

# Water vapour profiling by microwave radiometers: absorption model uncertainty and recent advancements

Nico Cimini<sup>1,2</sup>, P. Rosenkranz<sup>3</sup>, M. Tretyakov<sup>4</sup>,  
M. Koshelev<sup>4</sup>, and F. Romano<sup>1</sup>

<sup>1</sup>CNR-IMAA, Italy

<sup>2</sup>CETEMPS, Italy

<sup>3</sup>MIT, USA

<sup>4</sup>IAP RAS, Russia

[domenico.cimini@imaa.cnr.it](mailto:domenico.cimini@imaa.cnr.it)



National Research Council of Italy



# Introduction

Microwave Radiometer (MWR) provides:

- Low vertical resolution Temperature and Humidity profiles
- Integrated water vapor + liquid water path (IWV, LWP)
- high temporal resolution (~1min) and ~all weather

MWR applications require uncertainty characterization:

- Instrument
- Forward model (used for retrievals, validation, QC)
  - Radiative transfer
  - Atmospheric absorption model

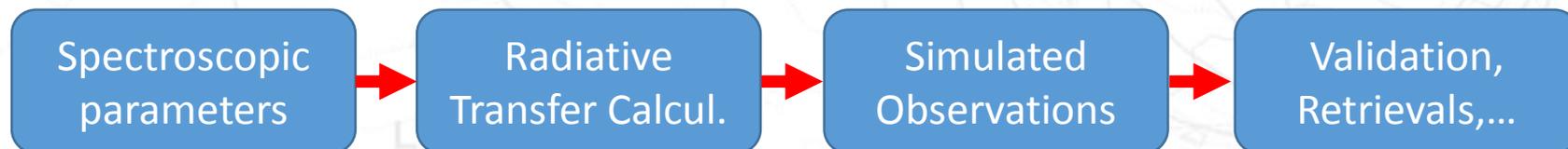
WMO GRUAN (GCOS Reference Upper Air Network)

- Focus: characterizing the atmospheric absorption model uncertainty



# Introduction

- Atmospheric absorption models
  - based on quantum mechanics theory
  - rely on parameterized equations using spectroscopic parameters
- Values of spectroscopic parameters are determined through
  - (i) theoretical calculations
  - (ii) laboratory experiments
  - (iii) field measurements
- Thus are inherently affected by uncertainty
  - Computational and/or experimental
  - Uncertainty propagates...



# Approach

The analysis consists of four steps:

1. **Review state-of-the-art** of spectroscopic parameters and their uncertainties
2. Perform a **sensitivity study** to investigate the dominant uncertainty contribution to radiative transfer calculations
3. Estimate the full **uncertainty covariance matrix** for the dominant parameters
4. **Propagate the uncertainty** covariance matrix to estimate the uncertainty of simulated observations and atmospheric retrievals

# 1. Review state-of-the-art

- Take one RT model and absorption model
  - **Here:** RTE routines (NOAA) updated with Rosenkranz 2017\*
  - But it could also be PAMTRA, ARTS, MonoRTM, AMSUTRAN,...
- List the used parameters (line & continuum absorption)
  - 21 for H<sub>2</sub>O
  - 298 for O<sub>2</sub>
- Uncertainties from 319 parameters were considered

\*<https://doi.org/10.21982/M81013>

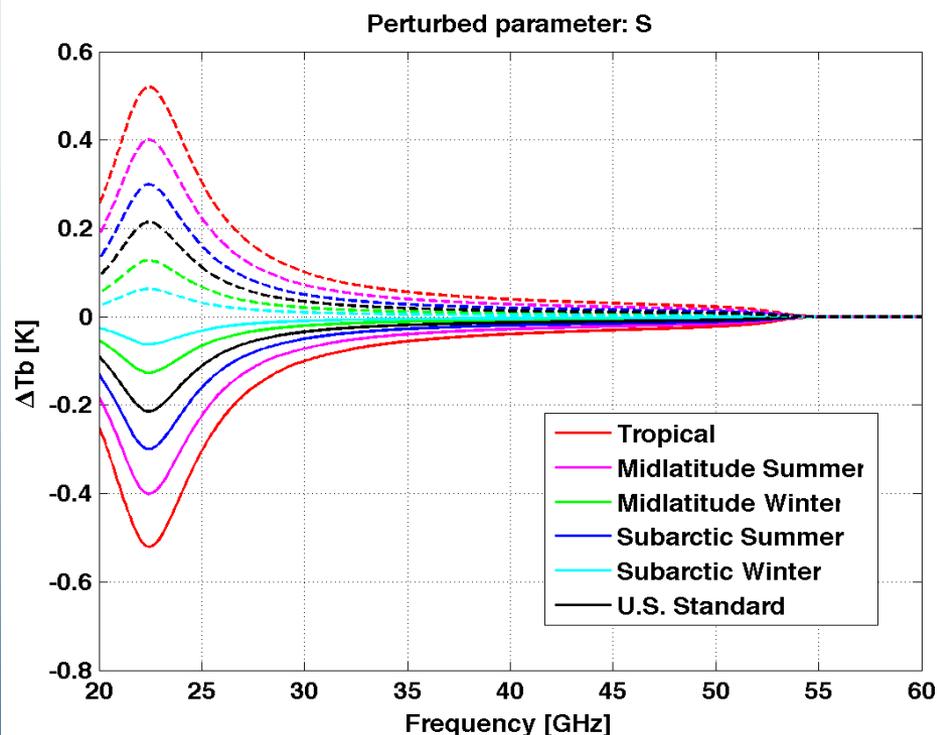


## 2. Sensitivity to model parameter uncertainty

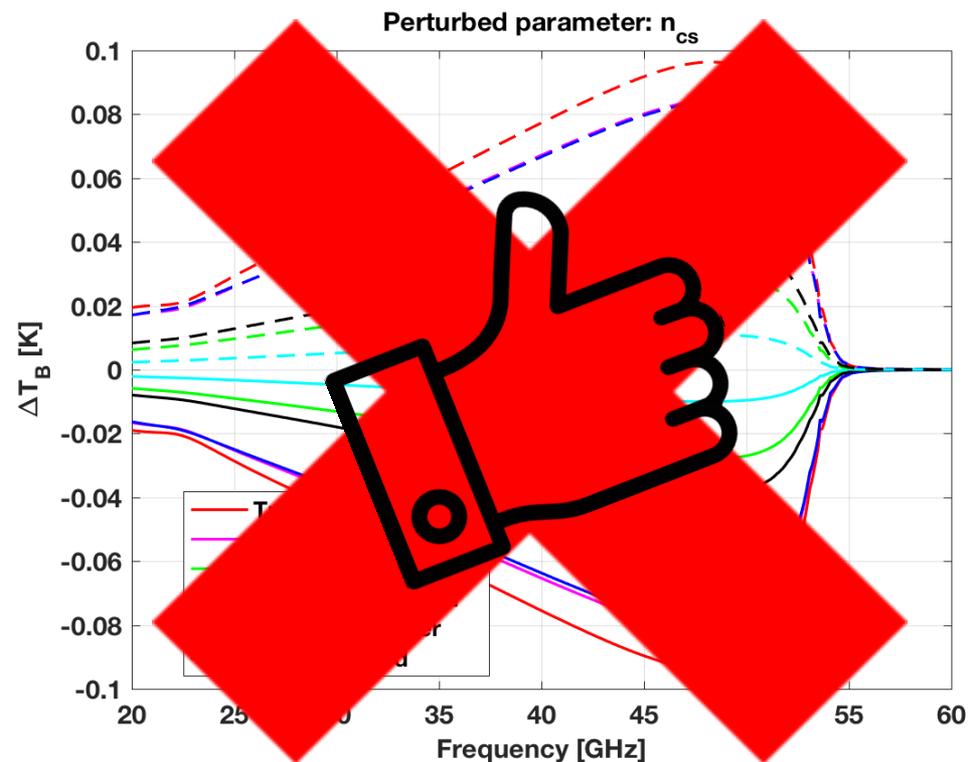
- Sensitivity to spectroscopic parameter uncertainty

$$T_B = F(\mathbf{p}) \quad \Delta T_B = T_B(p_i) - T_B(p_i \pm \sigma_{p_i})$$

WV line strength @ 22.2 GHz



WV self-continuum T exponent



Solid lines correspond to negative perturbation (value - uncertainty)

Dashed lines correspond to positive perturbation (value + uncertainty)

## 2. Sensitivity to model parameter uncertainty

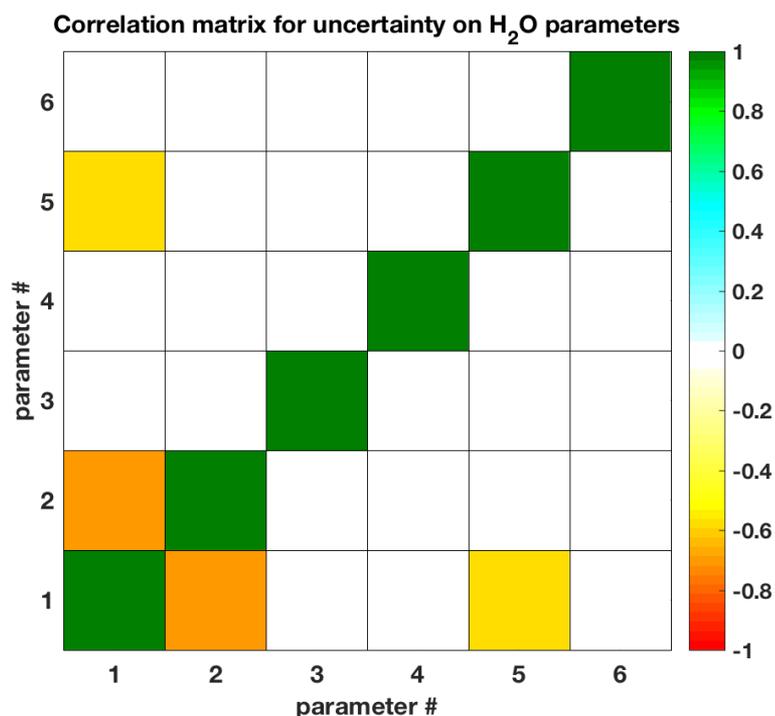
- H<sub>2</sub>O
  - Selected **6** dominating parameters (among **21**)
  - 3 for continuum (Cs, Cf, Xf)
  - 3 for lines ( $\gamma$ , S, shift-broad ratio)
- O<sub>2</sub>
  - Selected **105** dominating parameters (among **298**)
  - 1 for continuum
  - 104 for lines (strength, broadening, mixing, mixing temp. dep.)



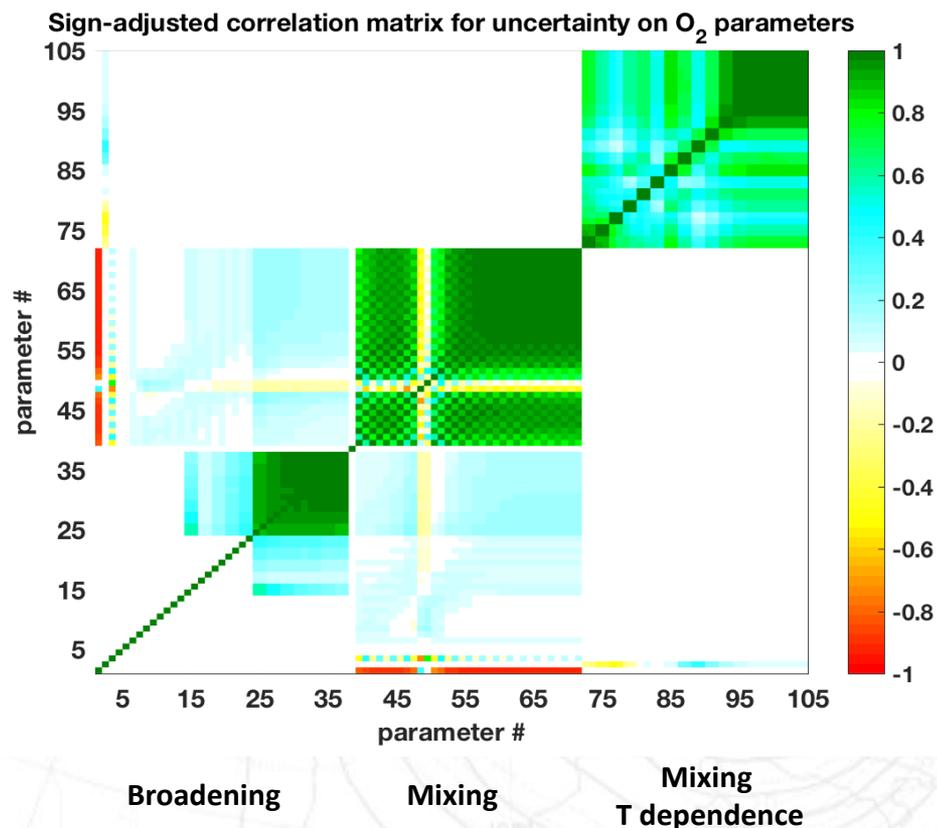
# 3. Uncertainty covariance matrix

- For the **111** dominant terms, we estimated the parameter uncertainty covariance **Cov(p)**

## Water Vapor (6 parameters)



## Oxygen (105 parameters)



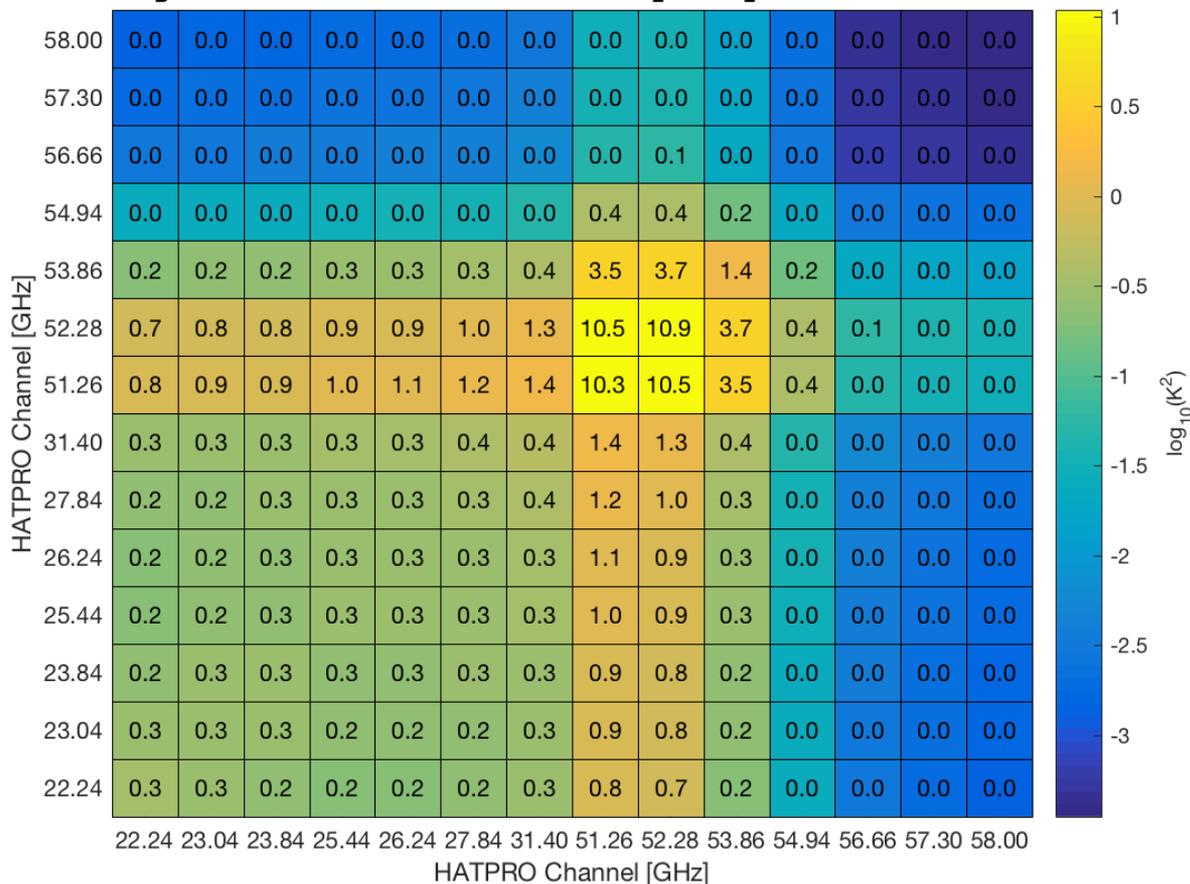
# 4. Uncertainty propagation

- Once  $\mathbf{Cov}(p)$  is determined, we can map into  $\mathbf{Cov}(T_B)$ :

$$\mathbf{Cov}(T_B) \cong K_p * \mathbf{Cov}(p) * K_p^T$$

Total  $T_B$  uncertainty (full matrix)

Full  $T_B$  uncertainty covariance matrix due to  $O_2$  and  $H_2O$  parameter uncertainty

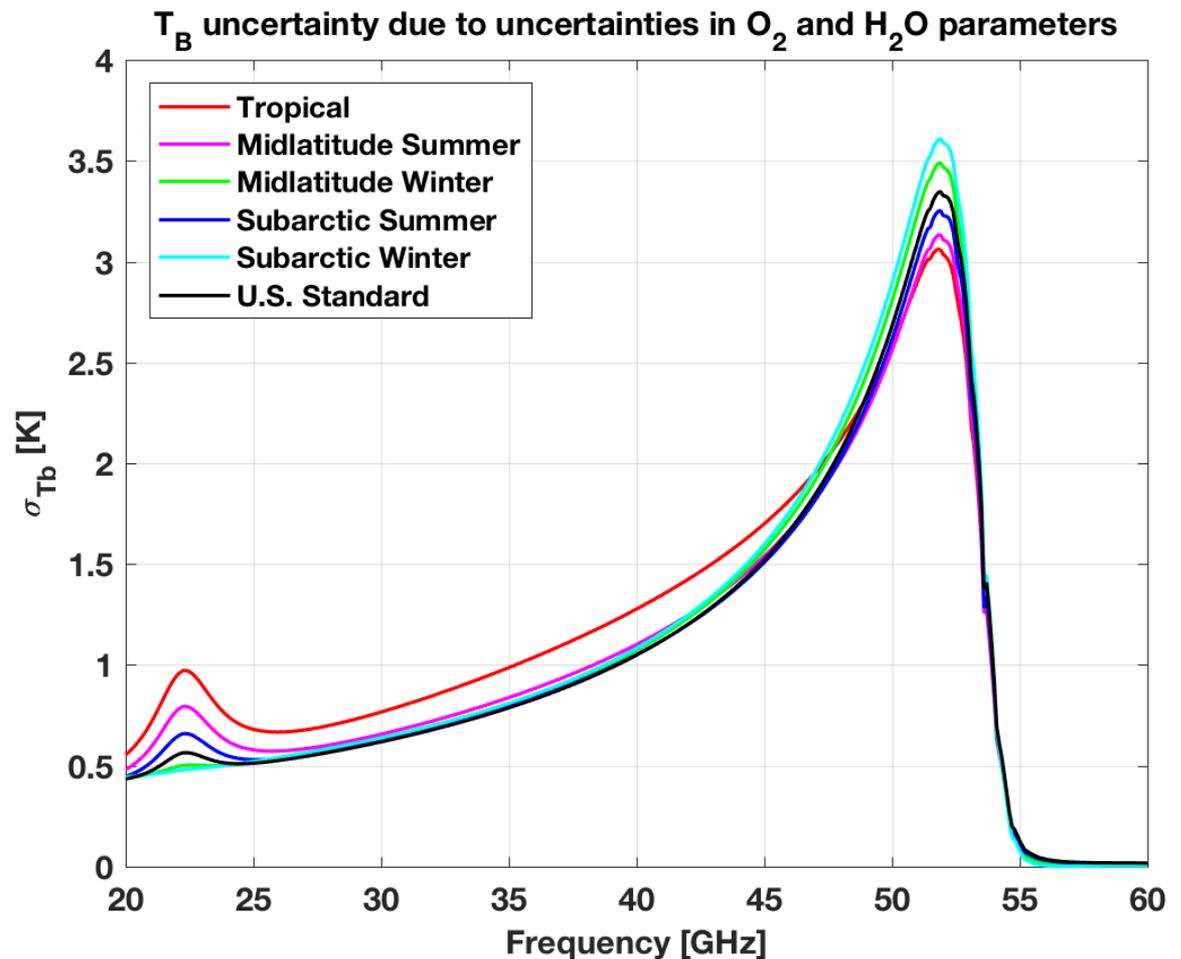


## 4. Uncertainty propagation

- Once  $\mathbf{Cov}(p)$  is determined,  $\mathbf{Cov}(T_B)$  can be easily computed:

$$\mathbf{Cov}(T_B) \cong K_p * \mathbf{Cov}(p) * K_p^T$$

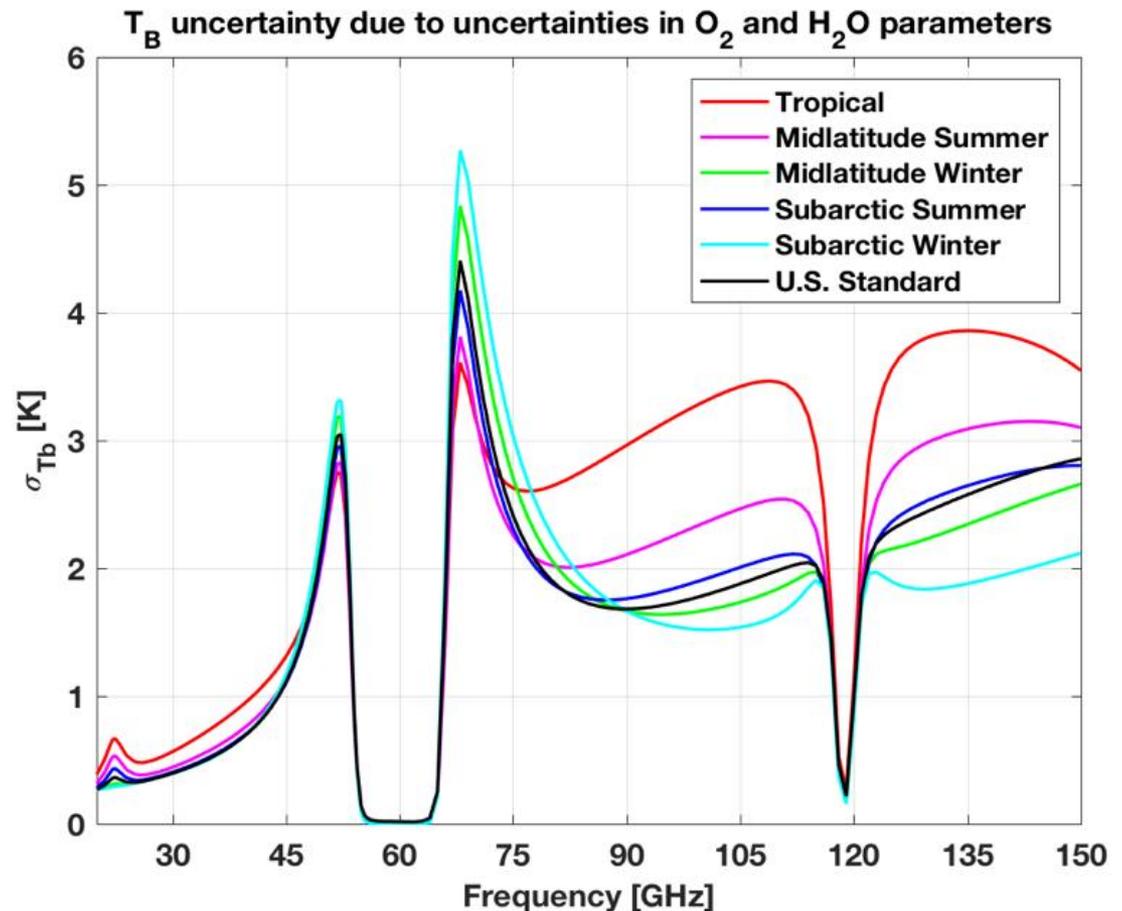
Total  $T_B$  uncertainty  
(diagonal terms)



# Extension to higher frequencies

- Extended to higher frequency (up to 150 GHz)
  - To include 90-150 GHz MWR used for low LWP retrievals
- New sensitivity study: 1 additional parameter to be considered

$n_{cs}$  (wv self continuum T dependence exponent) contributing 0.2-0.6 K to  $T_B$  uncertainty at 70-150 GHz

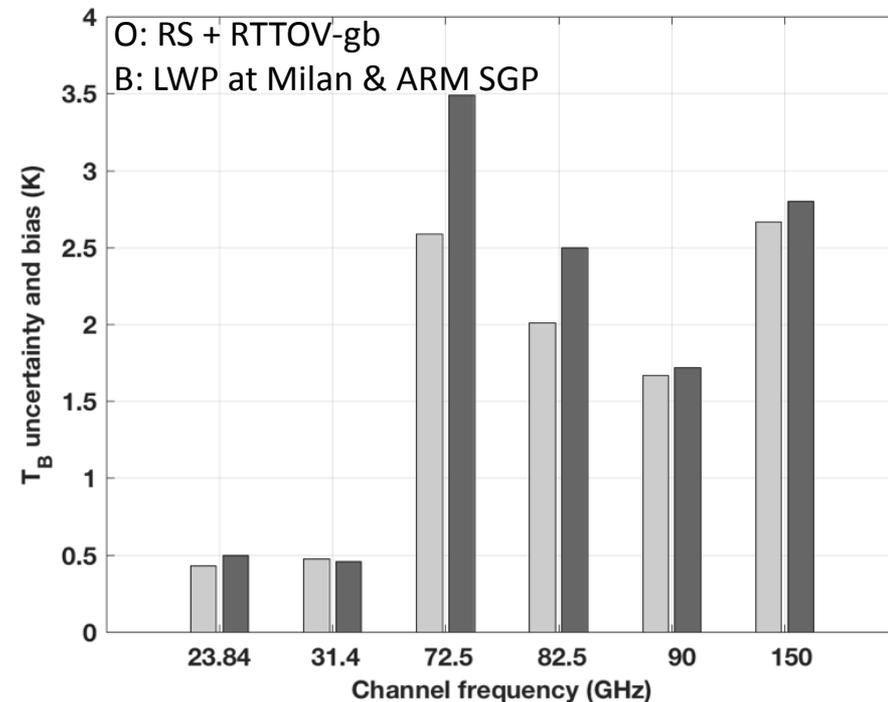
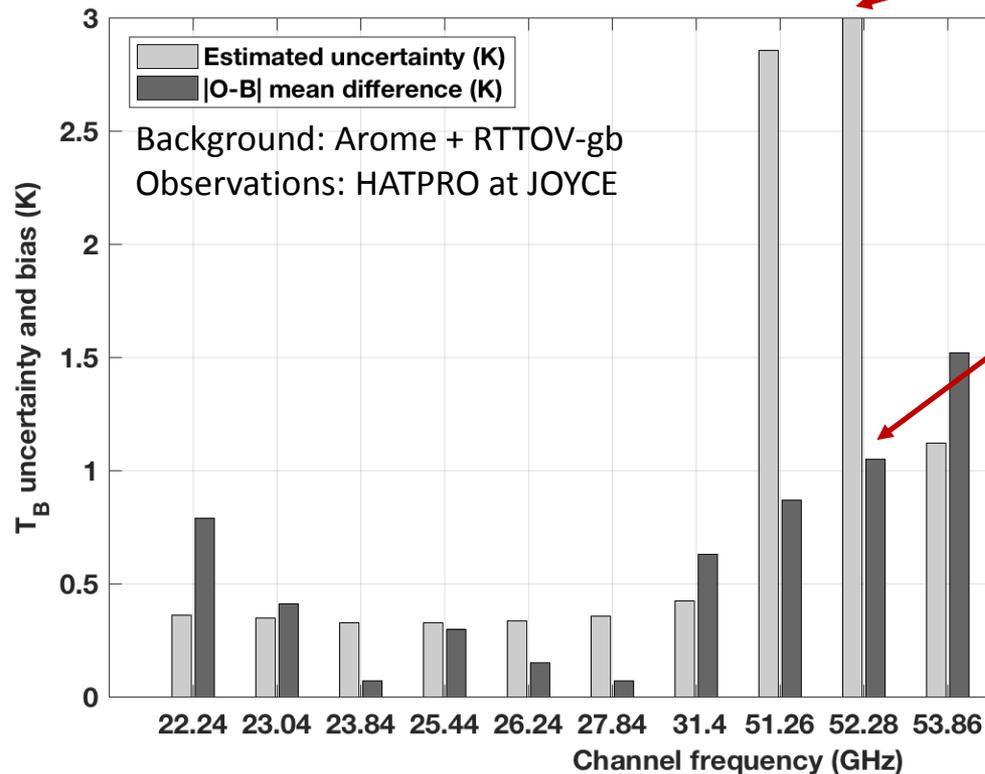


# Absorption model uncertainty

- For a well maintained MWR, absorption model uncertainty explains most of the observation minus simulation (O-S) differences

Abs. mod. uncertainty

O-S differences



# Investigation of systematic uncertainty

- Are there sources of systematic uncertainty in current MW absorption models?
- Speed-dependence of line shapes is currently not considered
  - collision probability (i.e. cross-section) slightly depends on molecular speed
- Recent laboratory measurements provides speed-dependence parameters
  - for 22 and 118 GHz lines (Koshelev et al., 2017; 2018)
  - for 183 GHz lines (Tretyakov 2019, personal comm.)



# Investigation of systematic uncertainty

- Theory for MW speed-dependent line shape has been developed

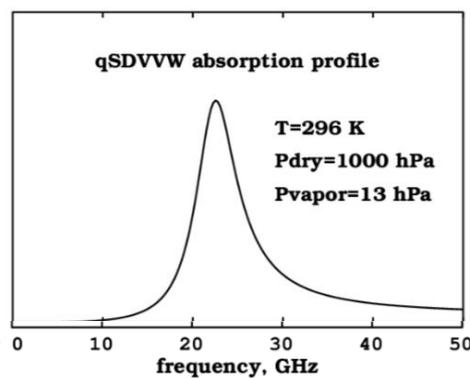
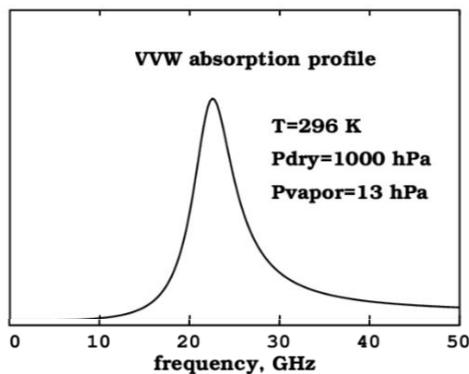
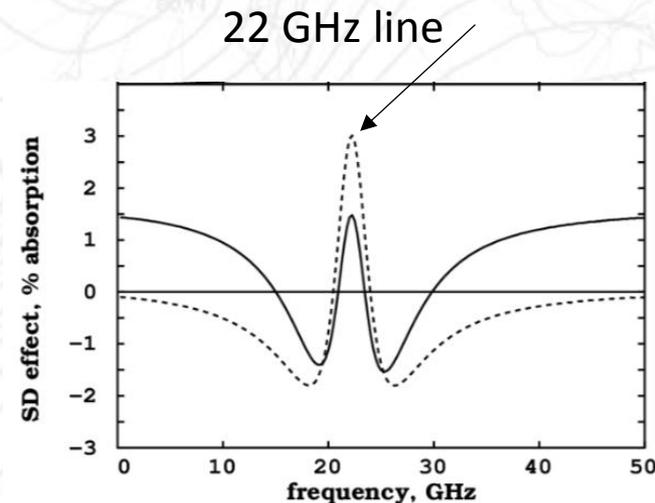
VVW



qSDVVW

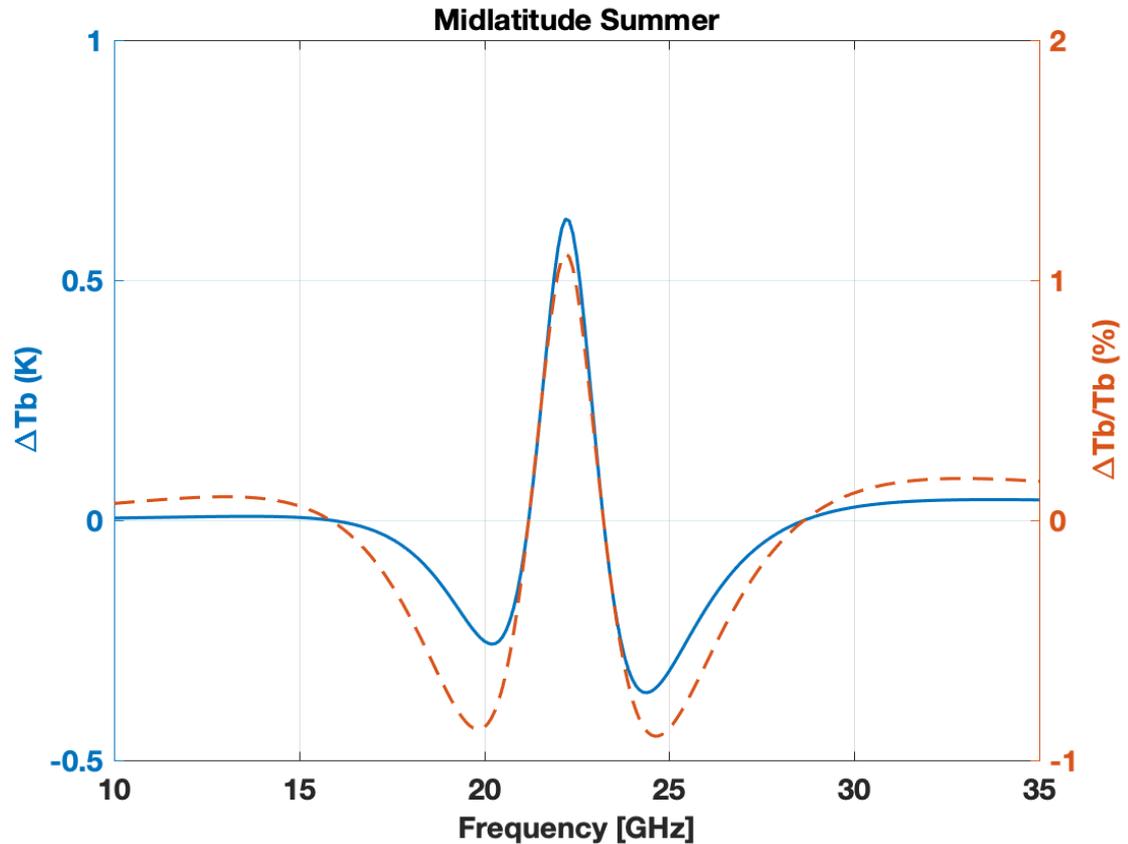
Van Vleck-Weisskopf  
line shape

quadratic Speed-  
Dependent Van  
Vleck-Weisskopf  
line profile



# Investigation of systematic uncertainty

- Does it make a big impact on  $T_B$ ? **Hopefully not!** 😊



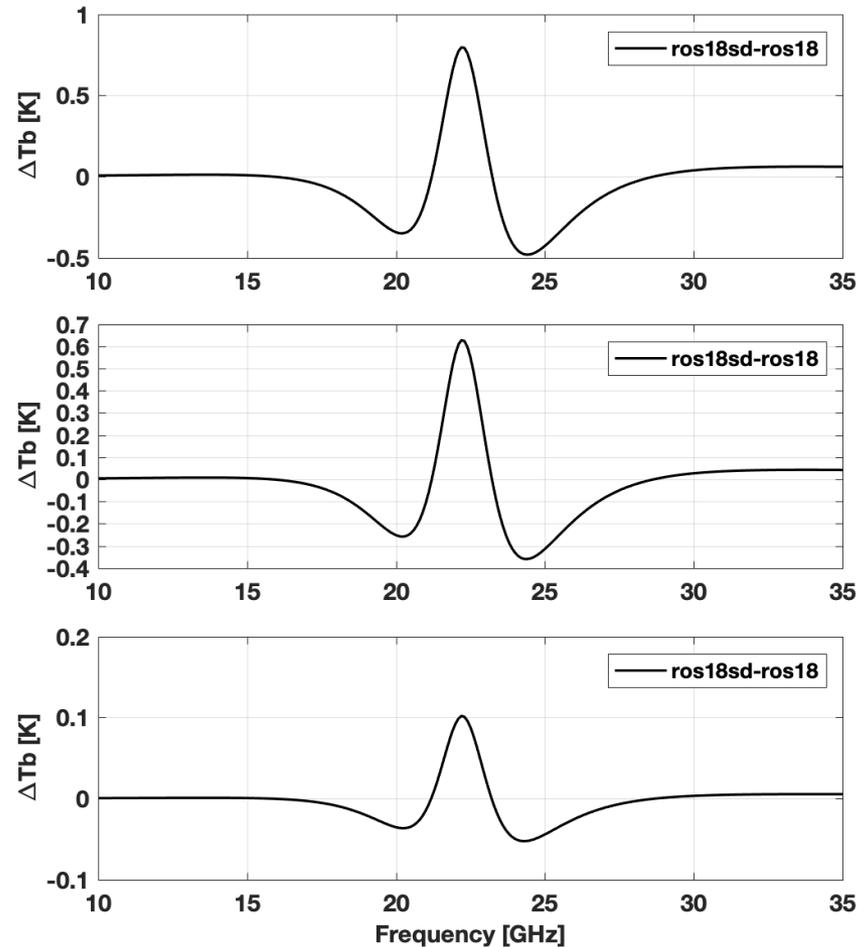
# Investigation of systematic uncertainty

- Does it make a big impact on  $T_B$ ? **Hopefully not!** 😊

Tropical  
~ 2%

Mid-lat Summer  
~ 1%

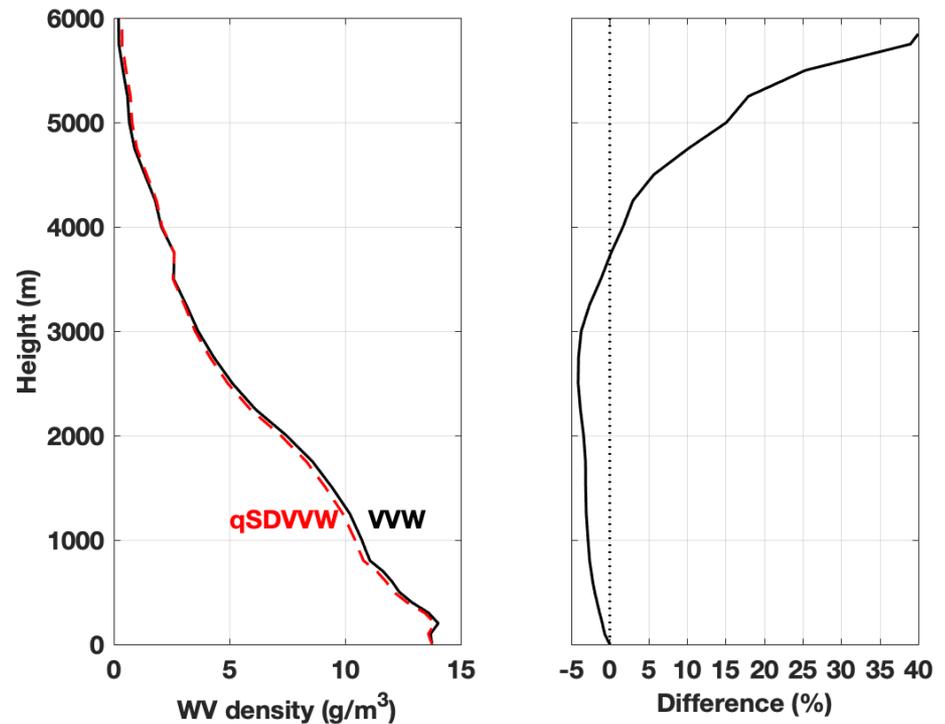
Sub Arctic Winter  
~ 0.5%



# Investigation of systematic uncertainty

- Impact on WV profile retrievals

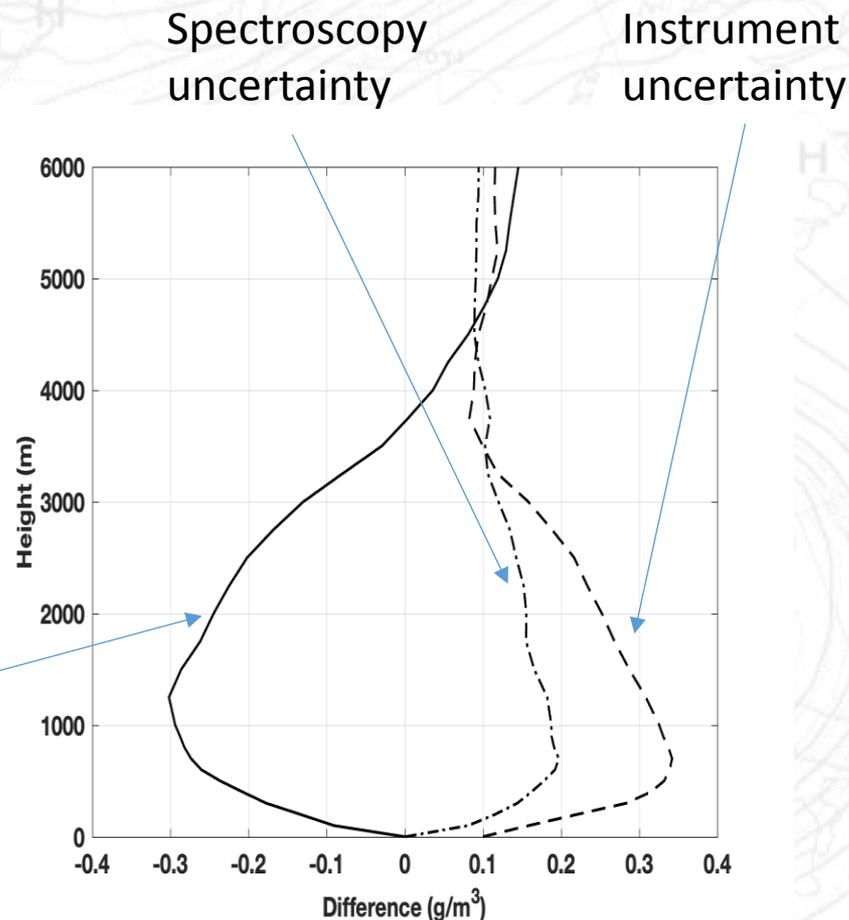
changes sign with height



# Investigation of systematic uncertainty

- Impact on WV profile retrievals
- SD comparable to other uncertainty contributions
- But SD is systematic!
- e.g. it implies a (-1.1%) negative bias in ARM 2-channel IWV retrievals

Speed-dependance contribution



# Summary and future work

- Absorption model uncertainty for ground-based MW simulations has been quantified in the 20-150 GHz range
- A source of systematic uncertainty has been identified and quantified (Speed-Dependent line profile)
  - Impact comparable to other uncertainty contributions
  - Implies ~1% negative bias in IWV 2-channel retrievals
- Currently extending both analysis (spectroscopic uncertainty and speed-dependence) to satellite-based simulations (up to 700 GHz)

**Thank you very much for your attention!**



# GRUAN

- GRUAN: GCOS (Global Climate Observing System) Reference Upper Air Network
- GRUAN delivers reference-quality measurement of essential climate variables (ECVs), for which the uncertainty contributions are carefully evaluated
  - Radiosonde observations (Dirksen et al., 2014)
  - Plans for ground-based MWR profilers
- MWR adds value to GRUAN by providing redundant measurements with respect to radiosondes, but covering the complete diurnal cycle at high (e.g., 1 min)
- Uncertainty for MWR retrievals have been reviewed
  - GRUAN-related GAIA-CLIM project
  - Spectroscopic parameter uncertainty was found to be the least investigated among all



# 3. Uncertainty covariance matrix

Just one example:

- Oxygen line-broadening parameters
  - Coefficients with  $N > N_*$  are determined through linear extrapolation of measured coefficients ( $N < N_*$ )

$$\gamma_N = \gamma_* + (N - N_*)\mu$$

pivot values:  $\gamma_*, N_*$

$N$  is the  $O_2$  rotational quantum number

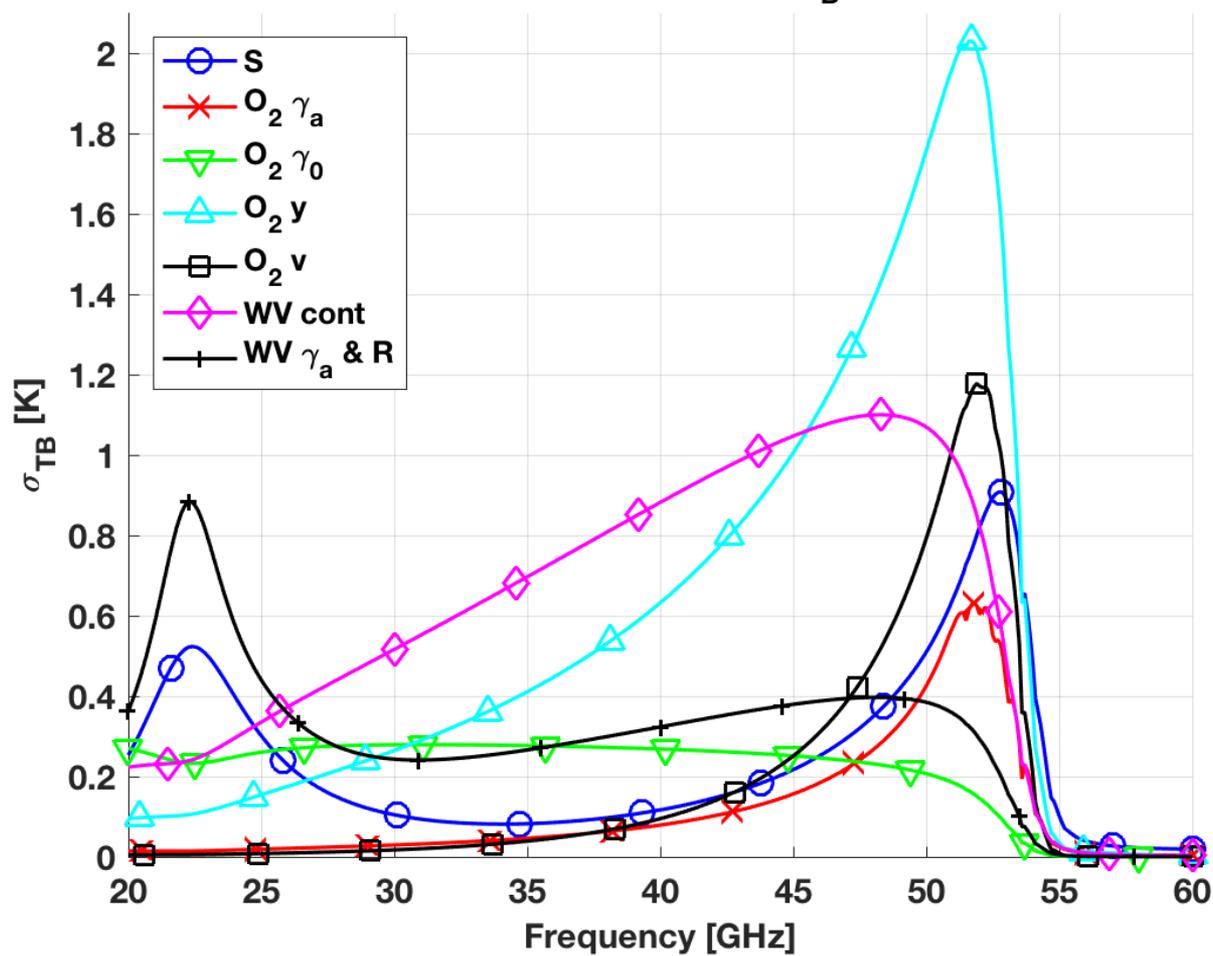
- The extrapolation introduces correlations among the coefficients

# 4. Uncertainty propagation

- Contributions  $T_B$  uncertainty

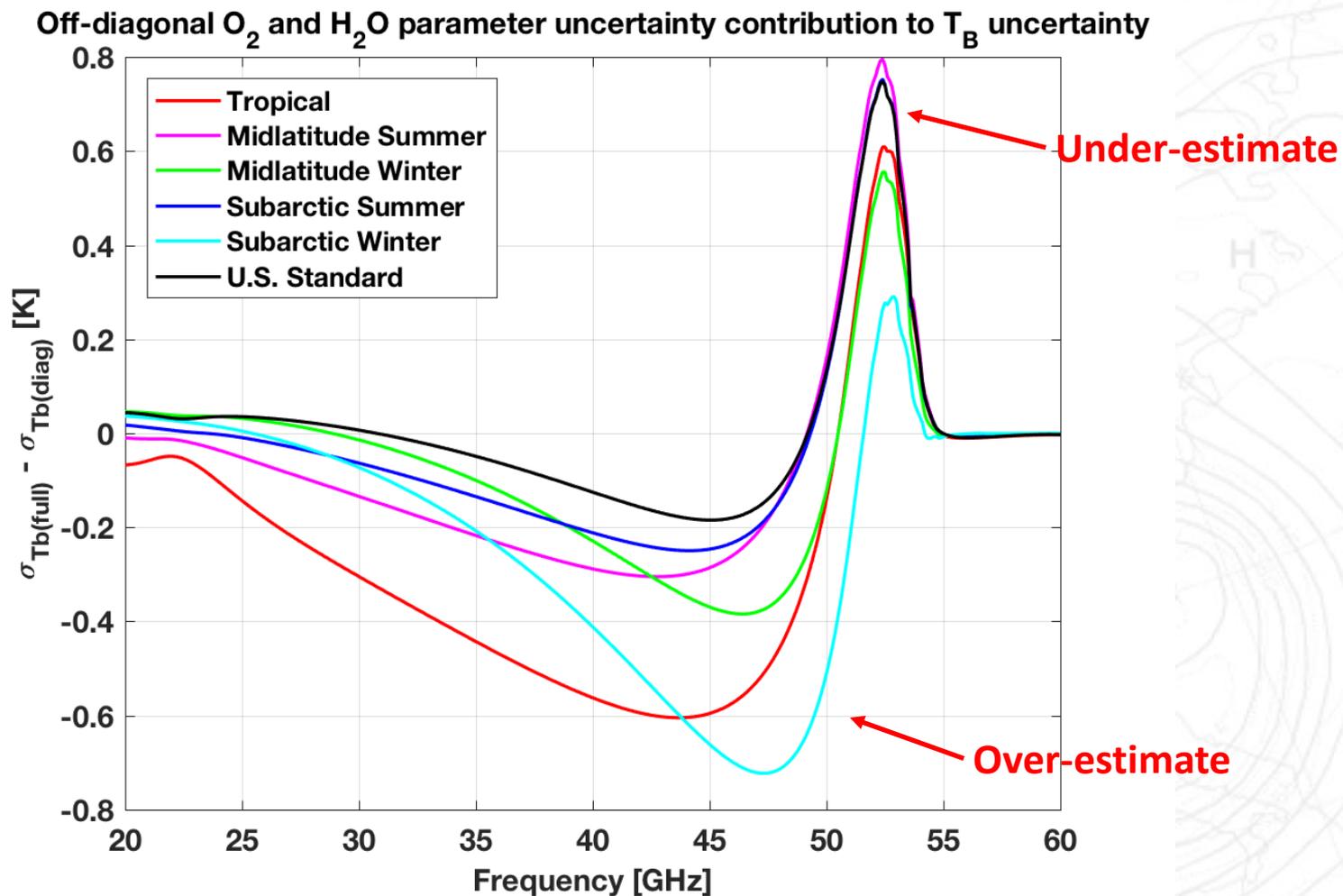
Tropical atmosphere

Parameter contribution to total  $T_B$  uncertainty



# 4. Uncertainty propagation

- Off-diagonal terms contributions to  $T_B$  uncertainty



## 2. Missing MW absorption model uncertainty

### Retrieval impact

$$\mathbf{S} = \mathbf{M} + \mathbf{N} + \mathbf{P}$$

Total retrieval error covariance matrix  
(considering model parameter contribution)

$$\mathbf{M} = \mathbf{D}_y \mathbf{S}_\epsilon \mathbf{D}_y^T$$

Retrieval measurements error covariance matrix

$$\mathbf{N} = (\mathbf{A} - \mathbf{I}) \mathbf{S}_a (\mathbf{A} - \mathbf{I})^T$$

Smoothing error covariance matrix

$$\mathbf{P} = (\mathbf{D}_y \mathbf{K}_b) \mathbf{S}_p (\mathbf{D}_y \mathbf{K}_b)^T$$

Model parameter error covariance matrix

$$\mathbf{D}_y = \partial \mathbf{I}(\mathbf{y}) / \partial \mathbf{y}$$

Contribution function matrix (i.e. Jacobian of the  
inverse model with respect to the measurement)

$$\mathbf{A} = \mathbf{D}_y \mathbf{K}_x$$

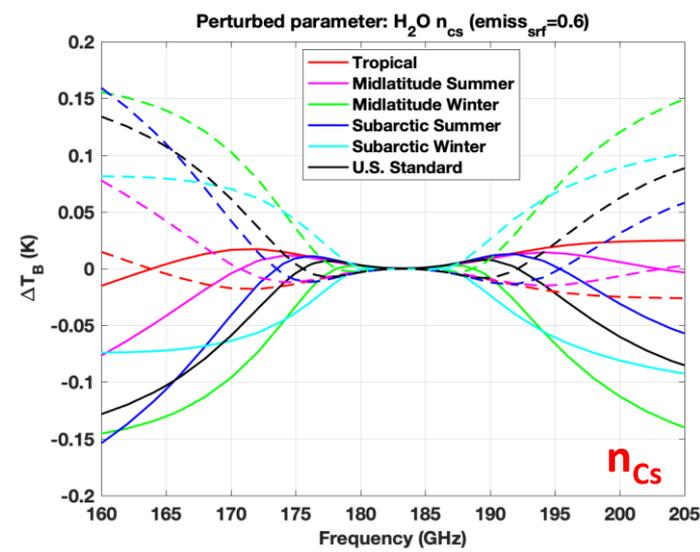
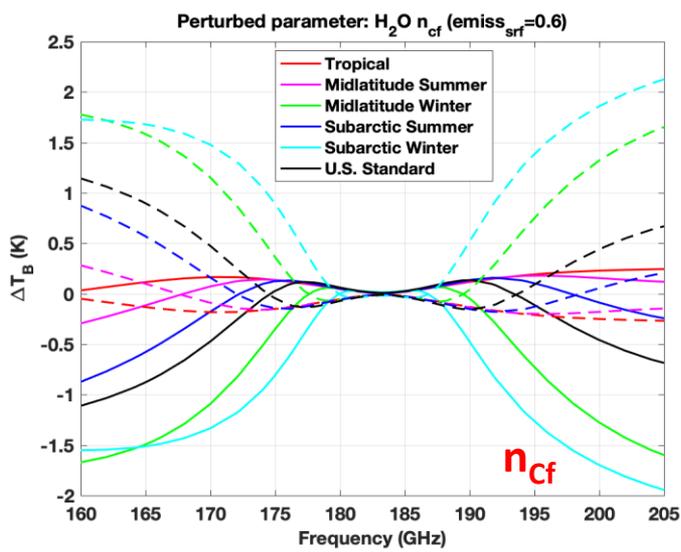
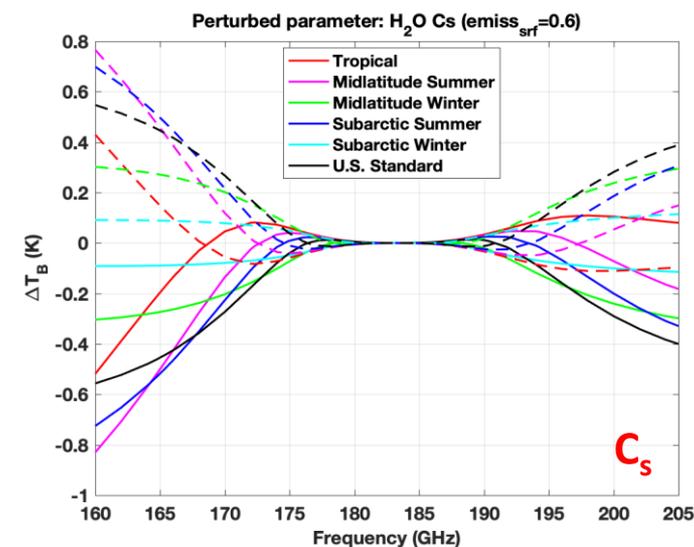
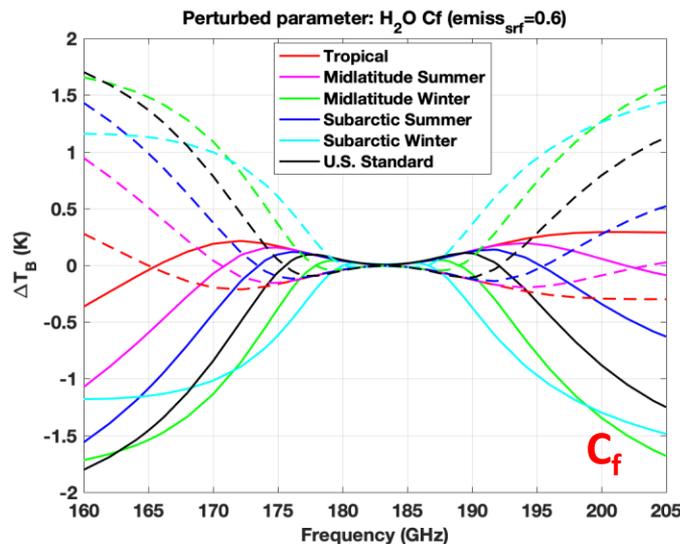
Averaging kernel matrix



# Extending to higher frequency + satellite

- WV continuum coeff. & T expon.

Surface emissivity = 0.6



# Extending to higher frequency + satellite

- WV continuum coeff. & T expon.

Surface emissivity = 0.6

