

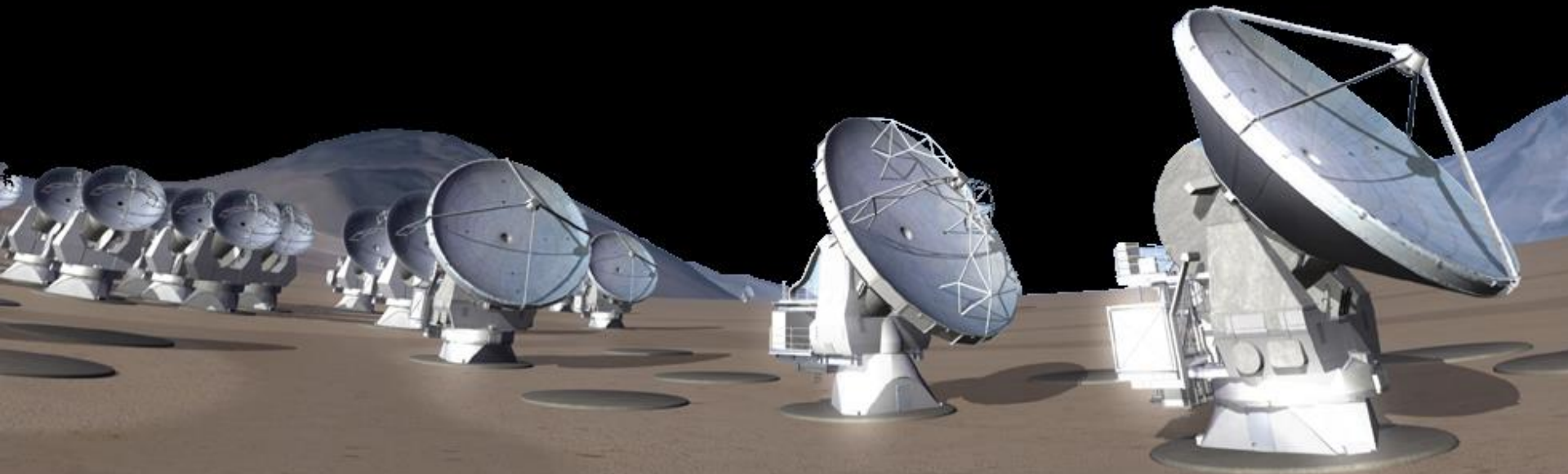


Spectroscopy and gas absorption at mm/submm wavelengths: Recent progress from ground-based observatories



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ASPECTS IN ATMOSPHERIC RT MODELS:

- Background
 - CBR
 - Astronomical source
 - Sea,
 - Land(s),...
- Scattering
 - Single
 - Multiple
 - Shapes of scatterers
 - Refraction indexes
- Polarization
 - Stokes parameters
 - E, B fields
- Spectroscopy
 - Main gases
 - Minor gases
 - Isotopologues
 - Vibrationally excited states
- Vertical profiles
 - Latitude, longitude
 - Day / Night
 - Season
- (Pseudo)continua
 - Collision induced
 - Synchrotron
 - Other
- Special effects
 - Zeeman
 - Stark
 - Other
- Geometry
 - 1D
 - 2D
 - 3D
- Operational constraints:
 - Spectral resolution
 - Fast codes for real time processing
 - Accuracy

3D atmospheric radiative transfer equation (coordinates: z , $\mu=\cos(\theta)$, φ)

$$\mu \frac{dI(z, \mu, \varphi)}{dz} = K(z, \mu, \varphi)I(z, \mu, \varphi) - \int_{-1}^1 d\mu' \int_0^{2\pi} d\varphi' Z(z, \mu, \varphi, \mu', \varphi') I(z, \mu', \varphi') - \sigma(z, \mu, \varphi) B[T(z)]$$

I=(**I**,**Q**,**U**,**V**)^T Radiation field (Stokes column vector)

K 4x4 extinction matrix

Z 4x4 phase matrix (describing scattering)

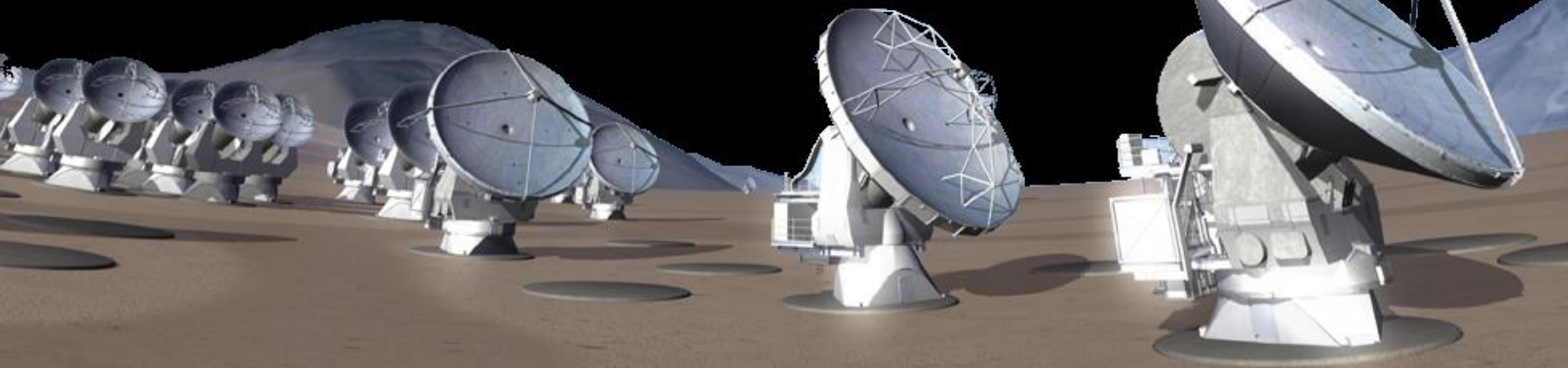
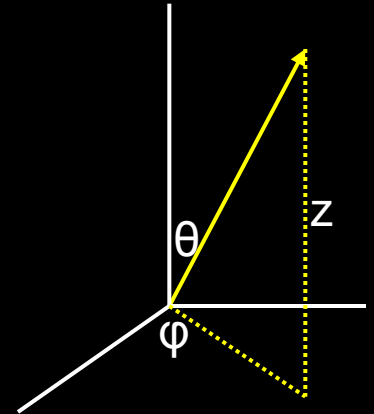
σ 4x1 emission column vector

B Blackbody radiance at temperature T (due to LTE)

Frequency dependence is implicit

$$K_{i1}(z, \mu, \varphi) = \int_{-1}^1 d\mu' \int_0^{2\pi} d\varphi' Z_{i1}(z, \mu, \varphi, \mu', \varphi') + \sigma_i(z, \mu, \varphi), i = 1, \dots, 4$$

Detailed energy balance

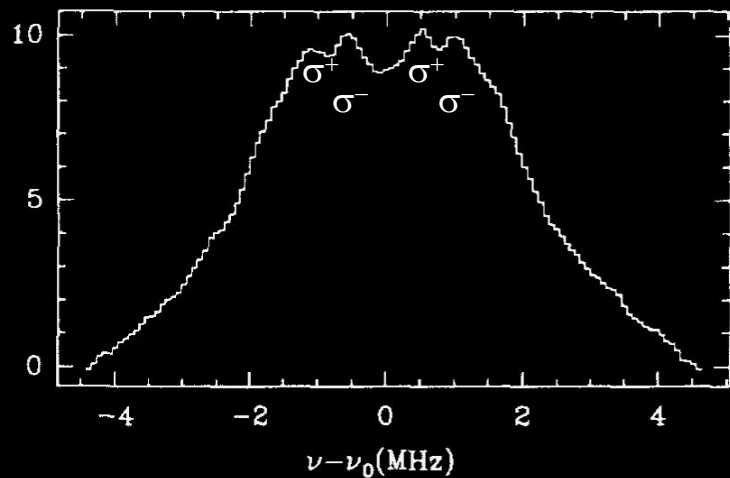


Another way of performing the radiative transfer: Propagate fields and take the average of the Poynting's vector

$$E_z = \exp[ikz(I + N_z 10^{-6})]E_0$$

We use this approach to study polarization introduced in the gas phase by Zeeman splitting on O₂ lines

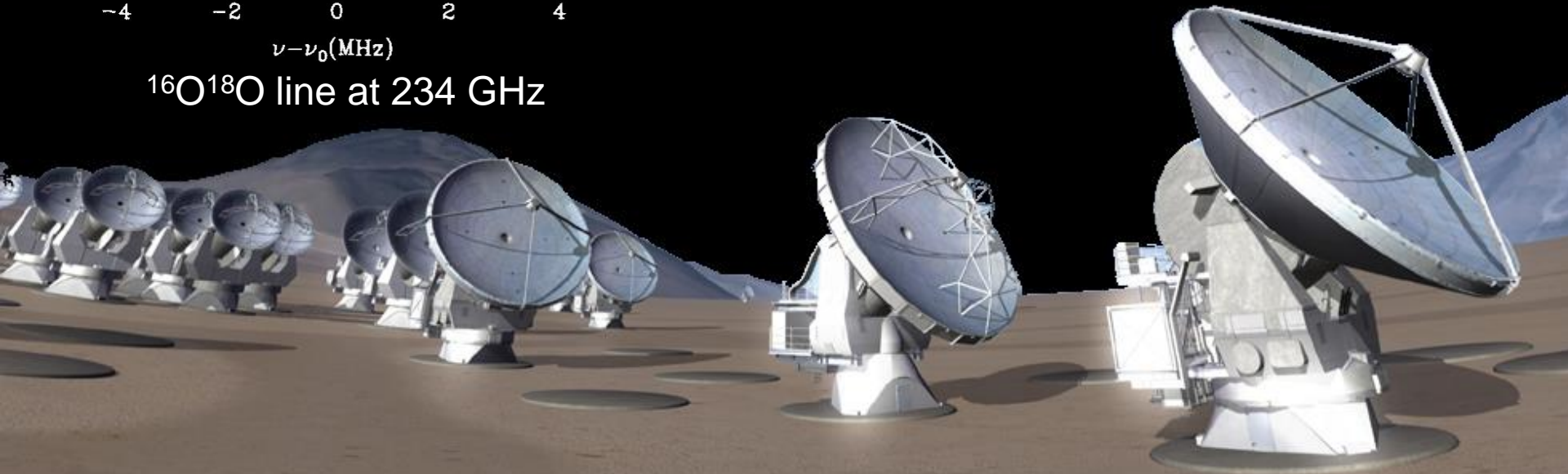
Refractivity is a complex matrix



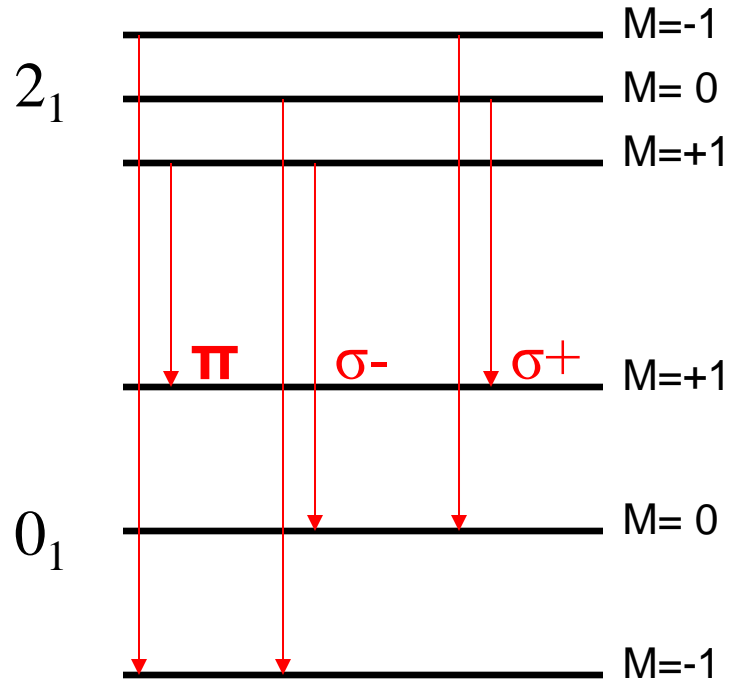
¹⁶O¹⁸O line at 234 GHz

$$\begin{bmatrix} N_0 \sin^2 \phi + (N_+ + N_-) \cos^2 \phi & -i(N_+ - N_-) \cos \phi \\ i(N_+ - N_-) \cos \phi & N_+ + N_- \end{bmatrix}$$

Angle between direction of propagation and geomagnetic field



N_J $^{16}\text{O}^{18}\text{O}$ $v=0$



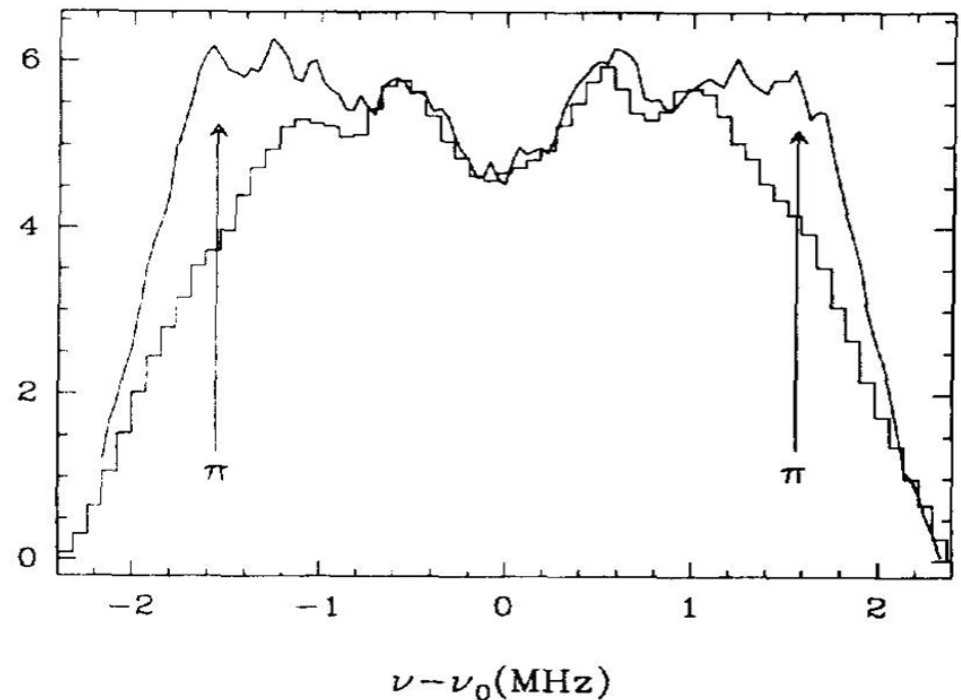
$$\Delta\nu(\text{GHz}) = 14.015 \cdot 10^{-6} H_{\mu T}(M_u + 2M_l)$$

We should expect differences in the line profile depending on the line of sight, the type of polarization detected, and the orientation of our detector with the geomagnetic field.

Transitions π ($\Delta M=0$): Radiation linearly polarized in the direction of the geomagnetic field.

Transitions σ ($\Delta M=\pm 1$): Radiation circularly polarized (right-hand or left-hand in the plane perpendicular to the direction of the geomagnetic field).

$\Delta T_{A,\text{corr}}(\text{K})$



Under clear atmosphere

$$\frac{dI_\nu(s')}{ds} = -I_\nu(s') + B_\nu(T[s'])$$

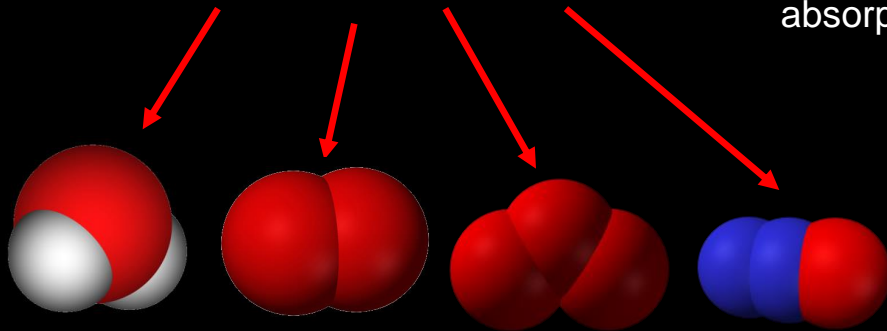
s' coordinate along the path;
 B_ν source function;
 $d\tau_\nu = \kappa_\nu ds$ differential opacity.

$$(\kappa_\nu)_{lu} = \frac{8\pi^3 N_\nu}{3hcQ} \left(e^{-E_l/kT} - e^{-E_u/kT} \right) \cdot |\langle u | \mu | l \rangle|^2 f(\nu, \nu_{l \rightarrow u})$$

gas-phase absorption

Line-by-line
absorption

Collision-induced absorption
(CIA)



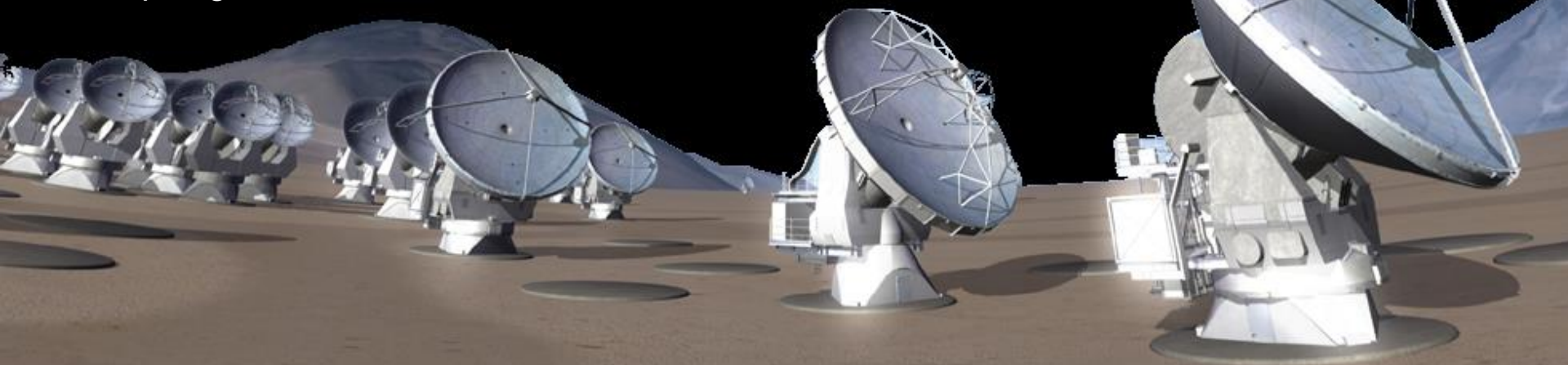
H_2O

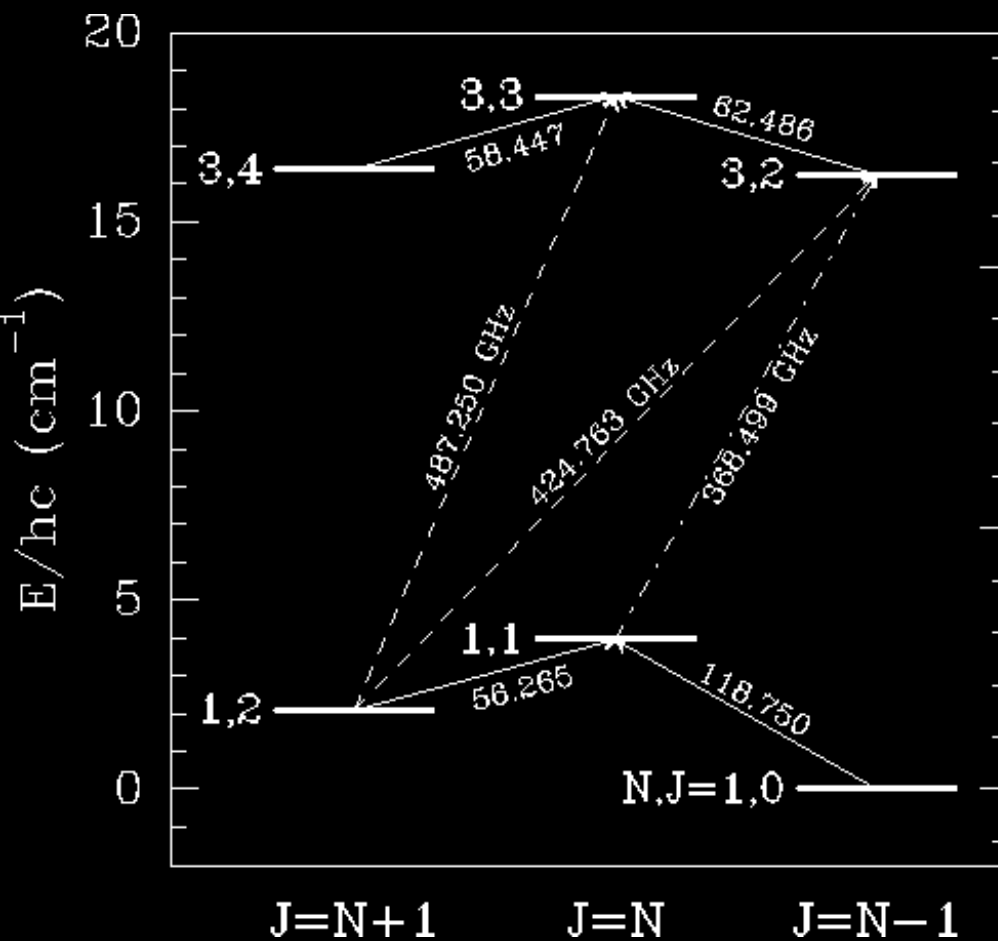
O_2

O_3

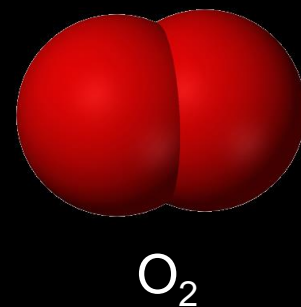
N_2O, CO, HCl ,+ Other (trace
gases)

Isotopologues – Vib. States



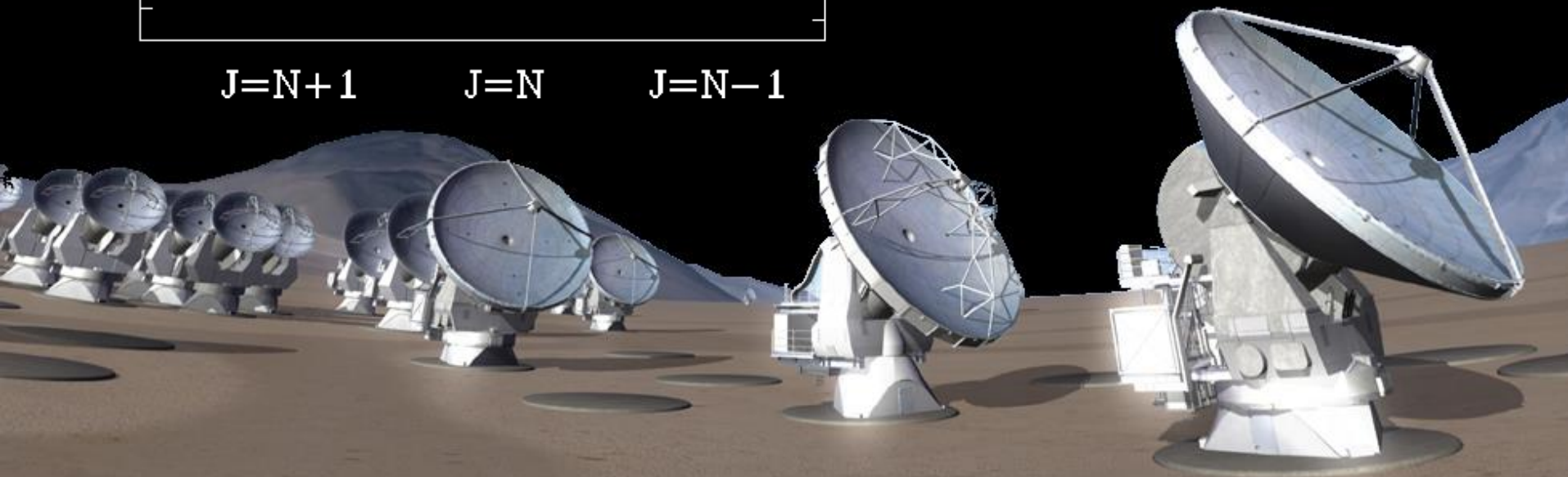


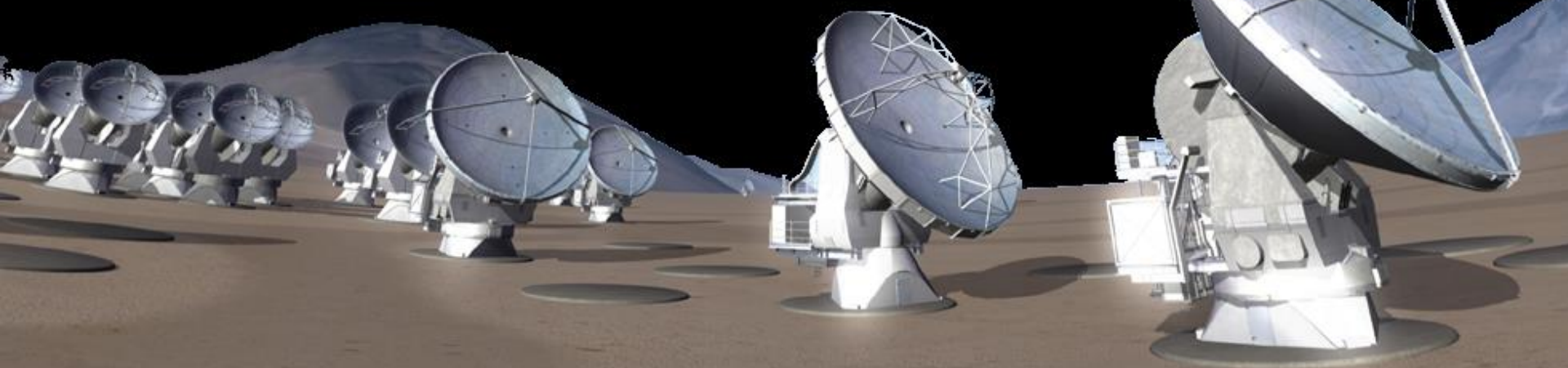
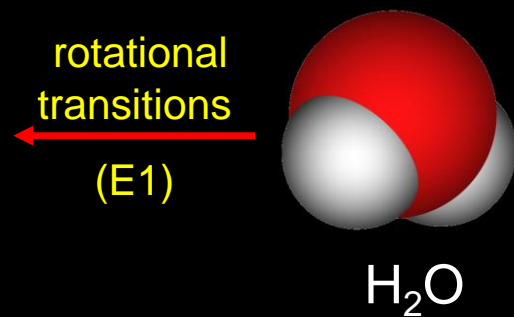
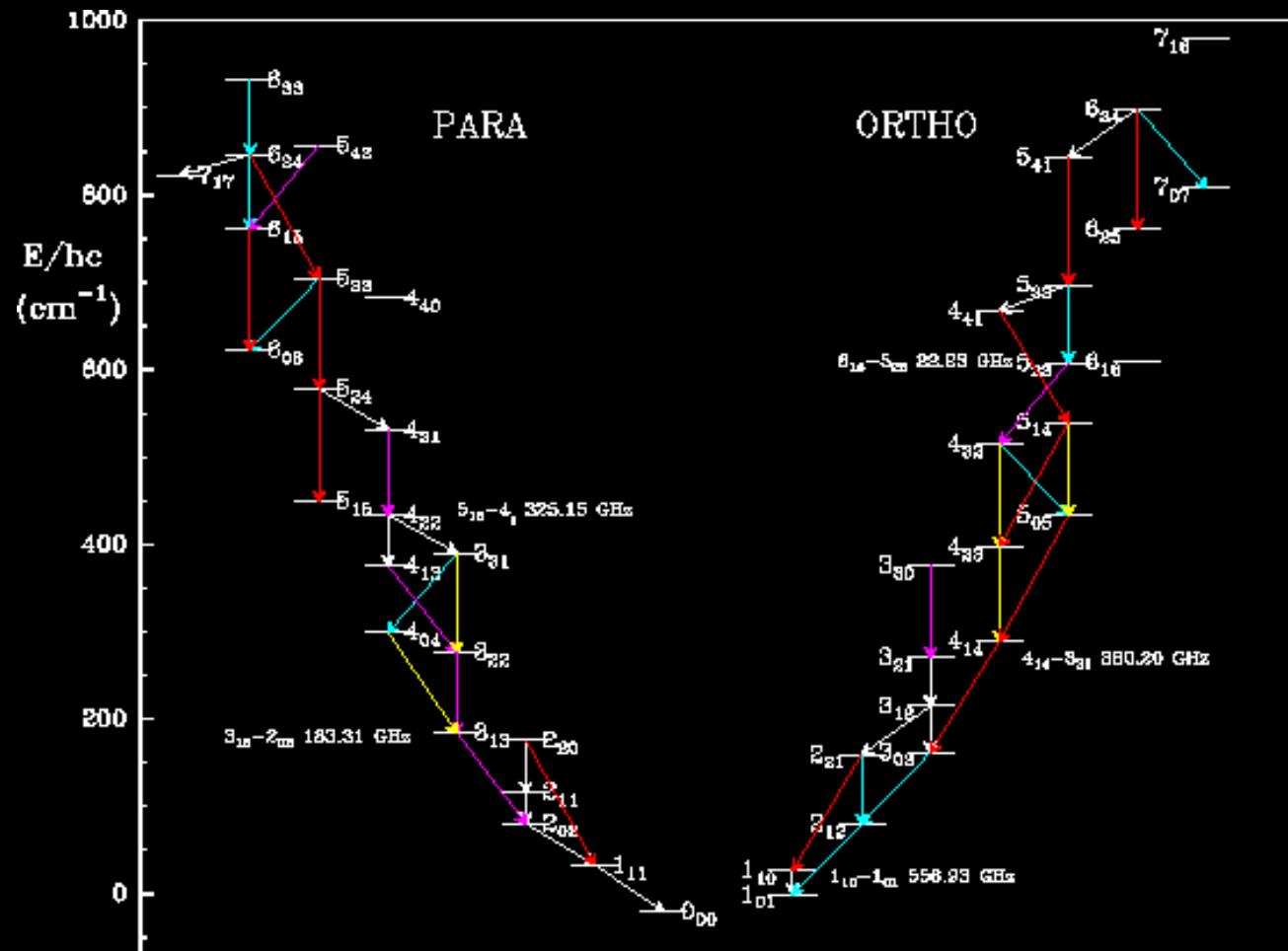
Lowest
rotational
transitions
(M1)



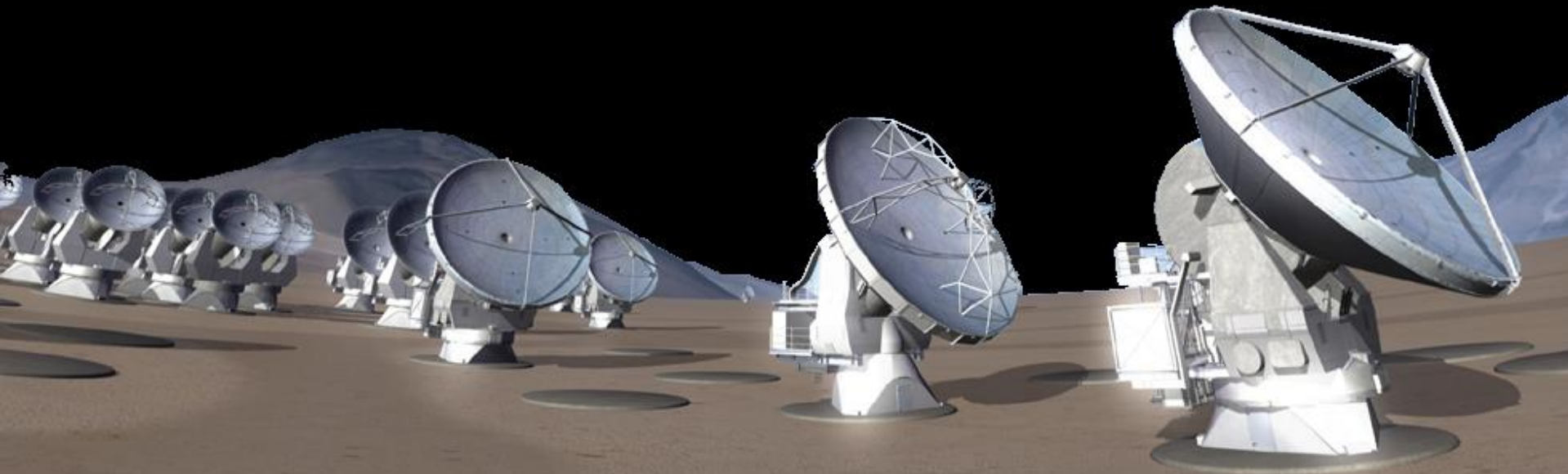
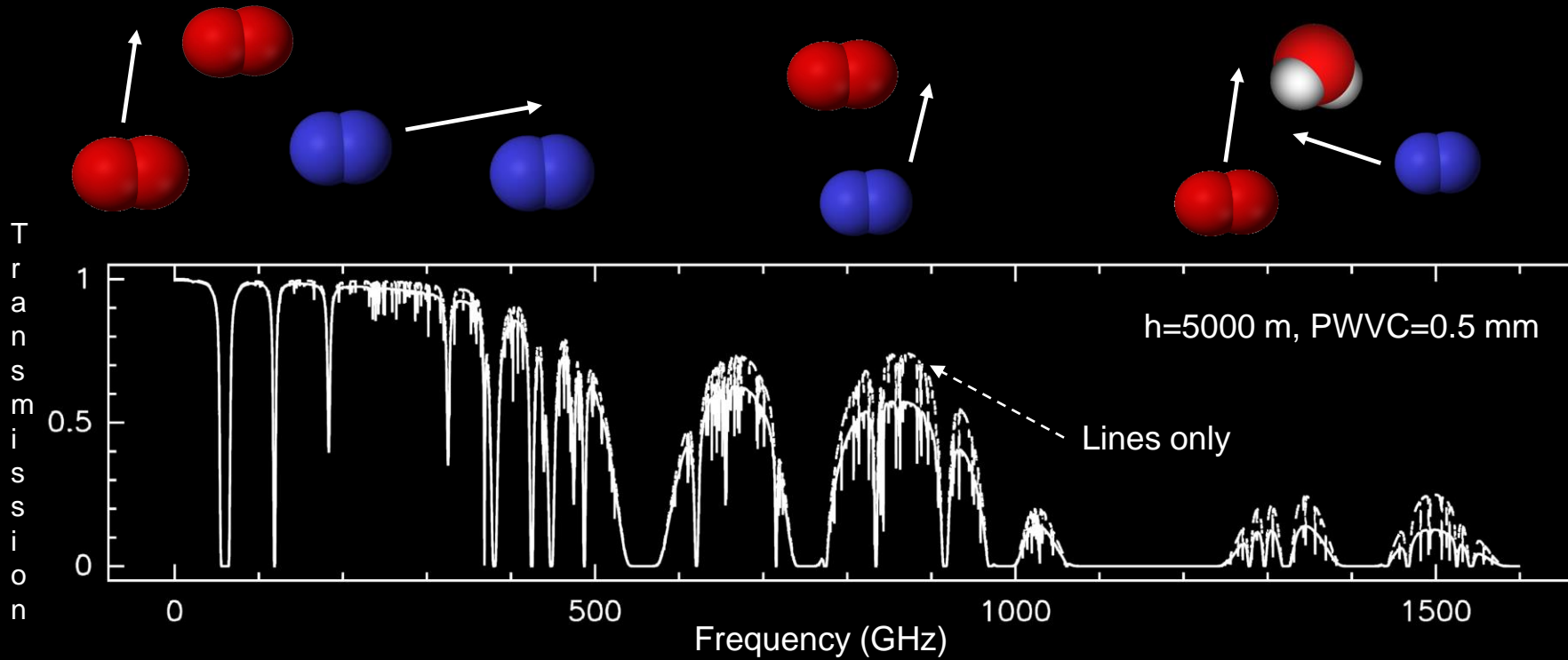
Paramagnetic molecule: Coupling of its permanent dipole moment with and external magnetic field causes ZEEMAN SPLITTING.

Modeling this effect is rather complex because of anisotropy, polarization, etc...





Collision-Induced absorption produces excess of sky opacity in the submm

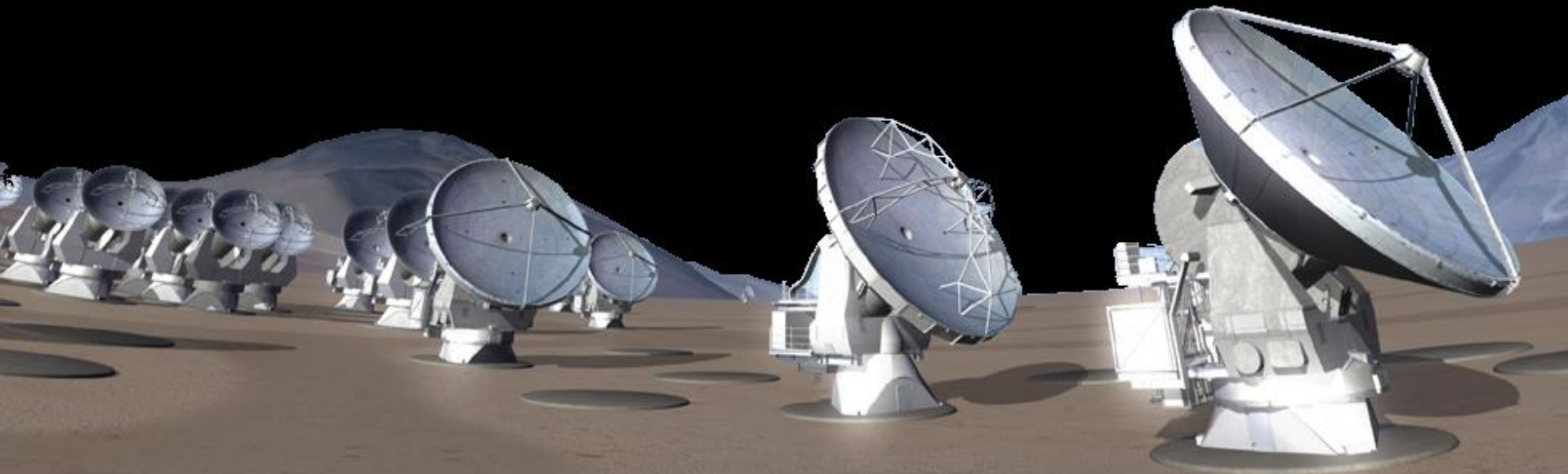


SINCE ATMOSPHERIC RT MODELS ARE DESIGNED FOR SPECIFIC APPLICATIONS, EACH ONE OVERLOOKS DIFFERENT ASPECTS

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GROUND-BASED OBSERVATORIES FOR ATMOSPHERE RT STUDIES:

- It is not their primary goal.
- However they have to deal with the atmosphere and need a good model.
- Up to date instrumentation is available.
- The instrumentation can be replaced.
- Weight and size is not a big problem
- Wide Frequency coverage.
- Extremely fine frequency resolution
- Good stability is now possible as well as clean spectra.
- Specific calibrations for atmospheric measurements now available.
- Interest in the phase (real part of refraction index).



Atmospheric Phase fluctuations



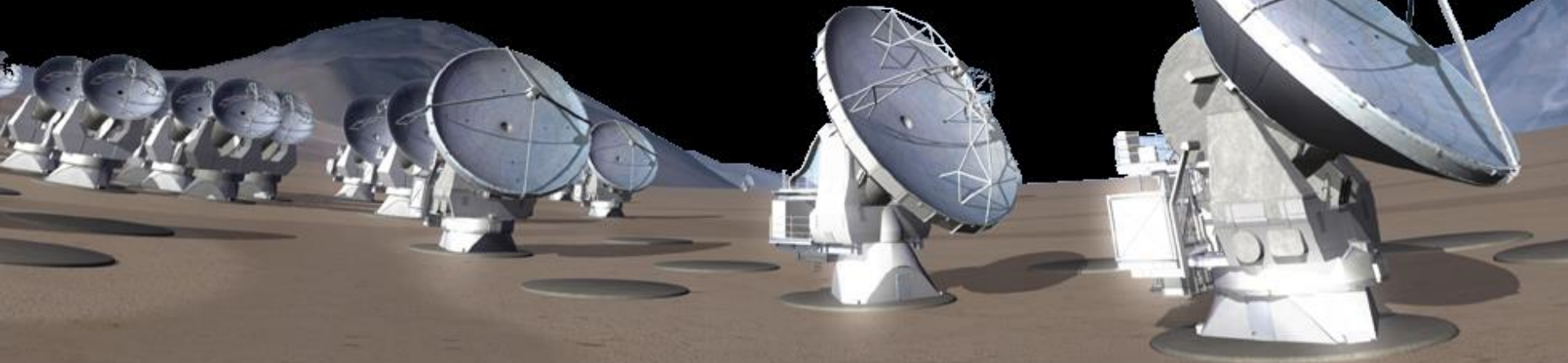
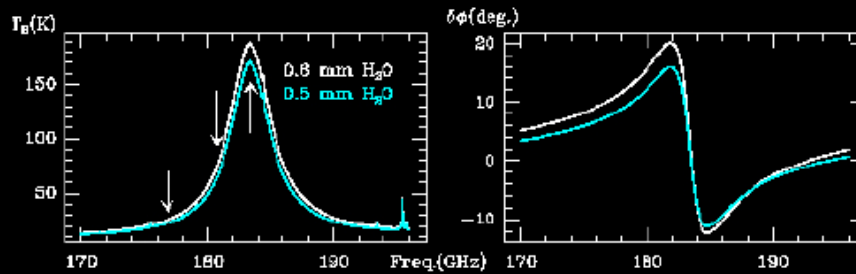
$$(\kappa_\nu)_{lu} = \frac{8\pi^3 N \nu}{3hcQ} \left(e^{-E_l/kT} - e^{-E_u/kT} \right) \cdot |\langle u | \mu | l \rangle|^2 f(\nu, \nu_{l \rightarrow u})$$

κ_ν Is a complex number

$$\mathcal{F}(\nu, \nu_{u \leftrightarrow l}) = \frac{\nu}{\pi \nu_{u \leftrightarrow l}} \left[\frac{1 - i\delta}{\nu_{u \leftrightarrow l} - \nu - i\Delta\nu} + \frac{1 + i\delta}{\nu_{u \leftrightarrow l} + \nu + \Delta\nu} \right] \quad (1)$$

Imaginary part (absorption)

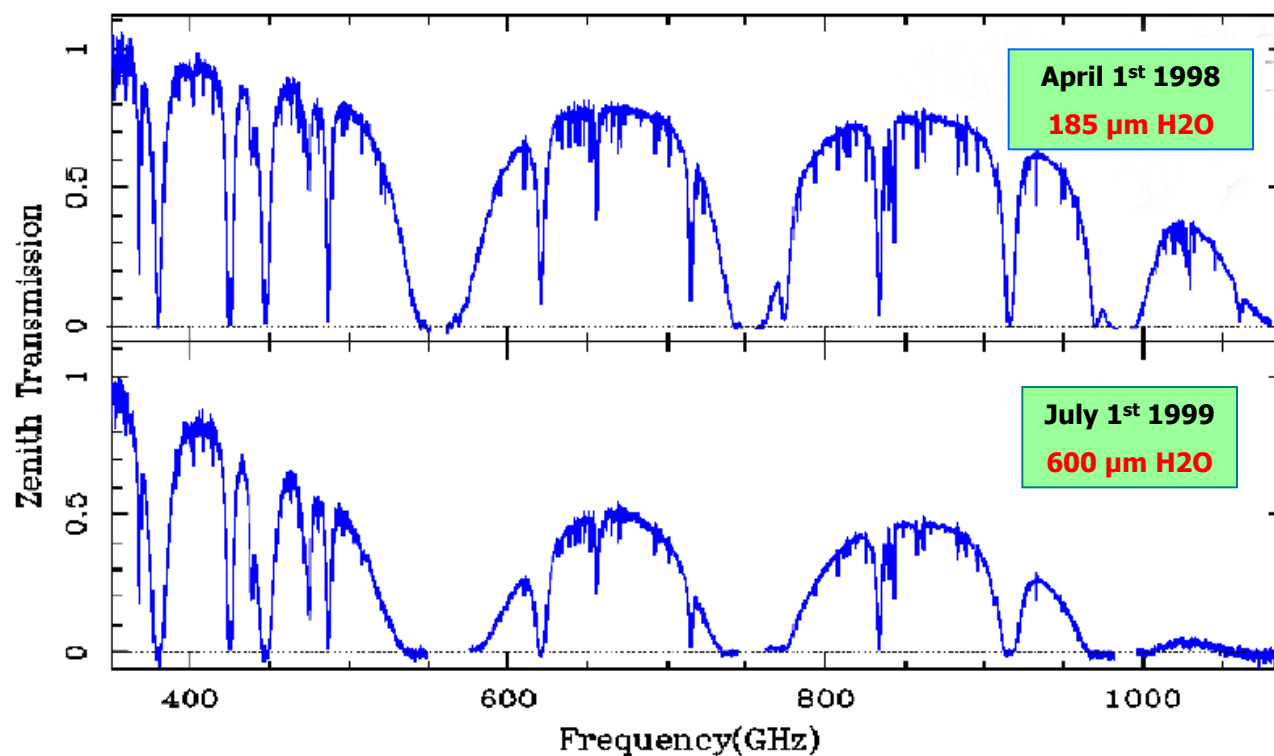
Real part (phase delay or pathlength variation)





Mauna Kea (4200 m, -5 °C), Hawai'i

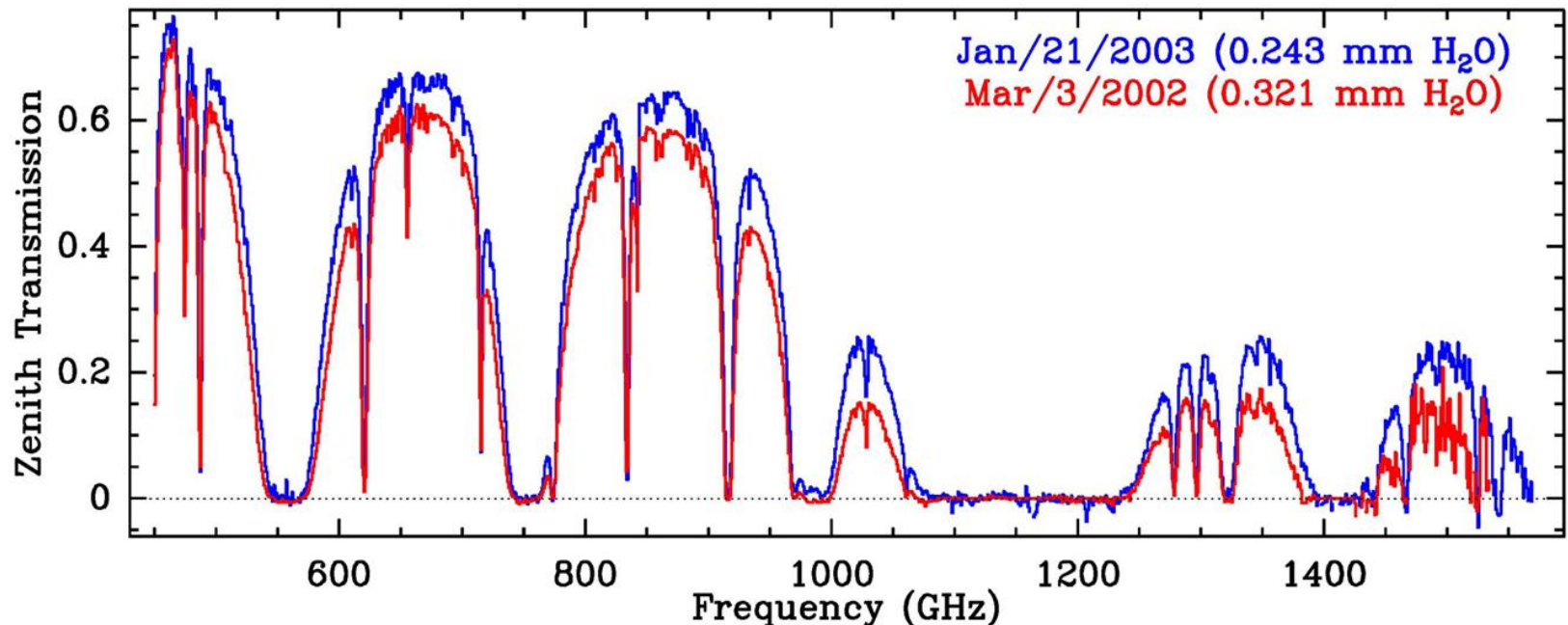
Hapuna Beach (0 m, 25 °C, Hawai'i)



Approach to study the Collision Induced Absorption

- Use well calibrated scans under dry and stable conditions.
- Ground temperature at CSO altitude $\sim 270 \pm 3$ K
- Ground pressure at CSO altitude $\sim 620 \pm 1.5$ hPa

The “dry” absorption is basically the same (within 1-3 %). The remaining opacity is proportional to the PWV. The PWV can be determined from strong water lines.





Since our ATM model is used in ALMA, APEX was the perfect choice for a study to validate and refine it.

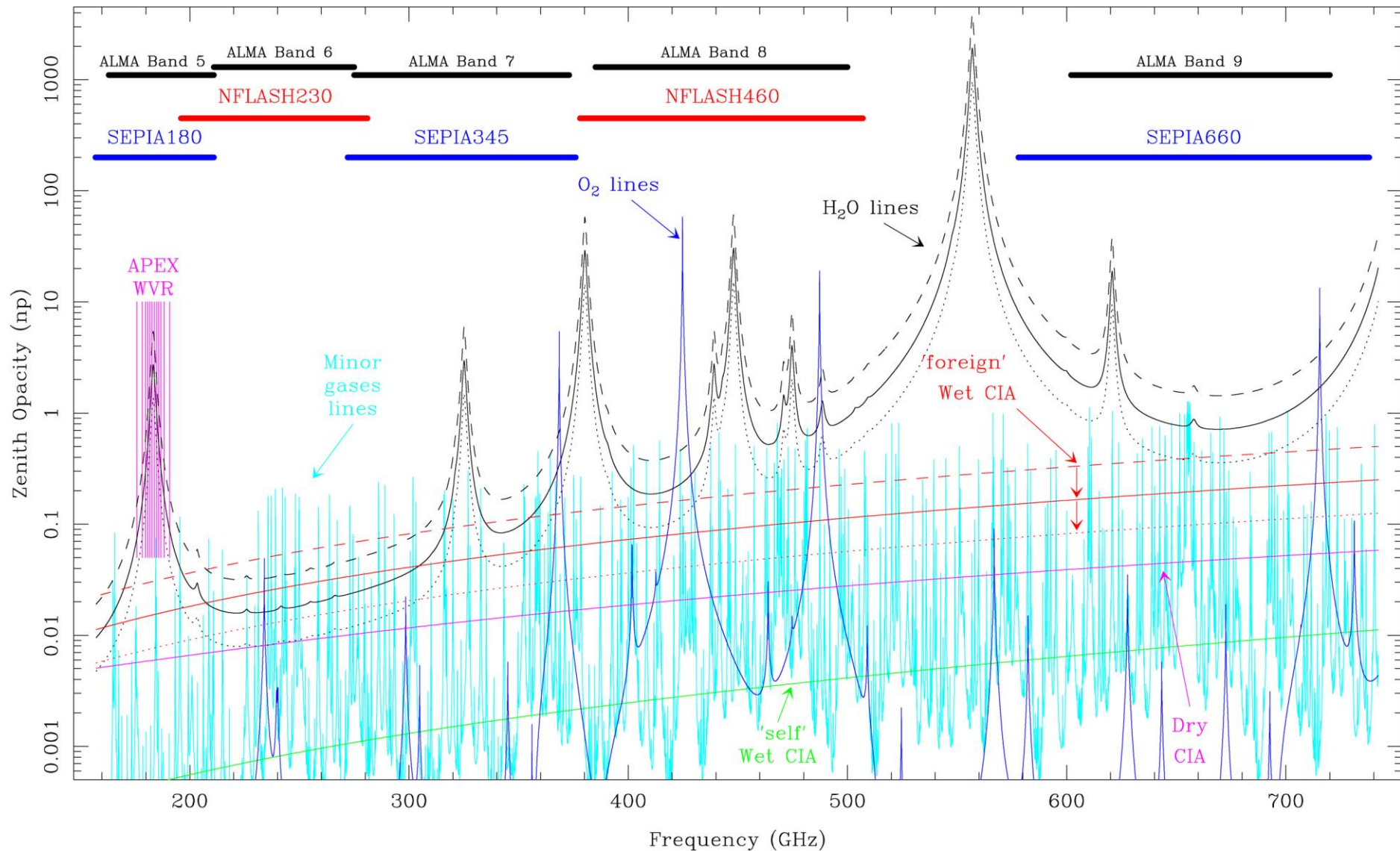
ALMA

APEX

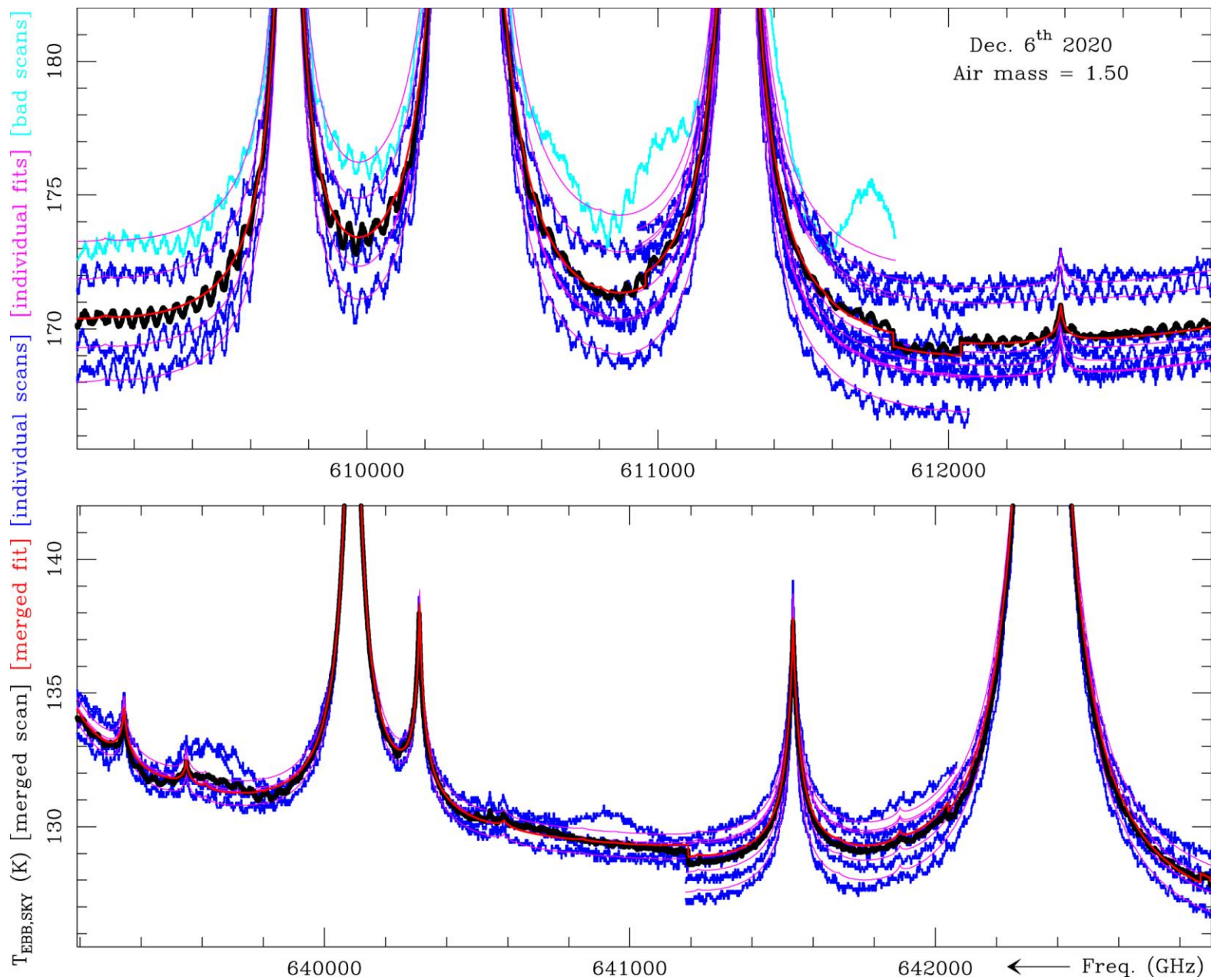
2.08 km

An aerial photograph of the ALMA observatory site in a high-altitude desert. Numerous white radio telescope dishes are arranged in a semi-circular pattern on the ground. In the background, there are rugged, snow-capped mountains under a clear blue sky. A semi-transparent blue rectangular box is overlaid on the image, tilted slightly, containing the text '2.08 km' in white, indicating the distance between the ALMA and APEX observatories.

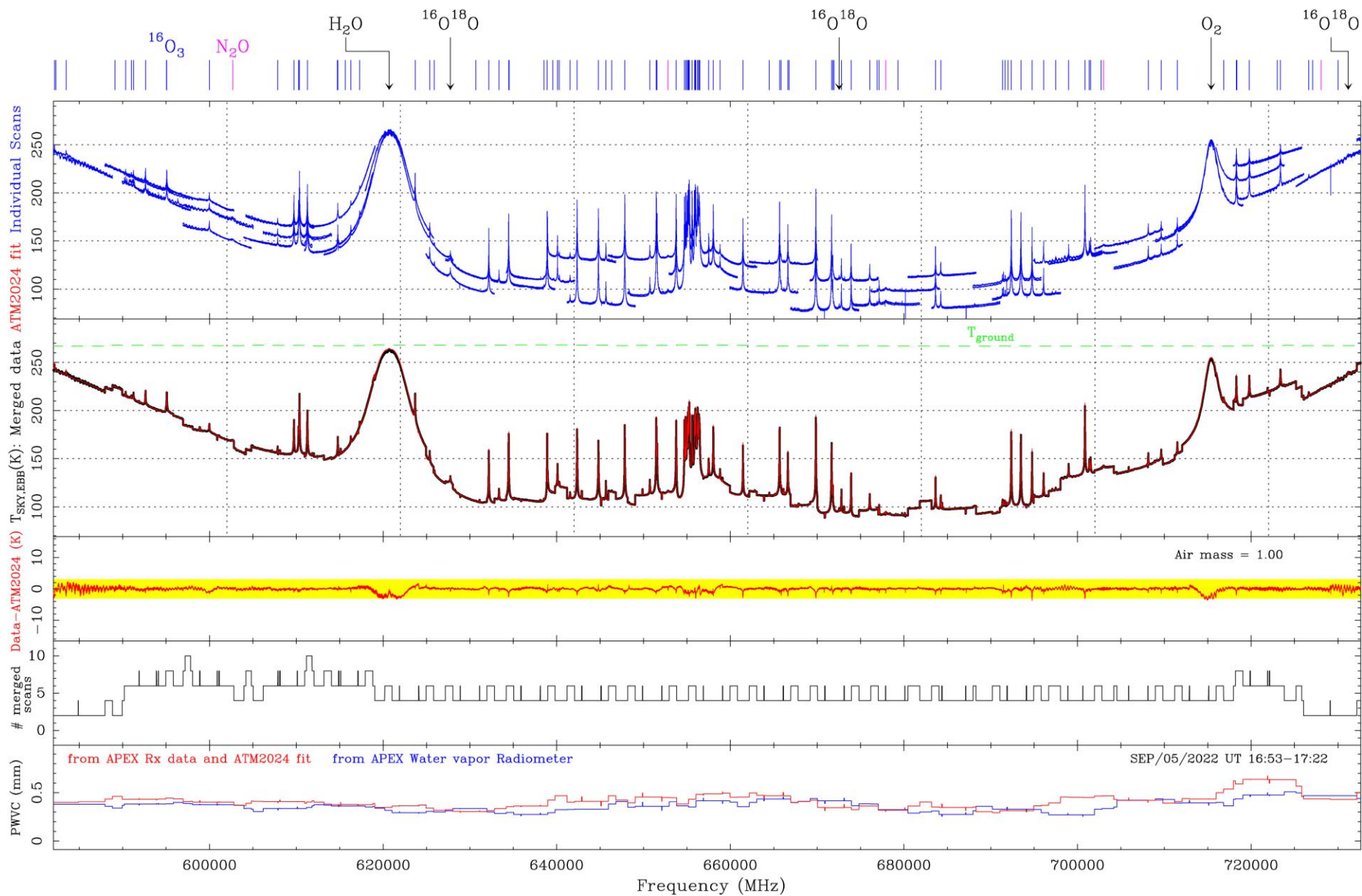
Atmospheric model (150-750 GHz) and available APEX instrumentation



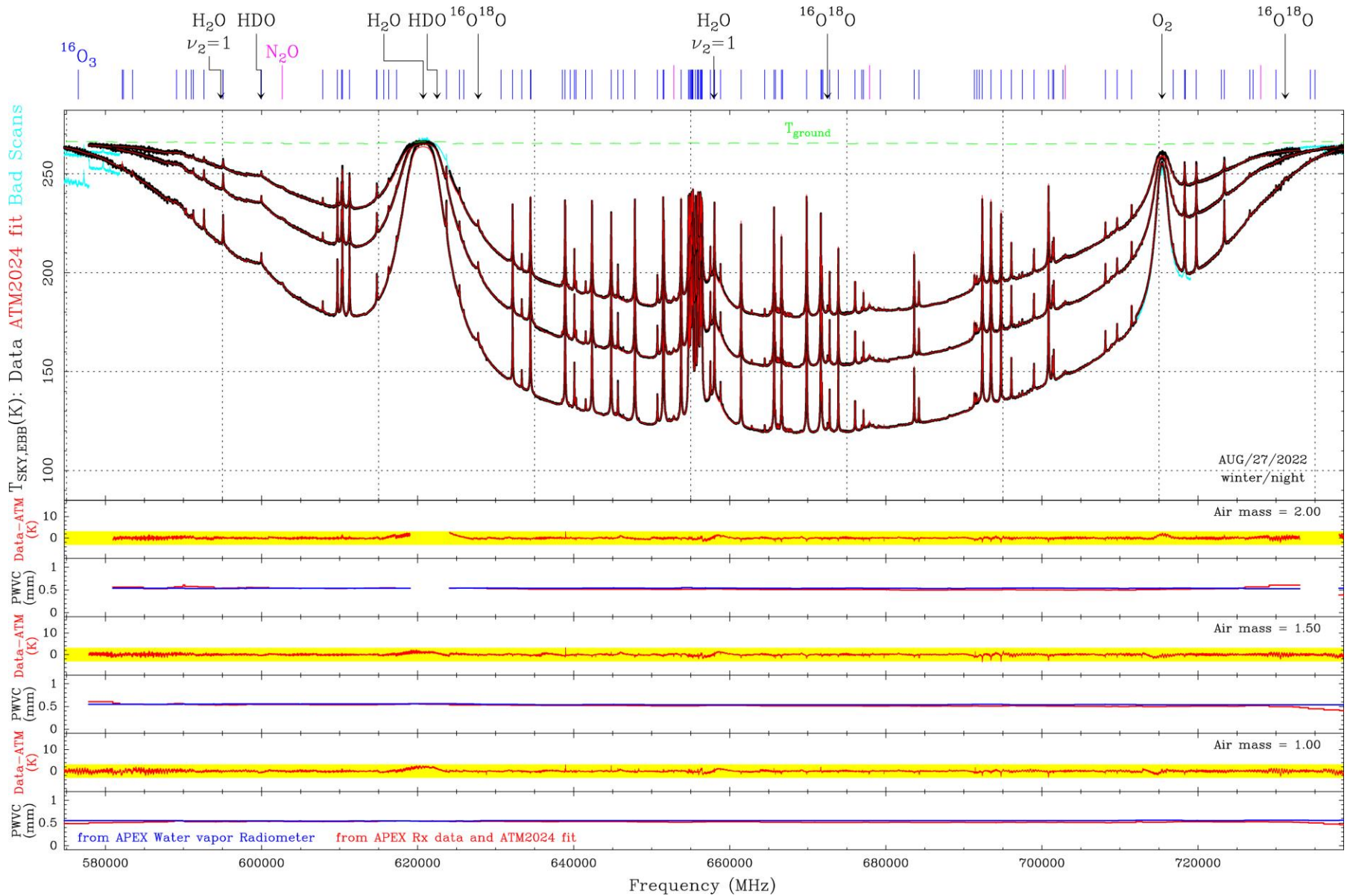
Good Scans are **fitted individually** and then **added**. **Bad scans** are **discarded**.



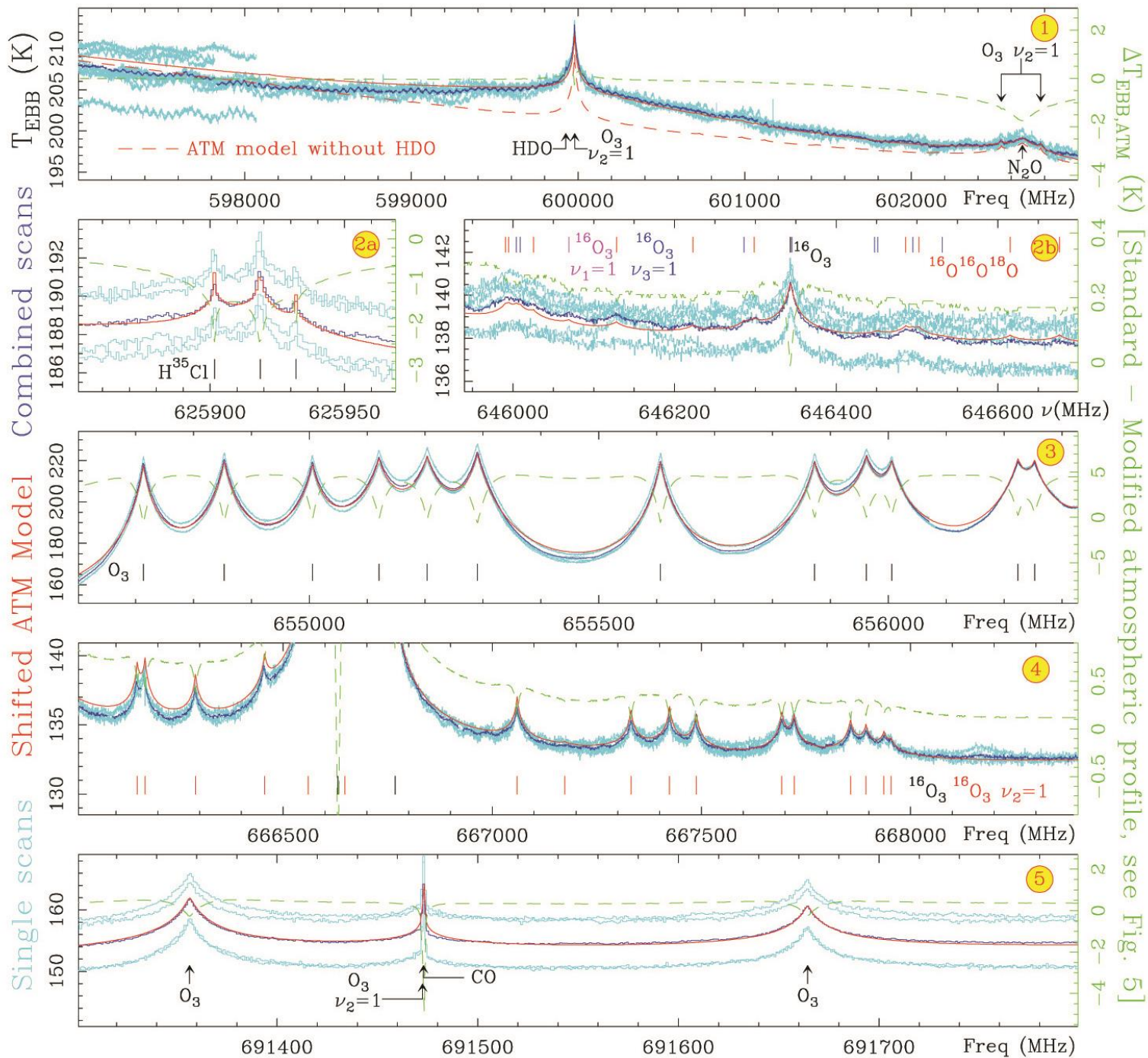
In some observing sessions the atmosphere was not very stable (here Sep. 5th 2022)



...but in other sessions the atmosphere was very stable



O_3
 O_3 isot.
 O_3 vib
 N_2O
 HCl
 CO



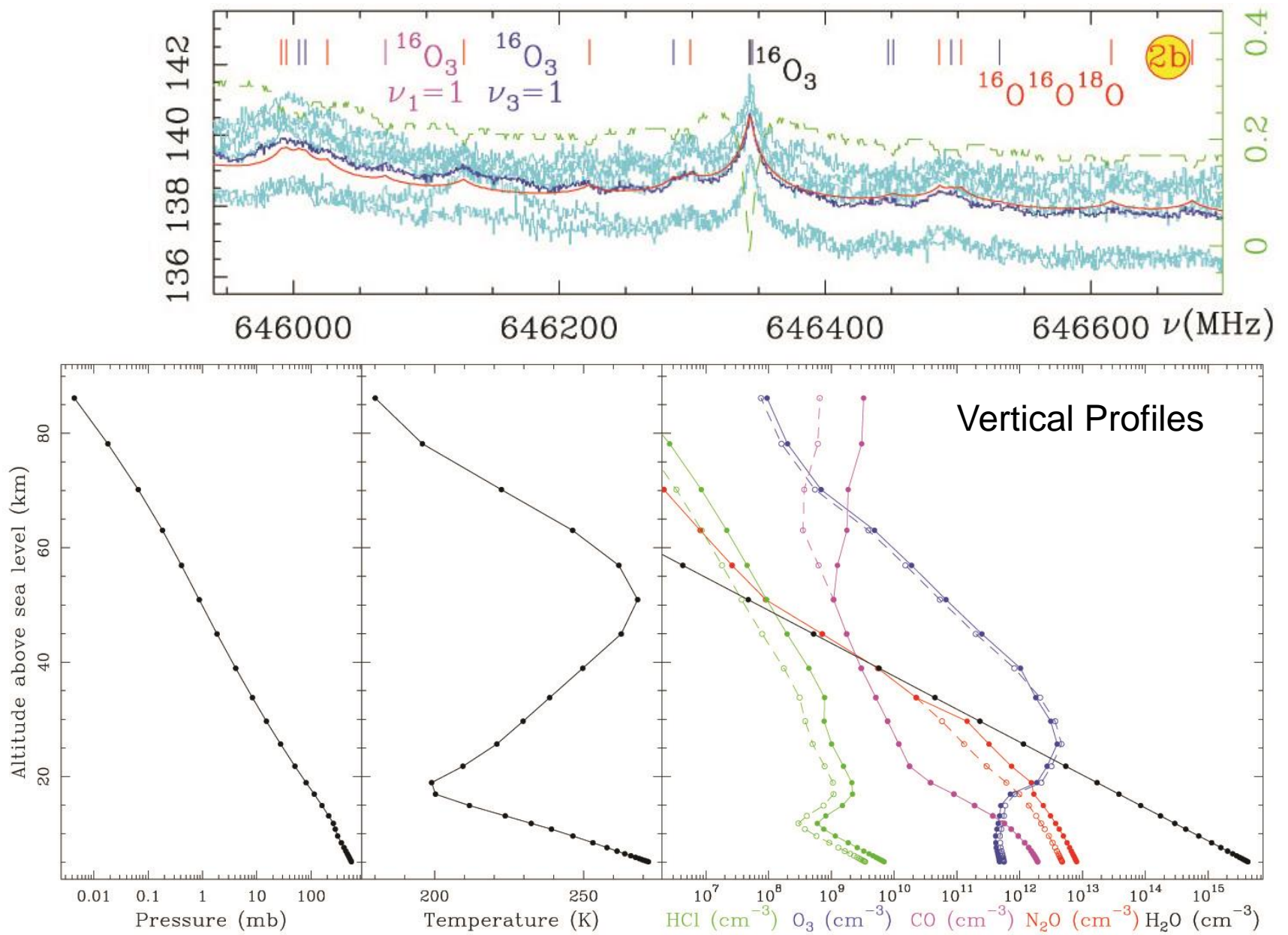
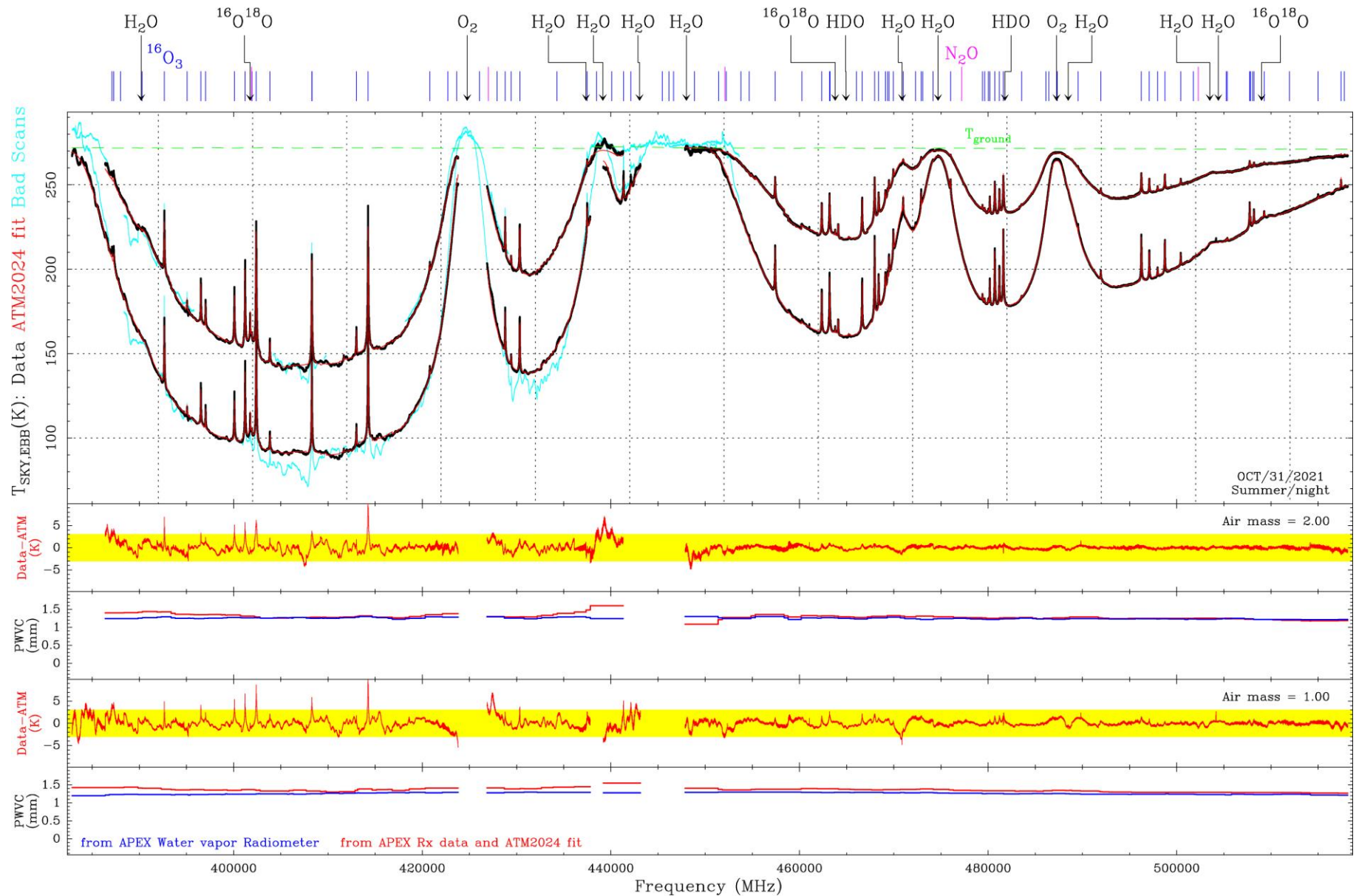
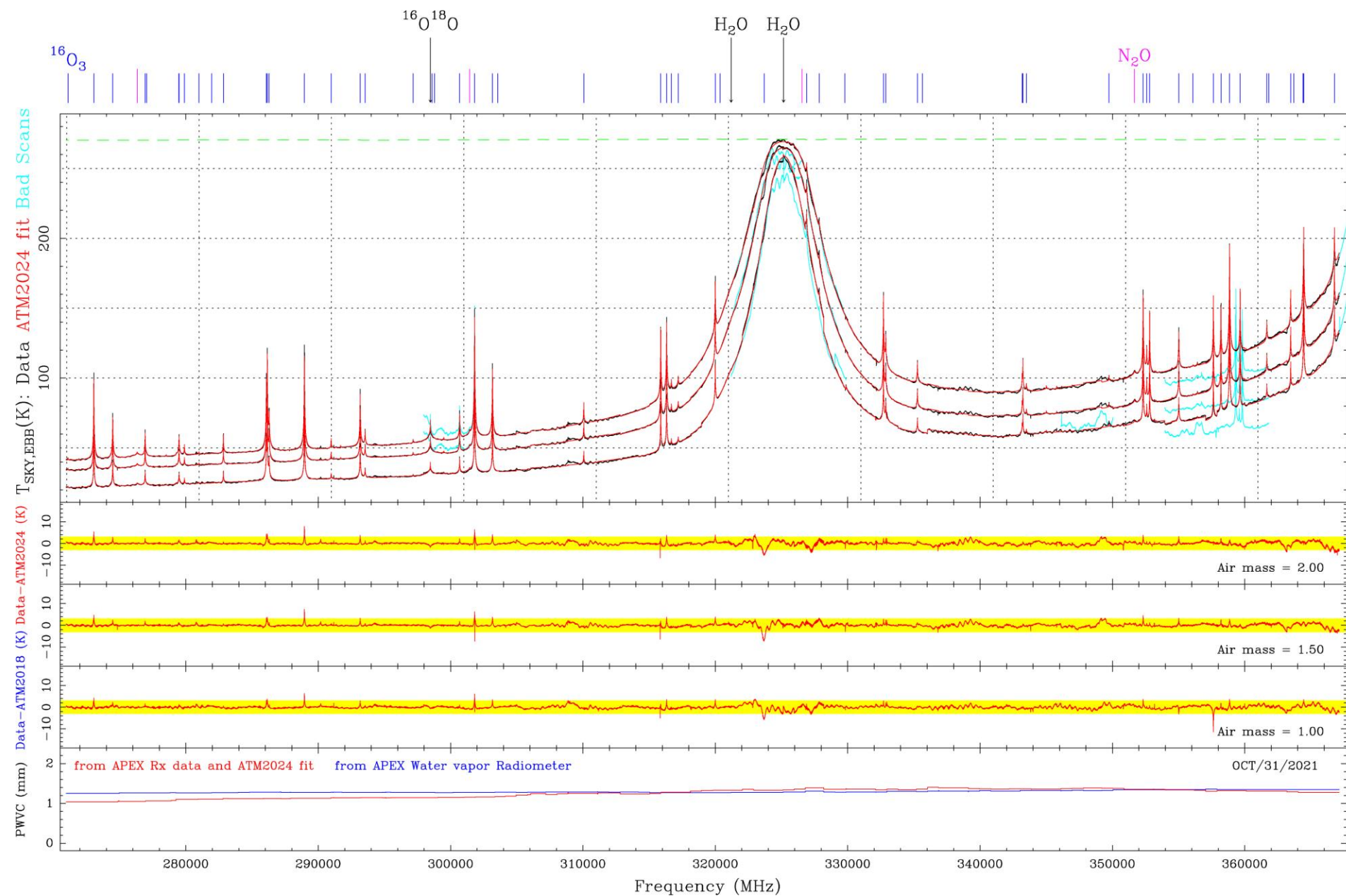


Fig. 5. Vertical profiles (solid lines) used as inputs to the ATM model for the model spectra shown in this work. The dots indicate the average values for the different layers (of increasing thickness) in which the atmosphere has been divided for the calculations. The dashed lines and open circles indicate profiles from U.S. Standard Atmosphere (1976) before being modified in order to better fit the observed lines of O_3 , N_2O and CO.

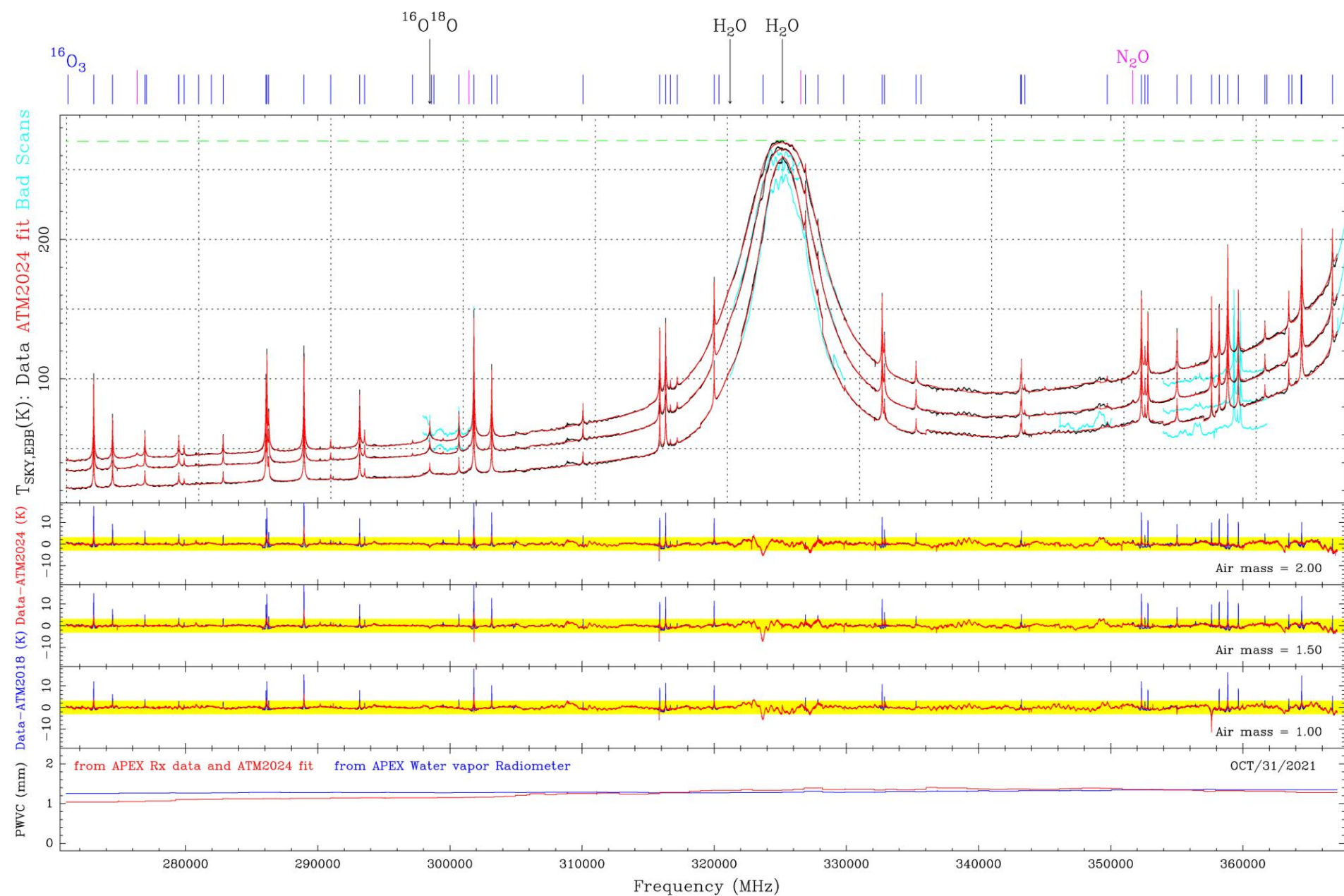
Other atmospheric “windows” (and receivers): 380 to 520 GHz, Oct 31st 2021

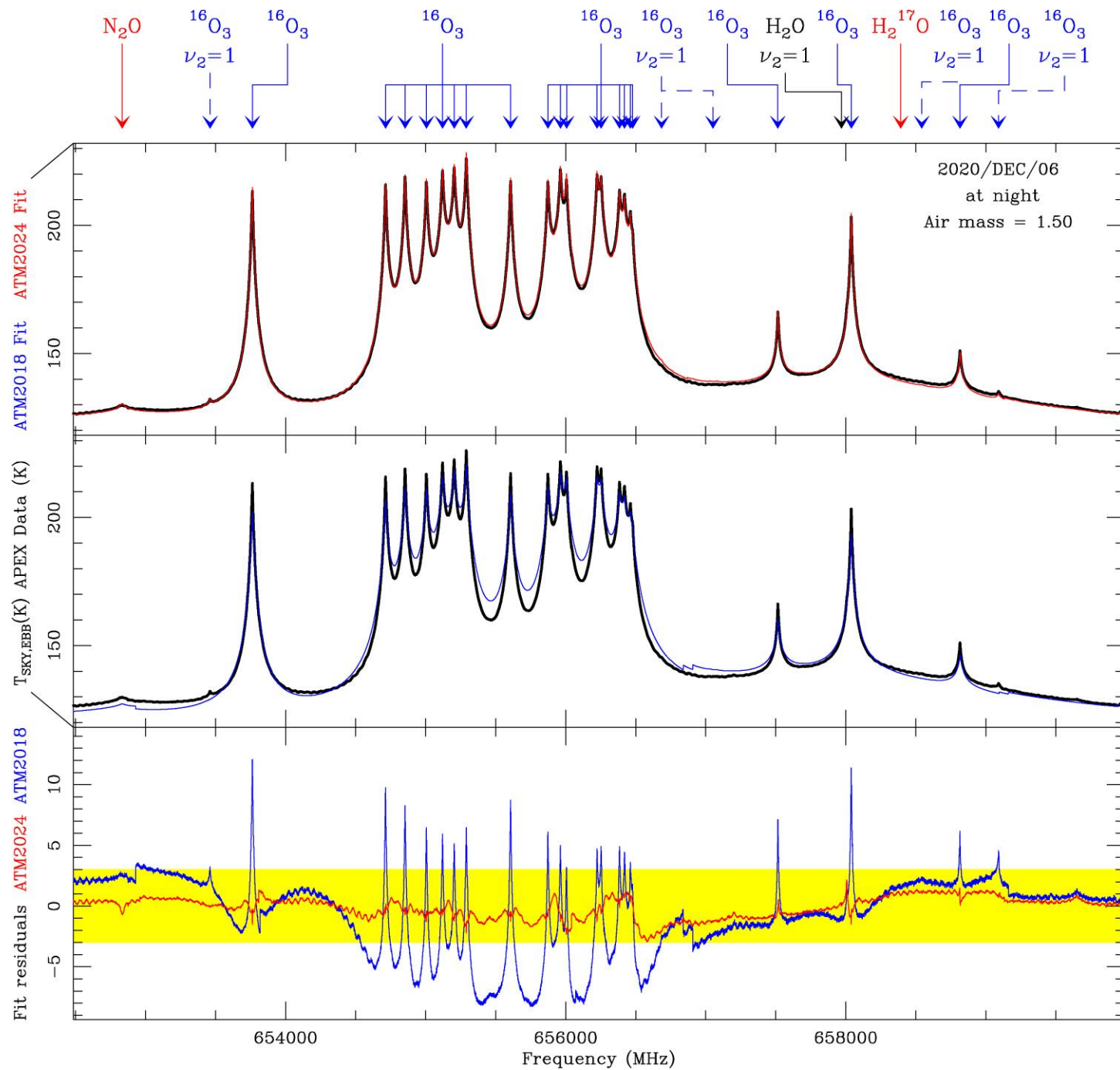


Around the 325 GHz water line, with best O3 profile



With standard (default) O₃ vertical profile

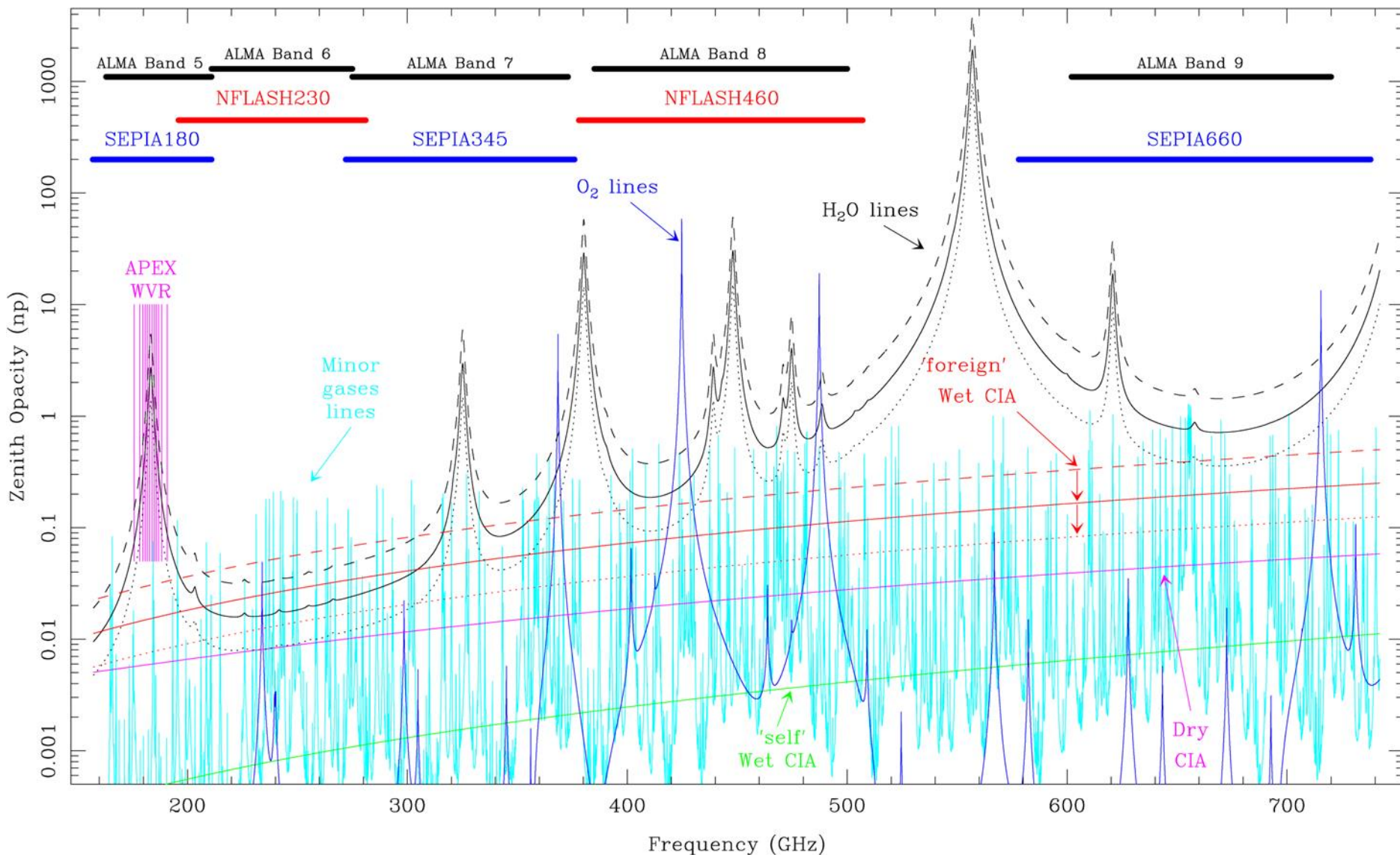




Fitting “minor”
gases vertical
profiles

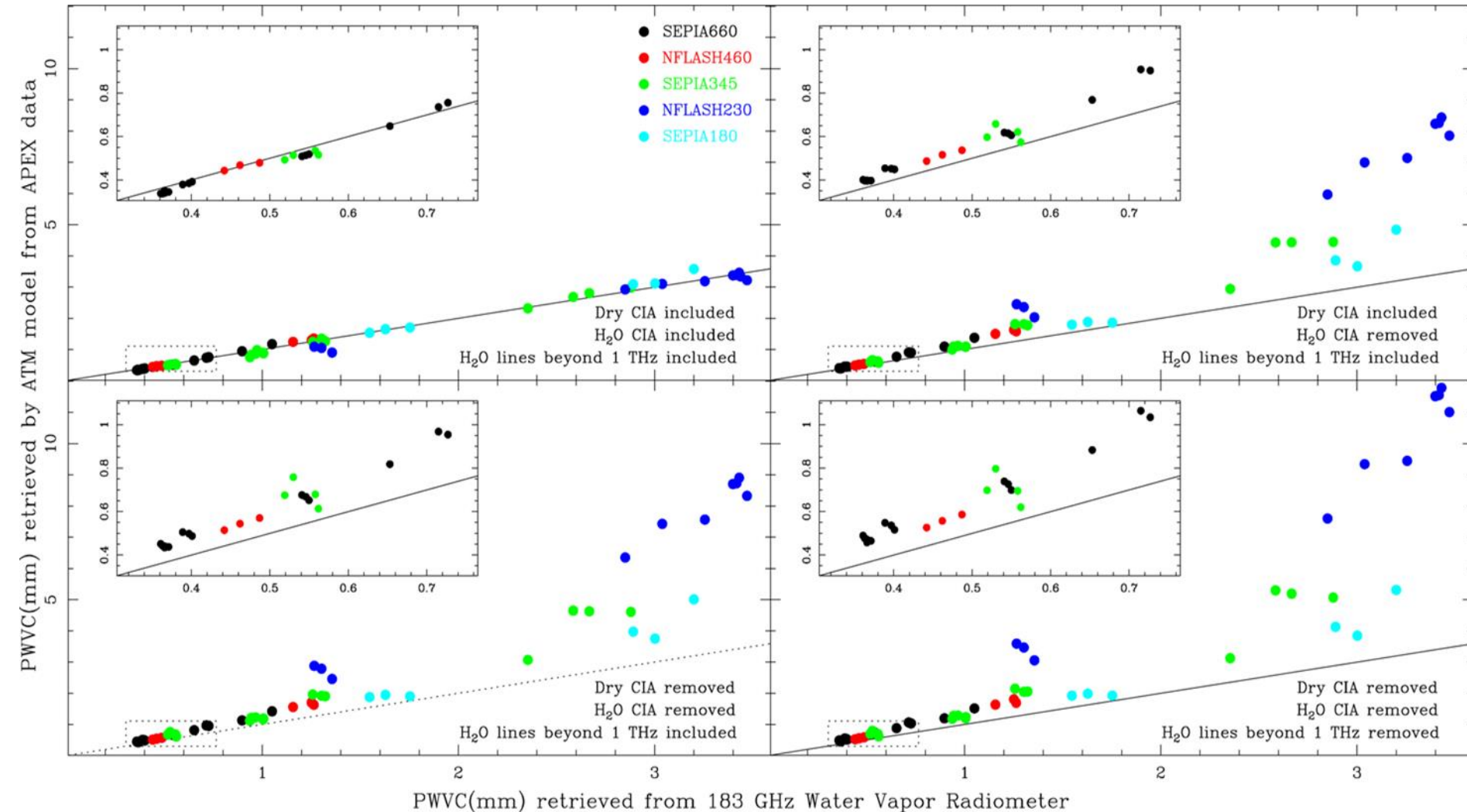
Validating “excess” of line-by-line absorption in the submillimeter

- Dry CIA ($\text{N}_2\text{-N}_2$, $\text{O}_2\text{-O}_2$, $\text{O}_2\text{-N}_2$ mechanisms).
- Foreign wet CIA ($\text{O}_2\text{-H}_2\text{O}$, $\text{N}_2\text{-H}_2\text{O}$).
- Far wings of H_2O lines centered beyond 1 THz.



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- Far wings of H_2O lines centered beyond 1 THz.



SUMMARY AND CONCLUSIONS

- Ground-based astronomical observatories have now very stable receivers + FFTS backends that allow to get absolutely calibrated atmospheric spectra covering hundreds of GHz at kHz resolution.
- Many fine aspects of the molecular spectroscopy parameters used for atmospheric models currently have been validated and/or improved.
- In particular the Dry and “foreign” wet CIA have been revisited
- Seasonal and day-night reference profiles can be updated.
- For satellite applications the ground-based observations from astronomical observatories provide very good validation databases.
- The effort will continue from other sites providing access to complementary geographical and altitude conditions.

