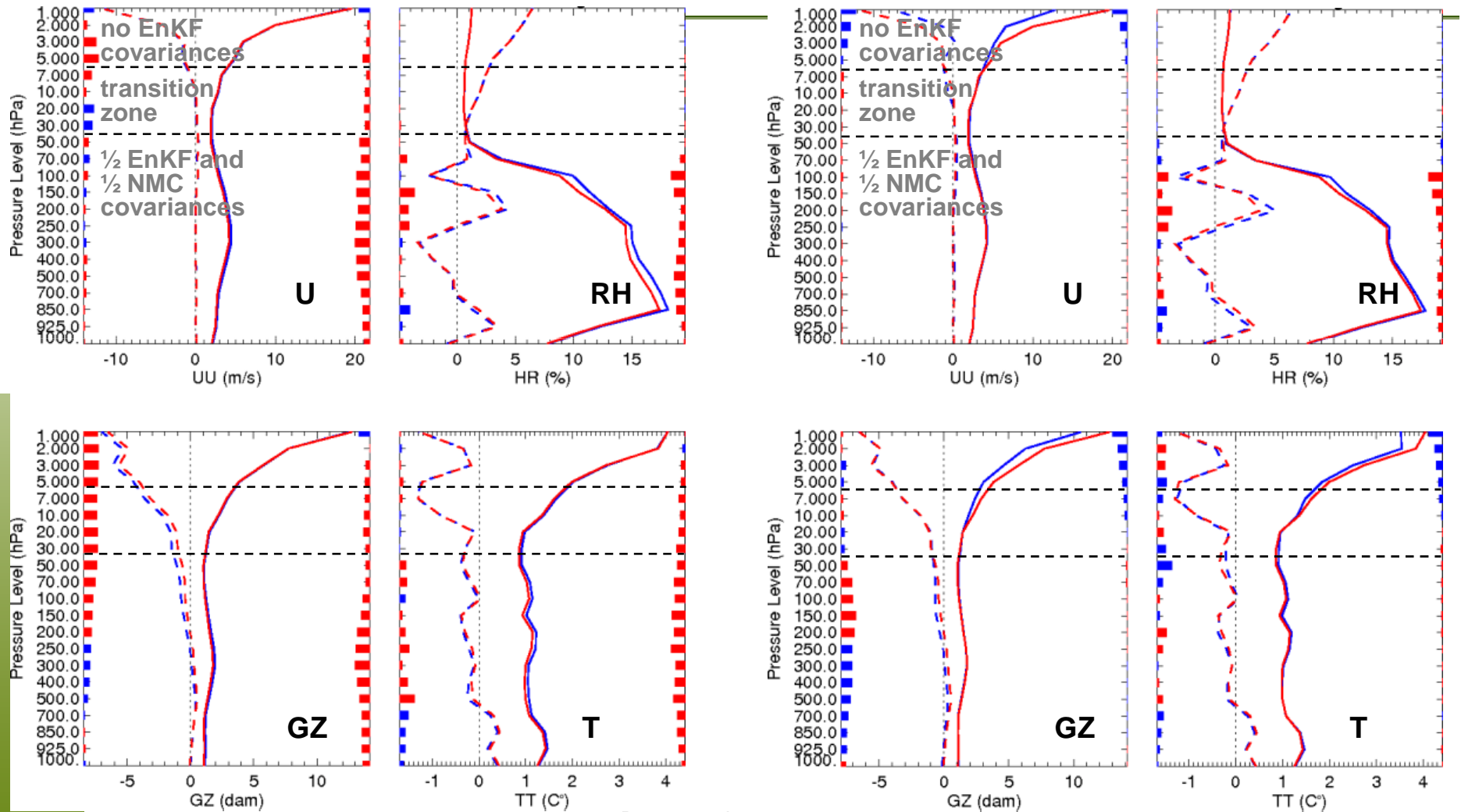
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48h forecast, global domain

EnVar vs. 4D-Var

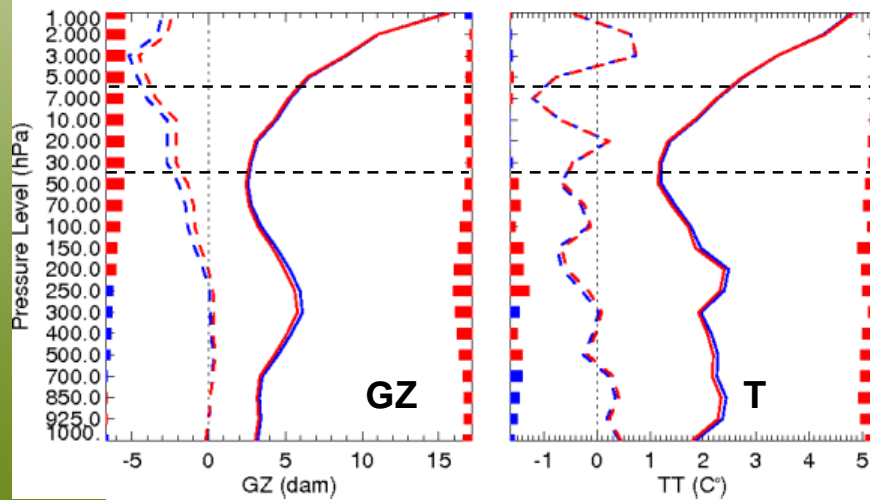
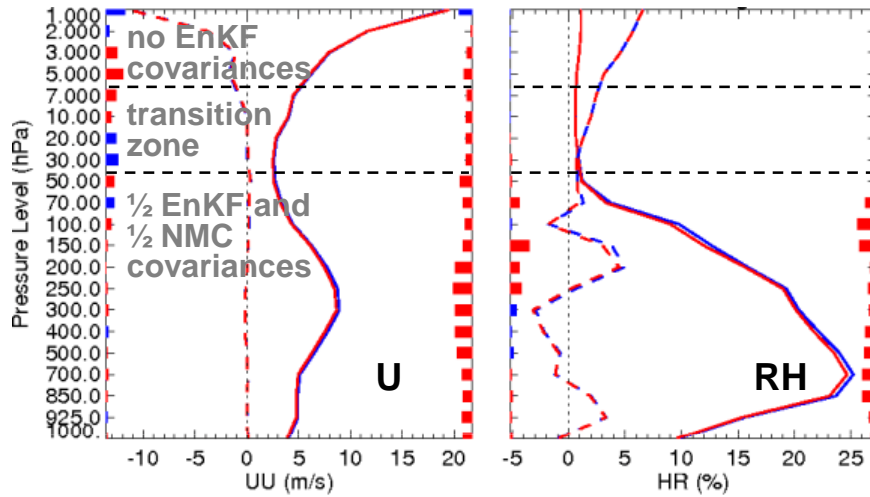


Forecast Results: EnVar vs. 3D-Var and 4D-Var

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EnVar vs. 3D-Var

120h forecast, global domain



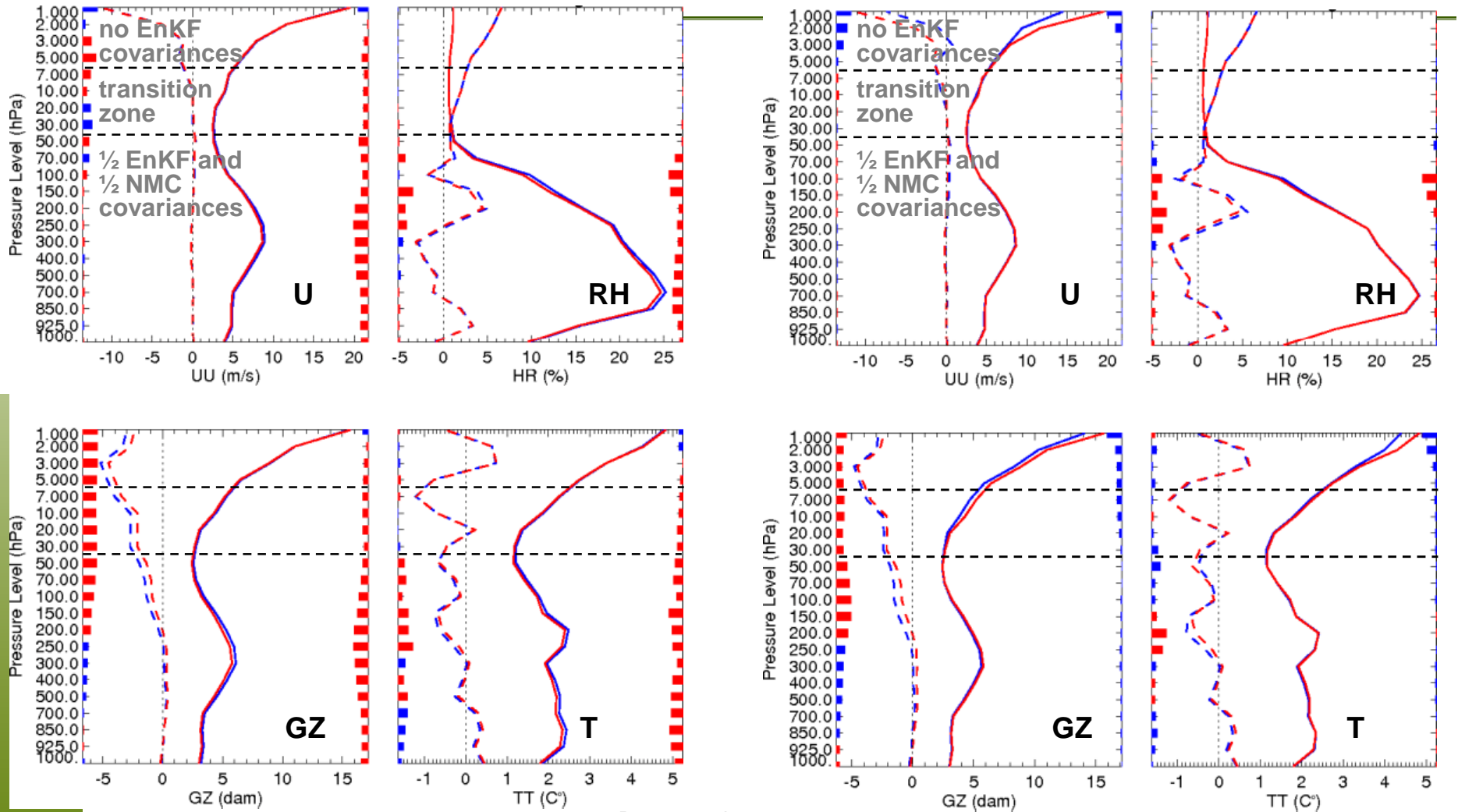
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EnVar vs. 3D-Var

120h forecast, global domain

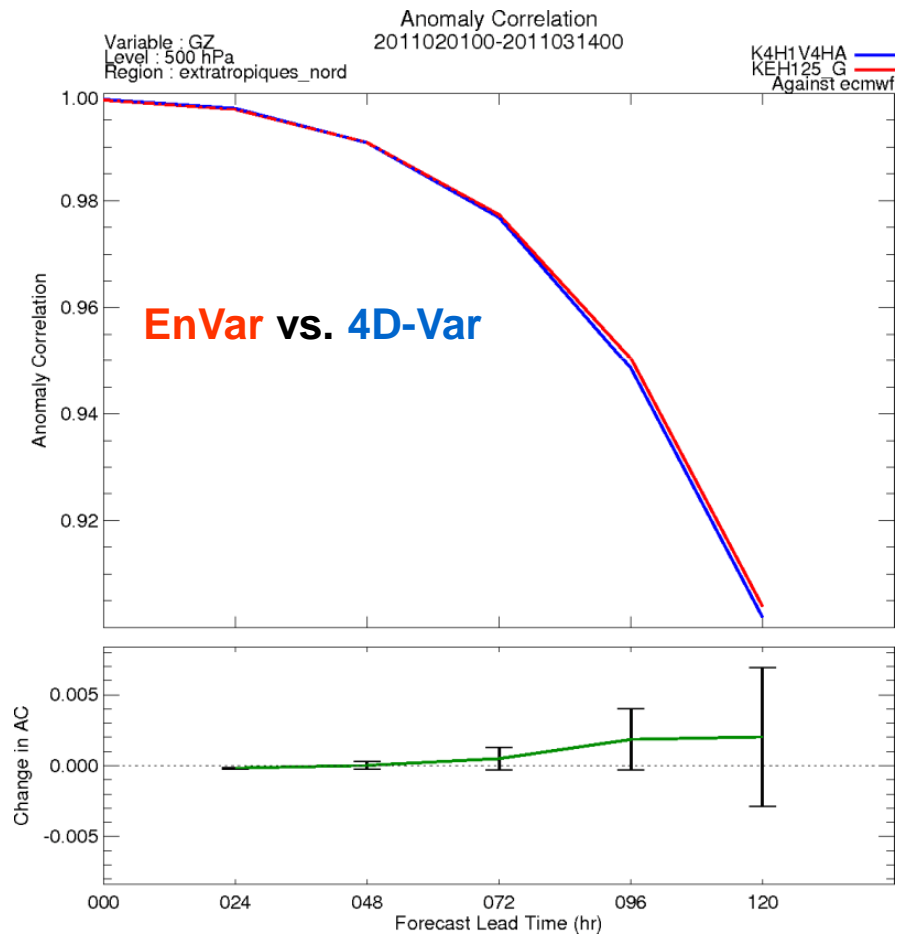
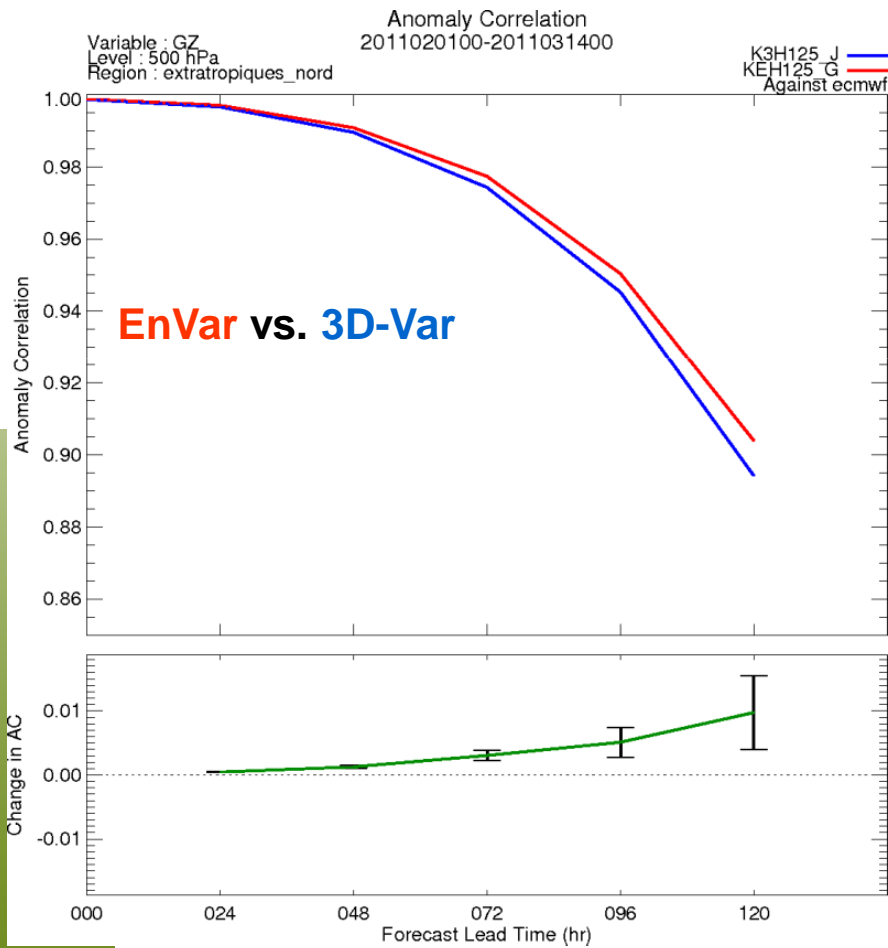
EnVar vs. 4D-Var



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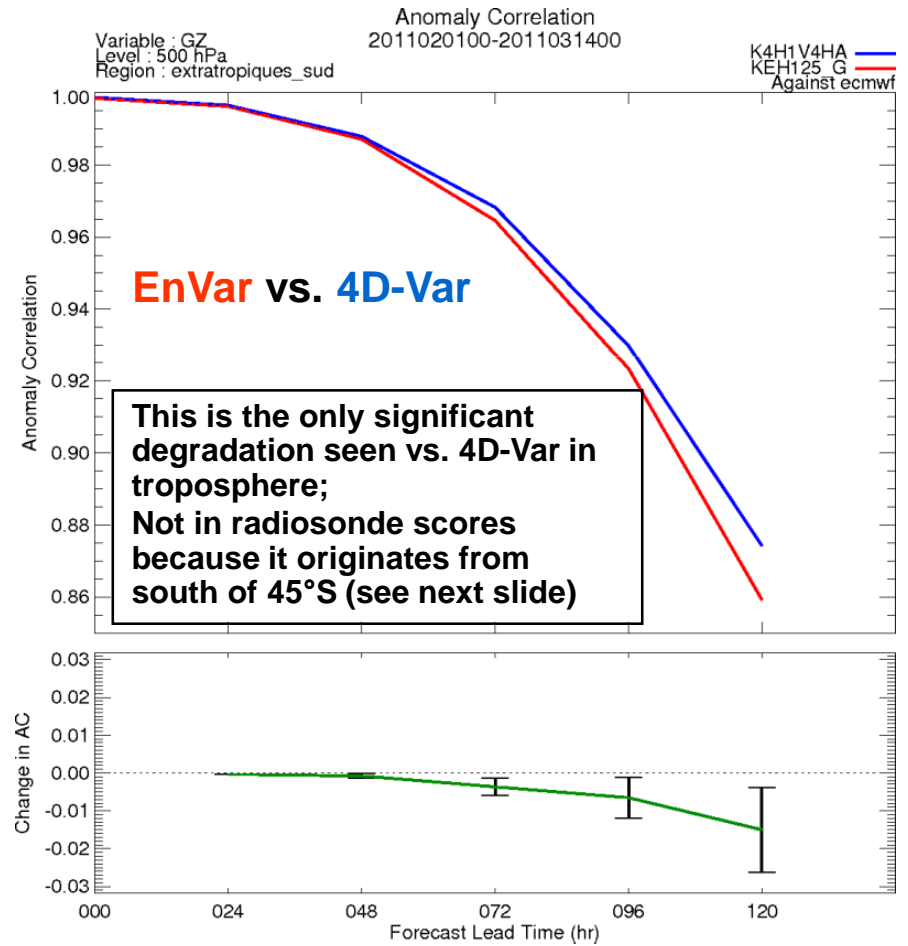
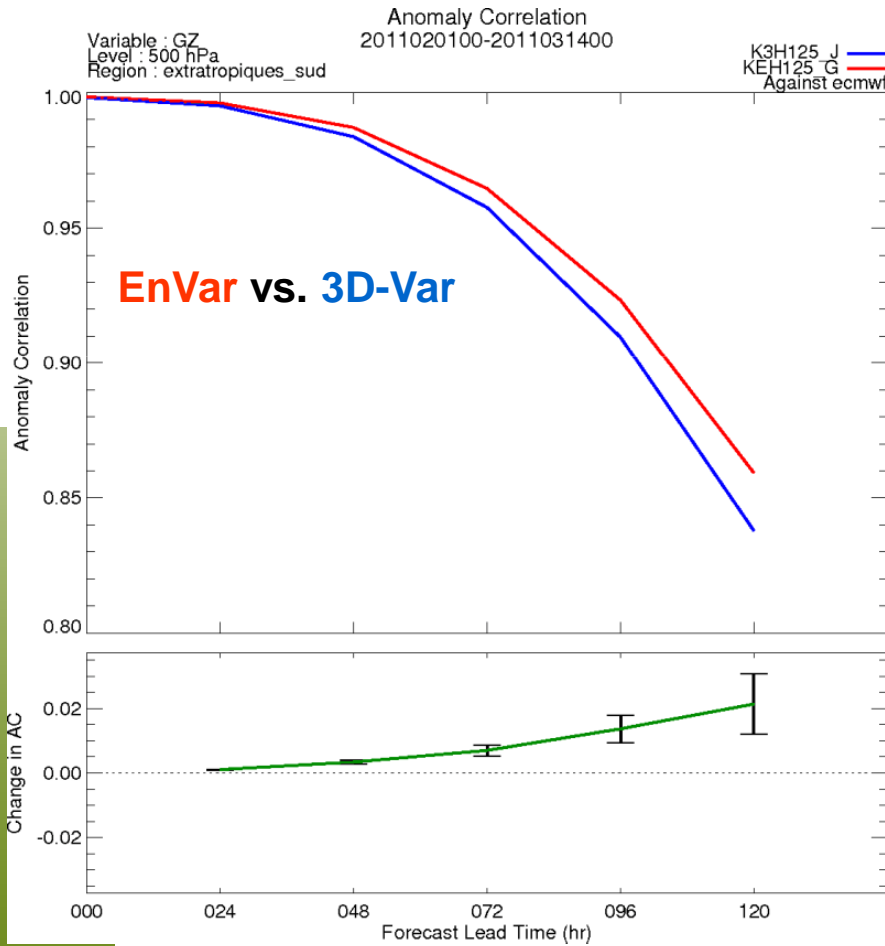
North extra-tropics
500hPa GZ correlation anomaly



Forecast Results: EnVar vs. 3D-Var and 4D-Var

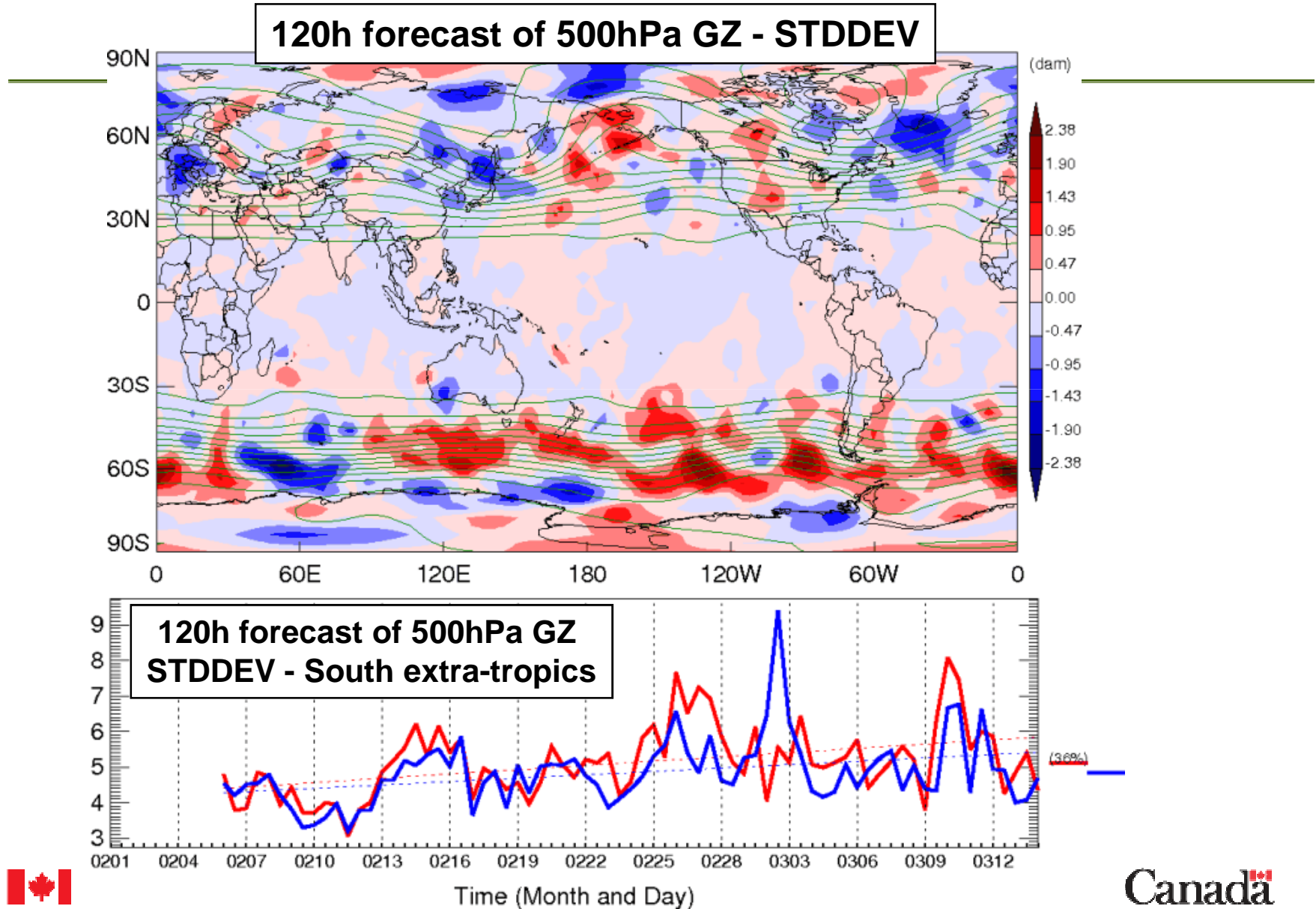
Verification against ERA-Interim analyses – 6 weeks, Feb/Mar 2011

South extra-tropics 500hPa GZ correlation anomaly



Forecast Results: EnVar vs. 3D-Var and 4D-Var

Verification against ERA-Interim analyses – 6 weeks, Feb/Mar 2011



Forecast Results: EnVar vs. 3D-Var and 4D-Var

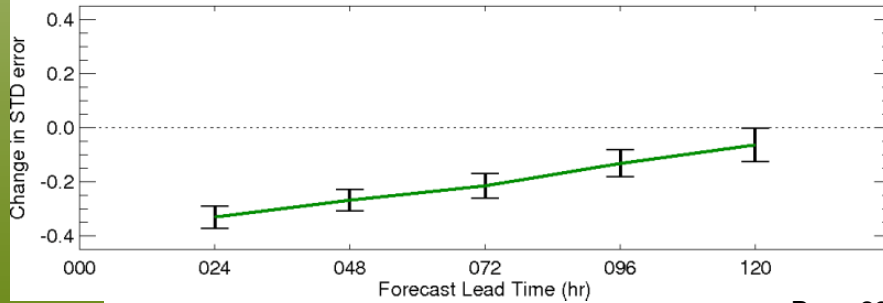
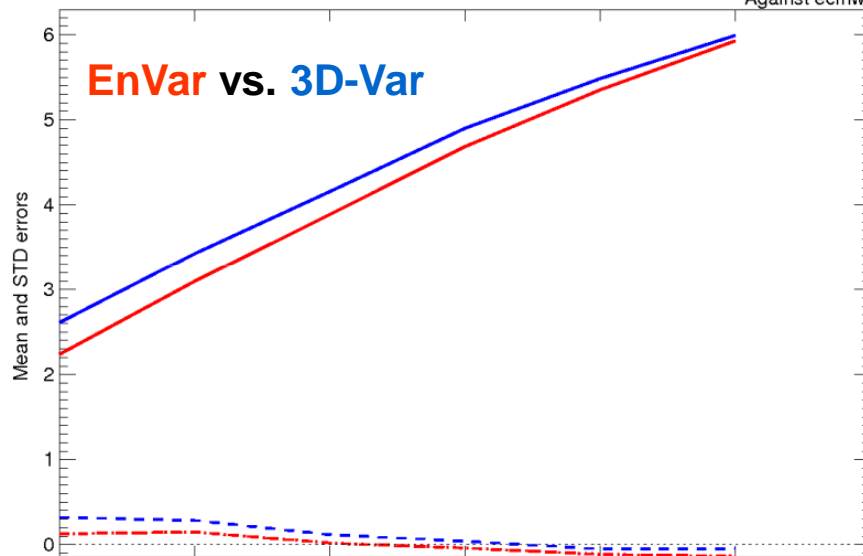
Verification against ERA-Interim analyses – 6 weeks, Feb/Mar 2011

Tropics 250hPa U-wind STDDEV

STD and Mean errors against analyses
2011020100-2011031400

Variable : UU
Level : 250 hPa
Region : tropiques

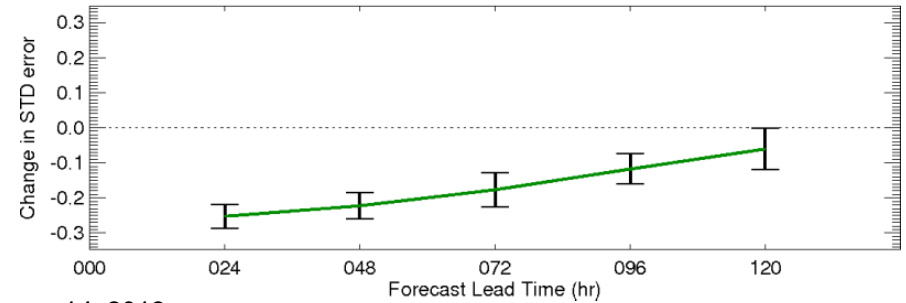
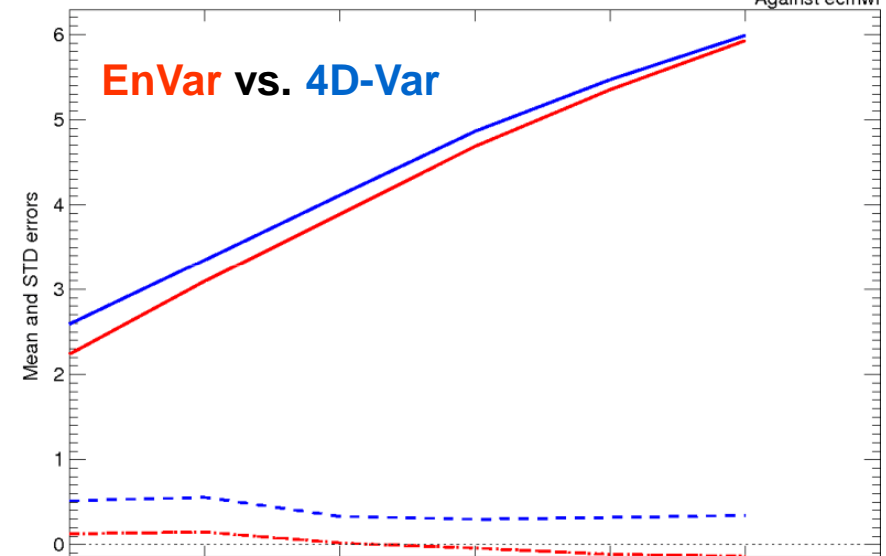
K3H125_J —
KEH125_G —
Against ecmwf



STD and Mean errors against analyses
2011020100-2011031400

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Level : 250 hPa
Region : tropiques

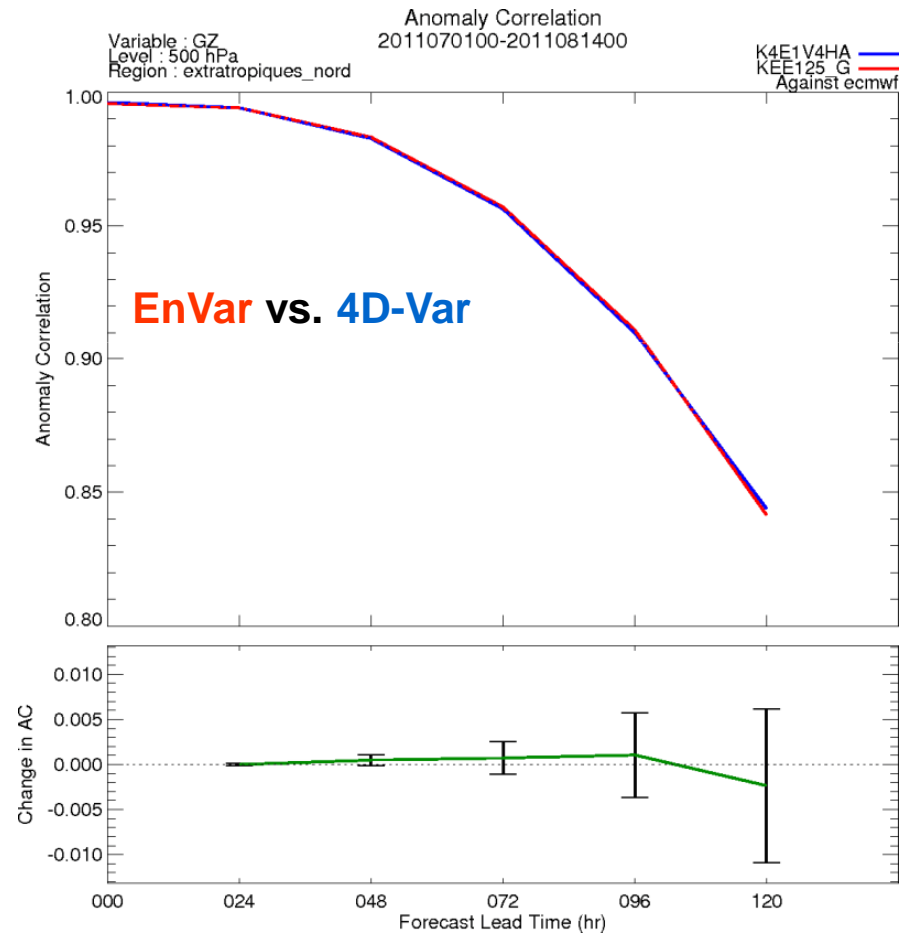
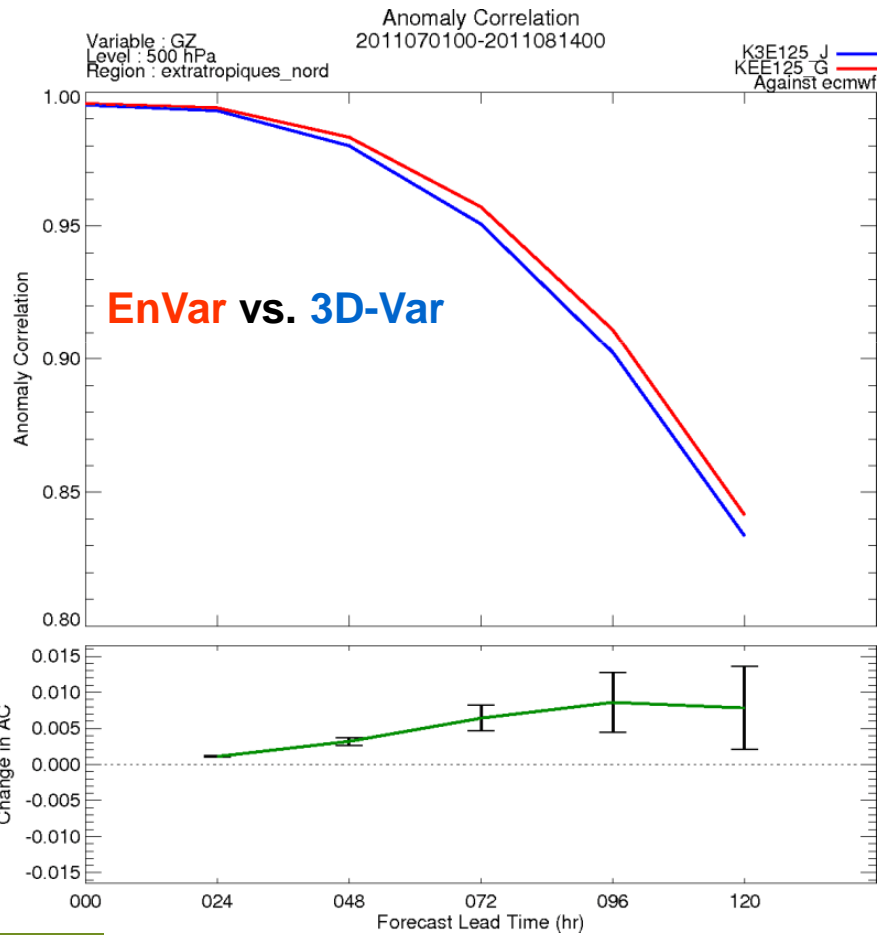
K4H1V4HA —
KEH125_G —
Against ecmwf



Forecast Results: EnVar vs. 3D-Var and 4D-Var

Verification against ERA-Interim analyses – 6 weeks, July-Aug 2011

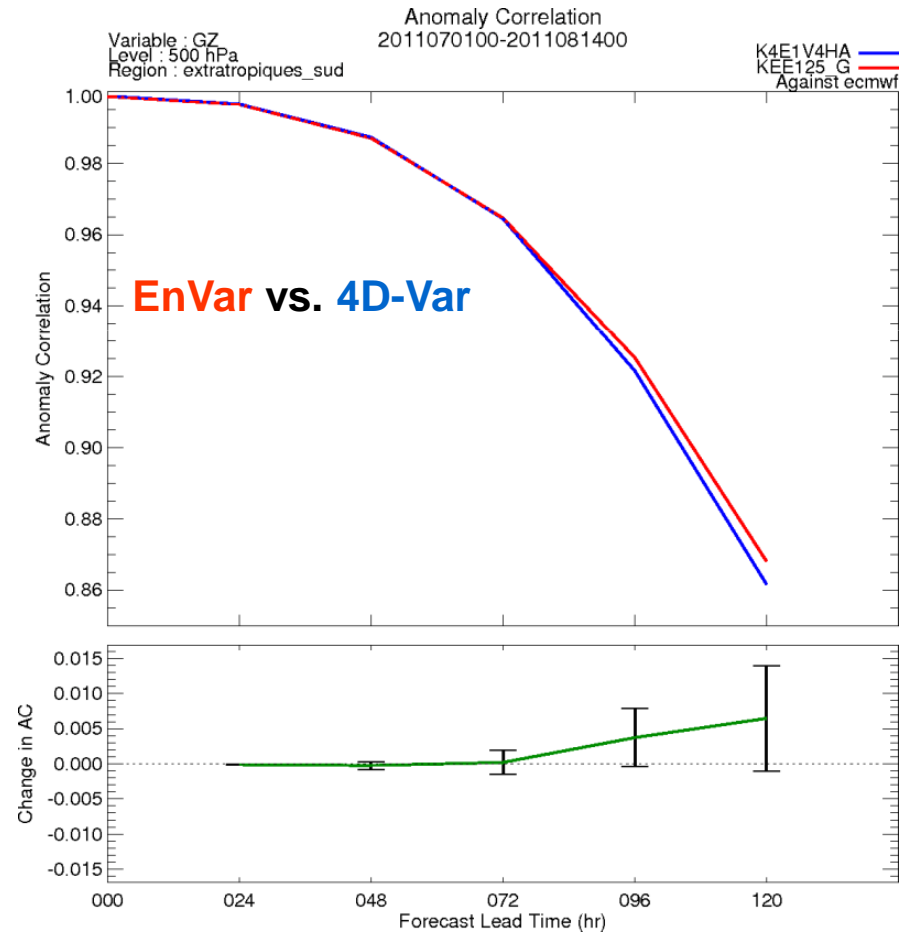
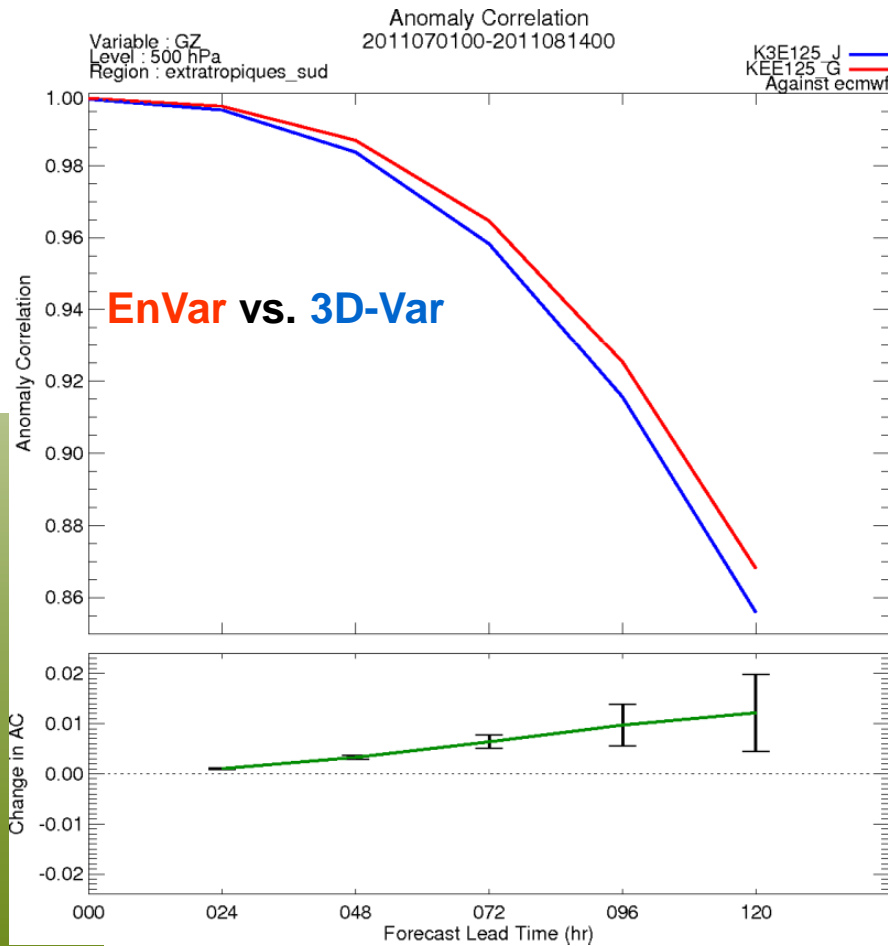
North extra-tropics
500hPa GZ correlation anomaly



Forecast Results: EnVar vs. 3D-Var and 4D-Var

Verification against ERA-Interim analyses – 6 weeks, July-Aug 2011

South extra-tropics
500hPa GZ correlation anomaly



Forecast Results: EnVar vs. 3D-Var and 4D-Var

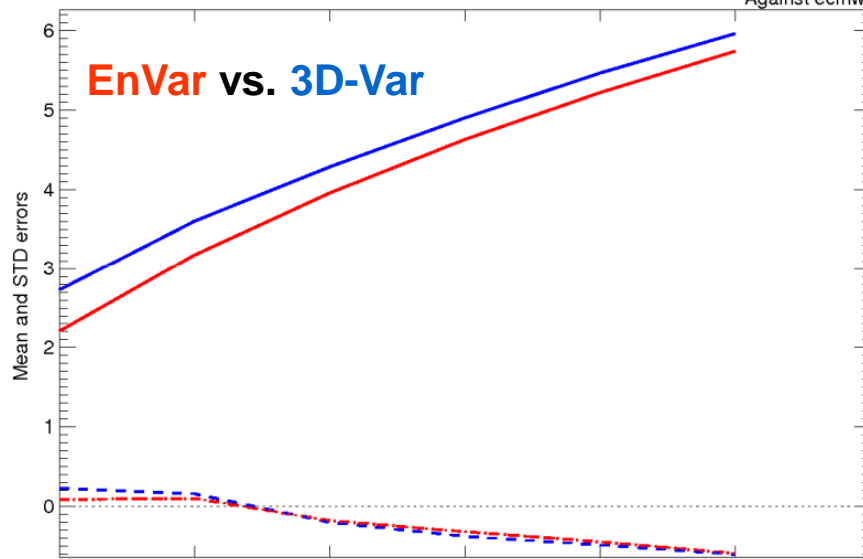
Verification against ERA-Interim analyses – 6 weeks, July-Aug 2011

Tropics 250hPa U-wind STDDEV

STD and Mean errors against analyses
2011070100-2011081400

Variable : UU
Level : 250 hPa
Region : tropiques

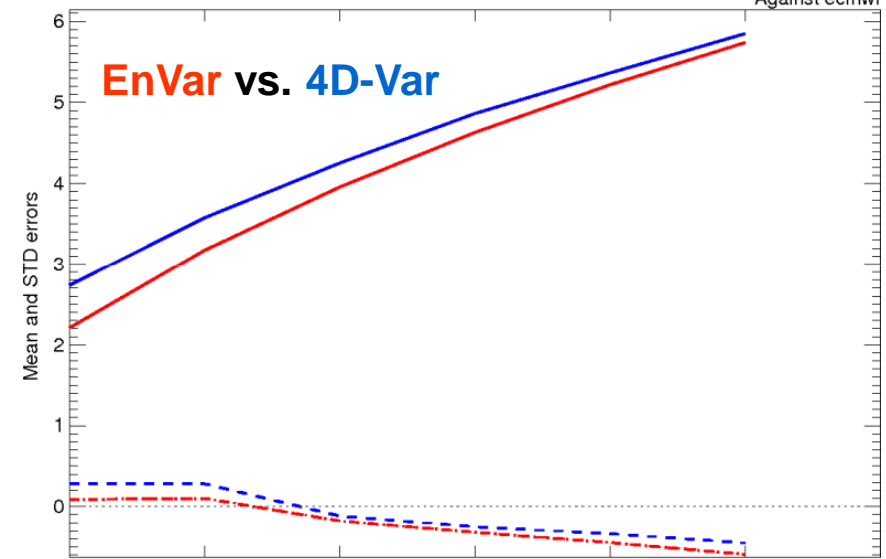
K3E125_J
KEE125_G
Against ecmwf



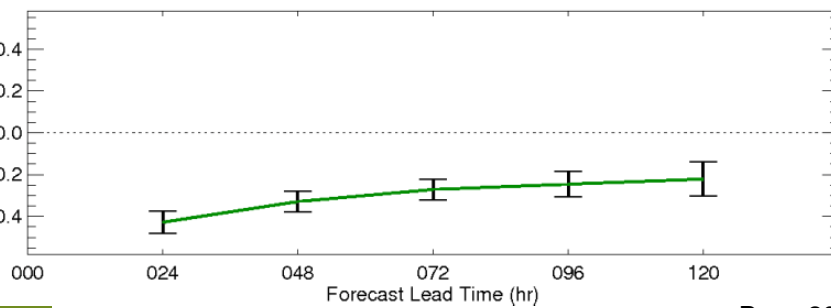
STD and Mean errors against analyses
2011070100-2011081400

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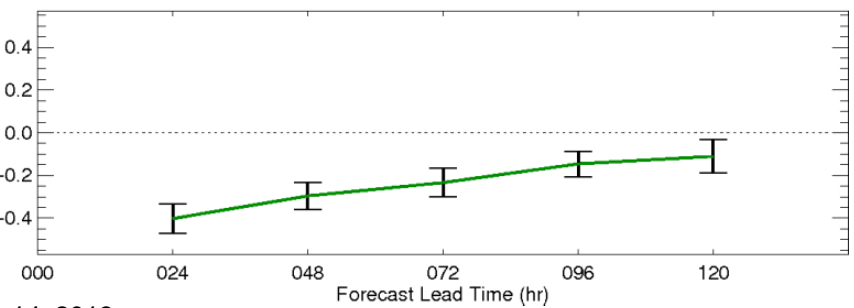
K4E1V4HA
KEE125_G
Against ecmwf



Change in STD error



Change in STD error



Experimental results:

4D-EnVar vs. 3D-EnVar

3D version of EnVar also tested: only uses EnKF flow-dependent ensembles valid at the centre of the 6h assimilation window, instead of every 60 minutes throughout the window

3D-EnVar compared with:

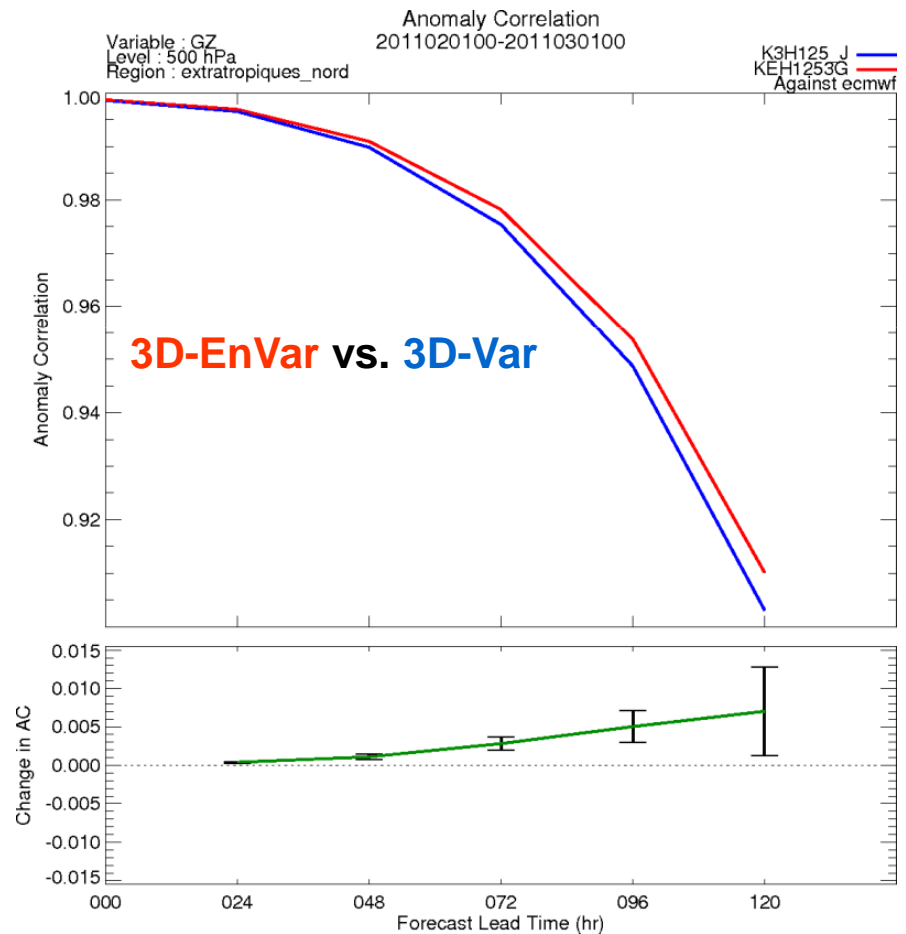
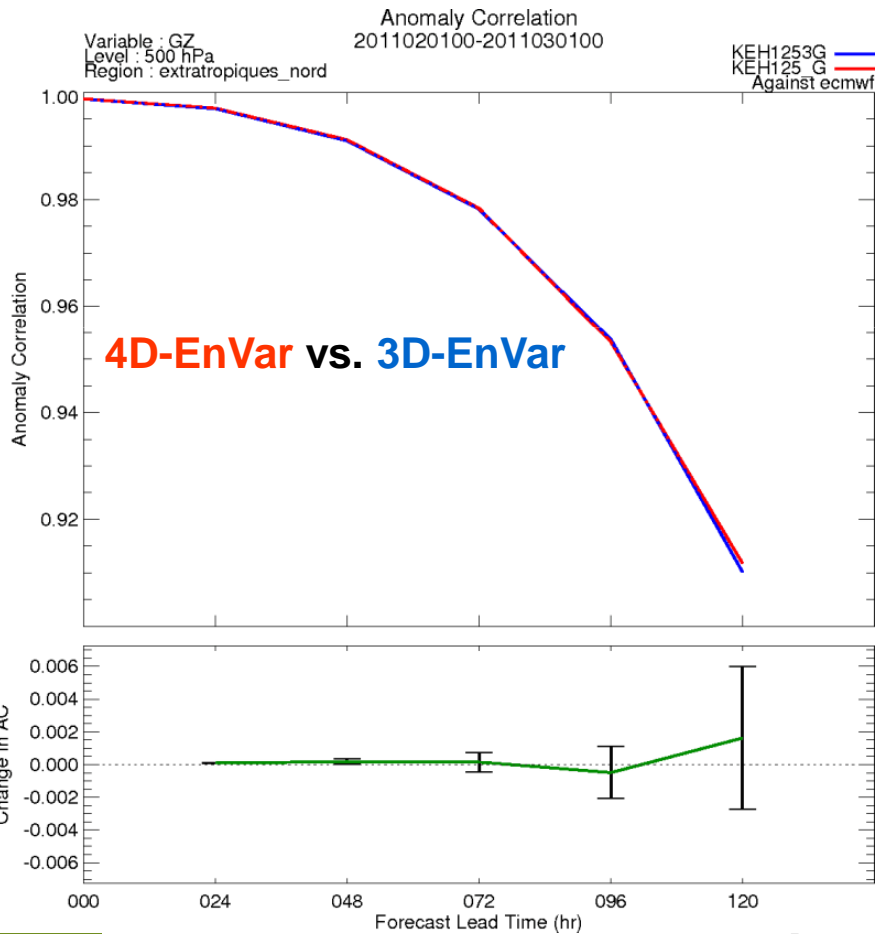
- 4D-EnVar: impact of 4D covariances, and
- 3D-Var: impact of flow dependent vs stationary (NMC) covariances (both 3D)



Forecast Results: 4D-EnVar vs. 3D-EnVar

Verification against ERA-Interim analyses – 4 weeks, Feb 2011

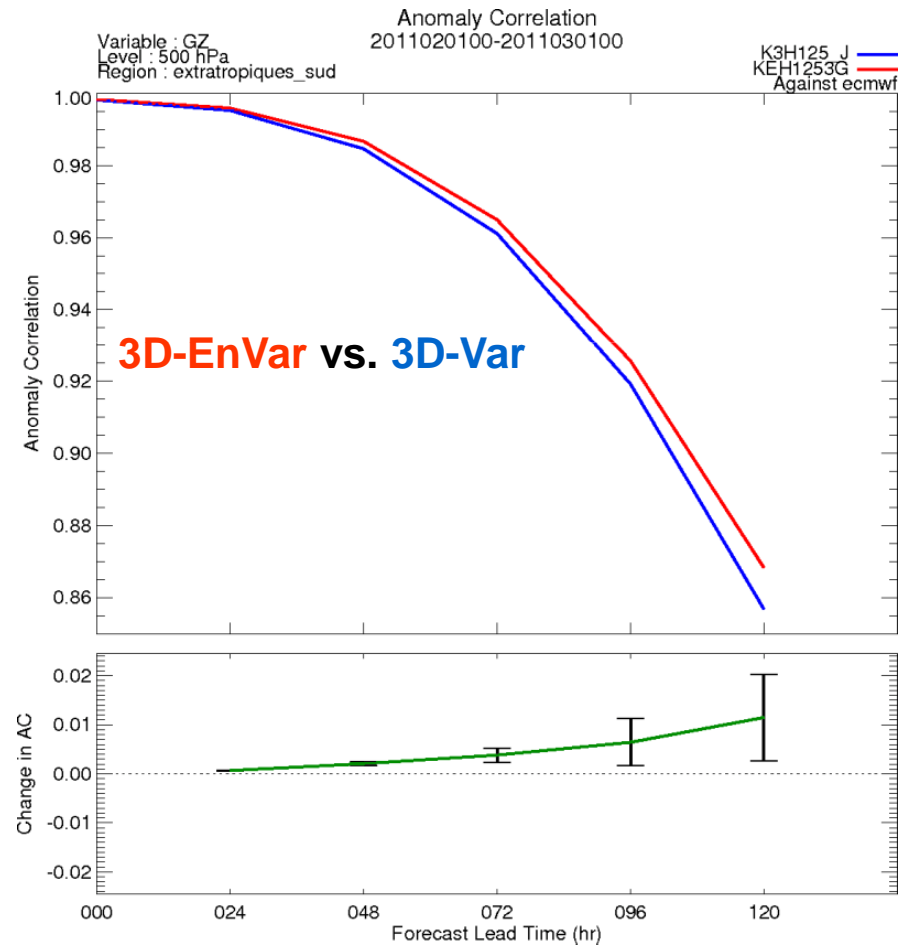
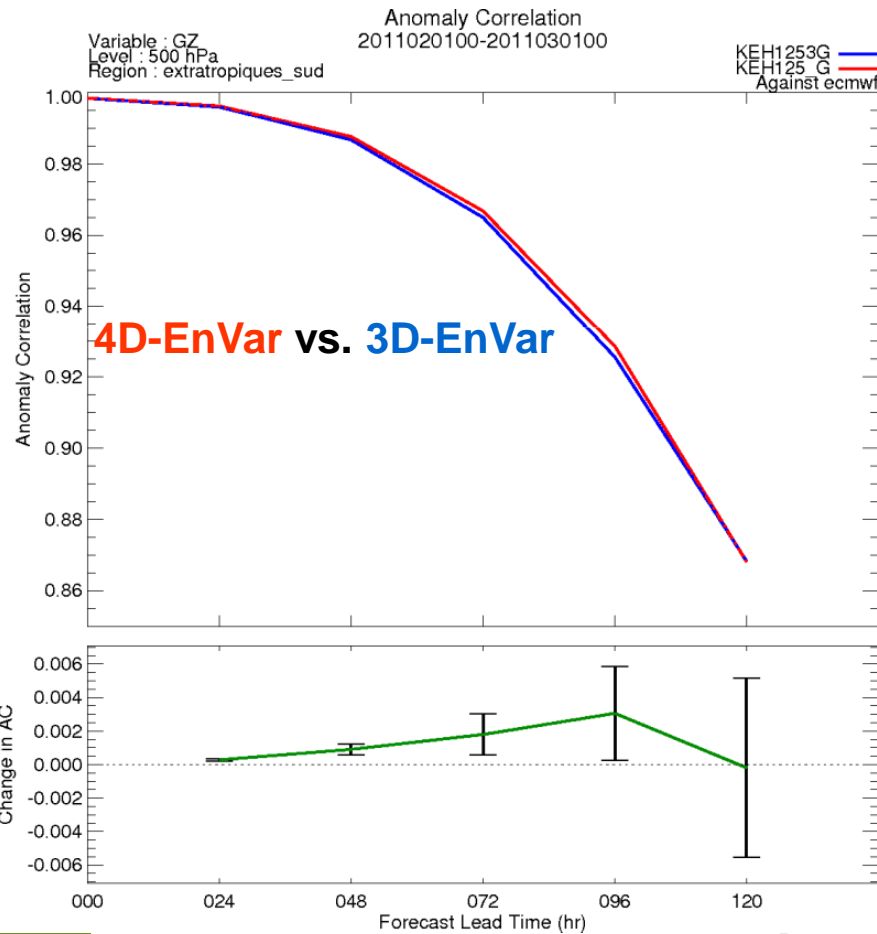
North extra-tropics
500hPa GZ correlation anomaly



Forecast Results: 4D-EnVar vs. 3D-EnVar

Verification against ERA-Interim analyses – 4 weeks, Feb 2011

South extra-tropics
500hPa GZ correlation anomaly



Forecast Results: 4D-EnVar vs. 3D-En-Var

Verification against ERA-Interim analyses – 4 weeks, Feb 2011

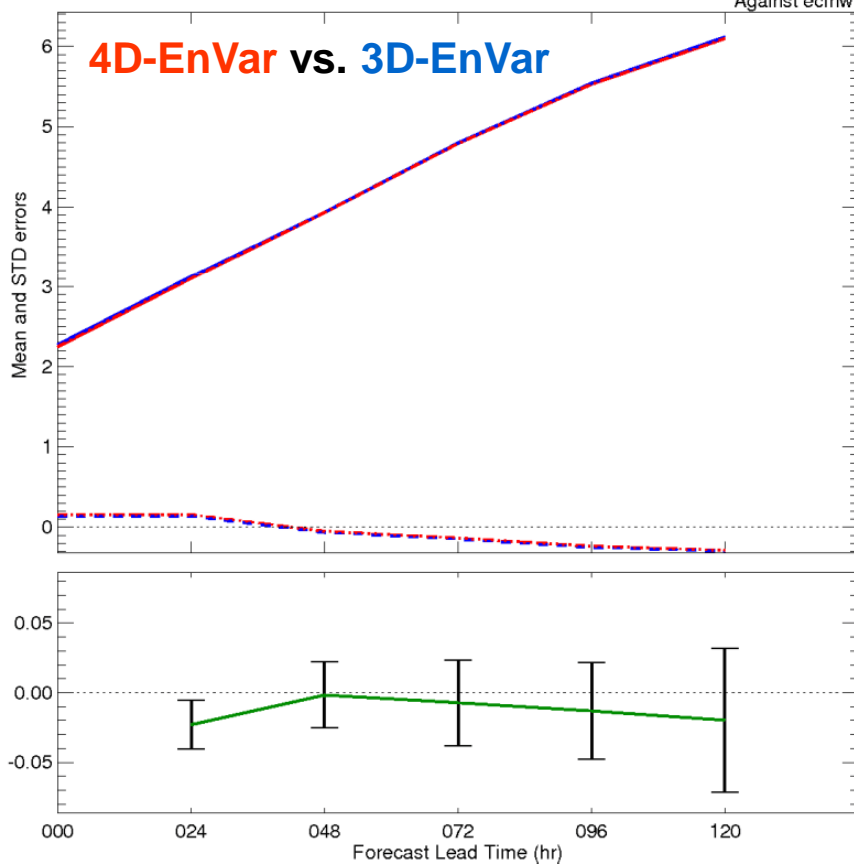
Tropics 250hPa U-wind STDDEV

STD and Mean errors against analyses

Variable : UU
Level : 250 hPa
Region : tropiques

2011020100-2011030100

KEH1253G
KEH125_G
Against ecmwf

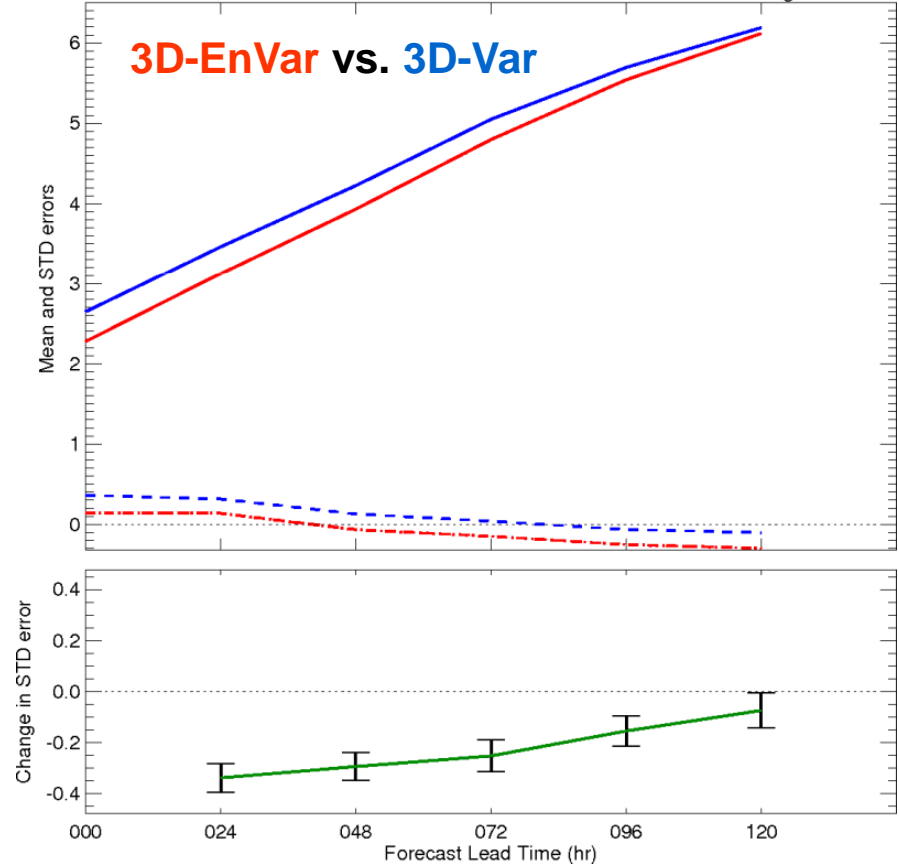


STD and Mean errors against analyses

Variable : UU
Level : 250 hPa
Region : tropiques

2011020100-2011030100

K3H125_J
KEH1253G
Against ecmwf



Conclusions

- Comparison of EnVar with 3D-Var and 4D-Var:
 - EnVar produces similar quality forecasts as 4D-Var below ~20hPa in extra-tropics, significantly improved in tropics
 - above ~20hPa, scores similar to 3D-Var, worse than 4D-Var; potential benefit from raising EnKF model top to 0.1hPa
- EnVar is an attractive alternative to 4D-Var:
 - like EnKF, uses full nonlinear model dynamics/physics to evolve covariances; no need to maintain TL/AD version of model
 - makes use of already available 4D ensembles
 - more computationally efficient and easier to parallelize than 4D-Var for high spatial resolution and large data volumes
 - computational saving allows increase in analysis resolution and volume of assimilated observations; more computational resources for EnKF and forecasts

Next Steps

- Finalize testing EnVar with goal of replacing 4D-Var in operational prediction system during 2013 in combination with other changes:
 - GEM global model on 15km Yin-Yang grid
 - CALDAS: new surface analysis system based on EnKF
 - modified satellite radiance bias correction scheme that gives conventional observations more influence on correction
 - improved use of radiosonde and aircraft data
 - additional AIRS/IASI channels and modified observation error variances for all radiances
 - possibly increased resolution of EnKF 66km → 50km
- Testing of EnVar in regional prediction system as possible replacement of 4D-Var already started

