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# **Performance of Coherent Lidar Receivers Using Atmospheric Compensation Techniques**

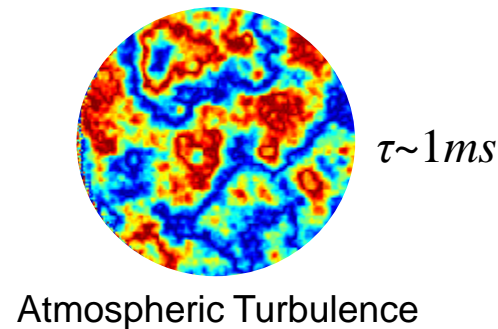
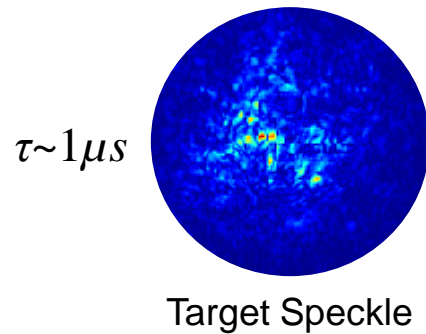
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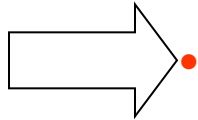
# INTRODUCTION

- Atmospheric turbulence coupled with target speckle can deteriorate coherent laser radar performance
- Speckle driven by turbulence reduces heterodyne mixing efficiency
- Spatial and temporal diversity methods, along with phase correction techniques, can be applied to mitigate signal deterioration
- Measures of performance are required to estimate the effectiveness of the compensation methods



# Outline

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- **Introduction**

Atmospheric Turbulence and Target Speckle  
Compensation Techniques

- **An Statistical Model for Coherent Lidar Signals**

Turbulence and Speckle Fading  
Compound Statistics

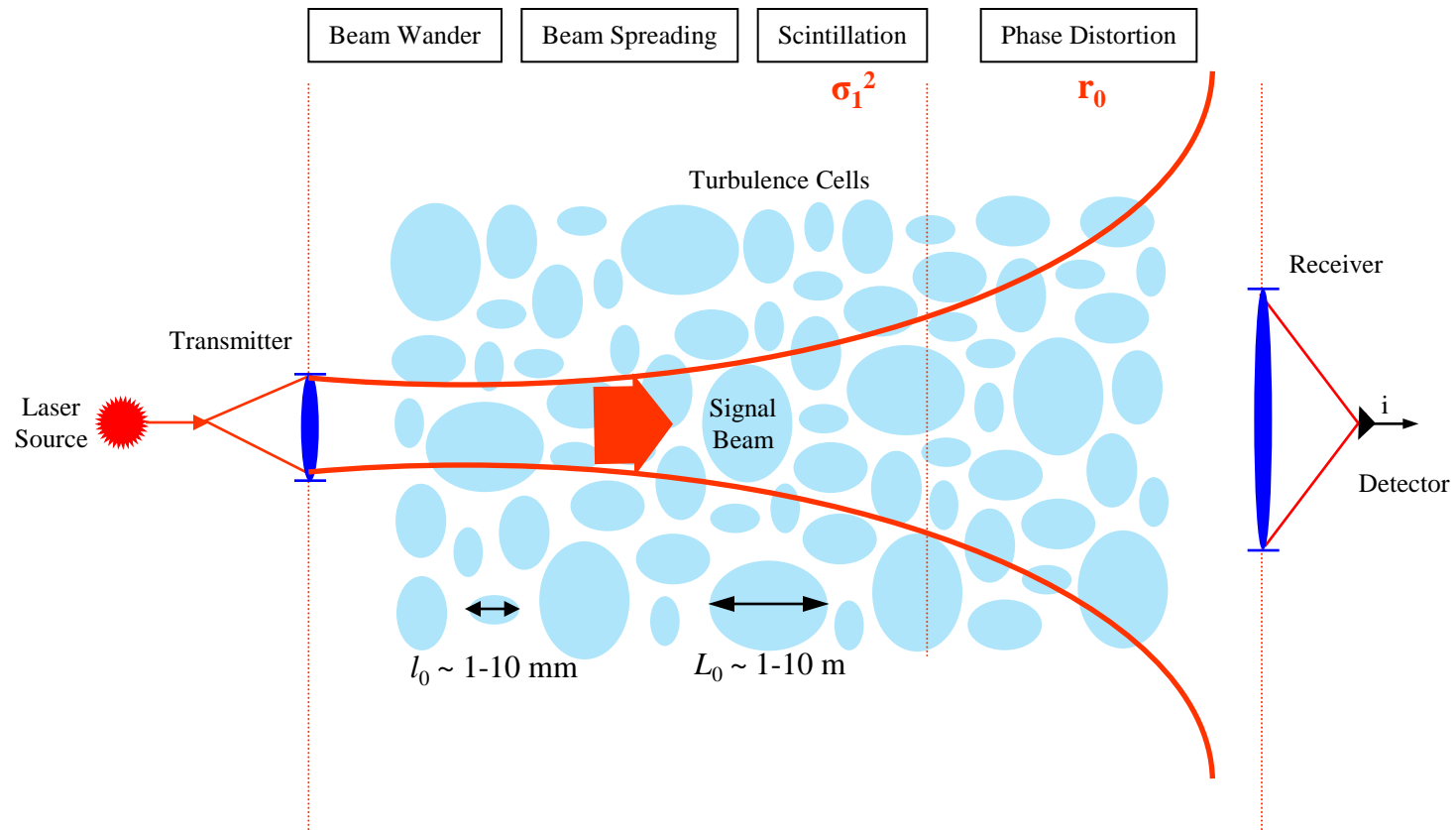
- **Measures of Performance**

Average SNR and Amount of Fading  
Outage probability and Mean Outage Rate

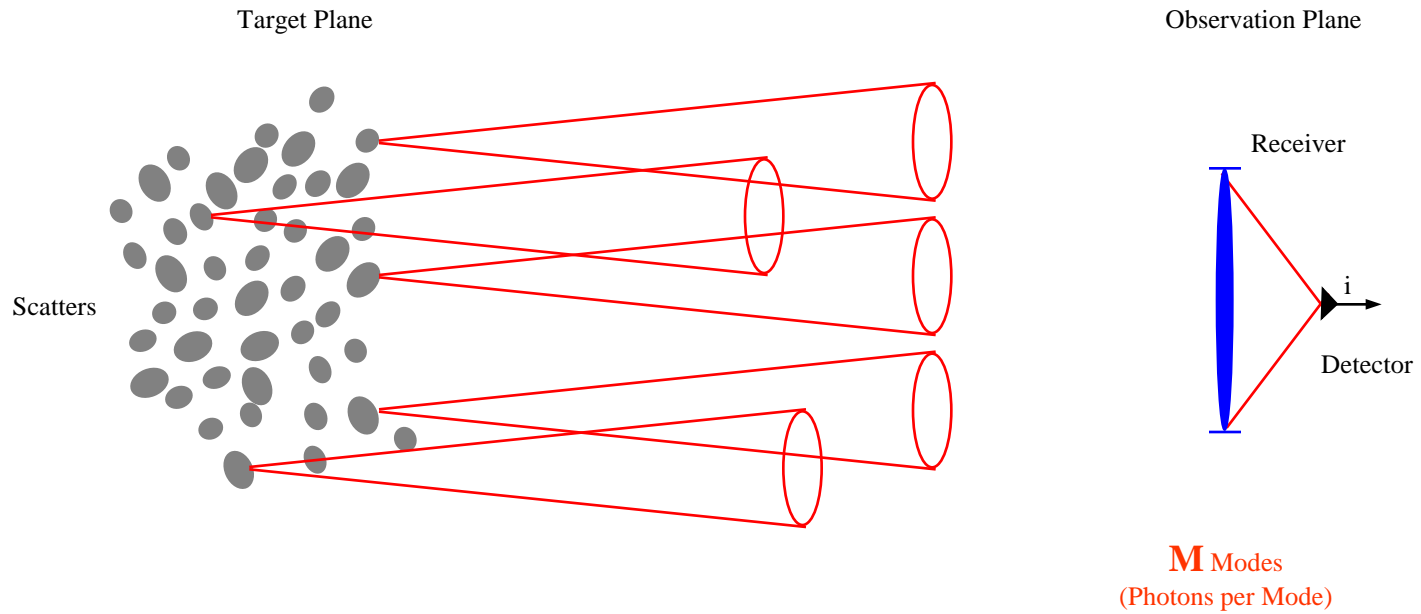
- **Conclusions**

Final Remarks and Research Opportunities

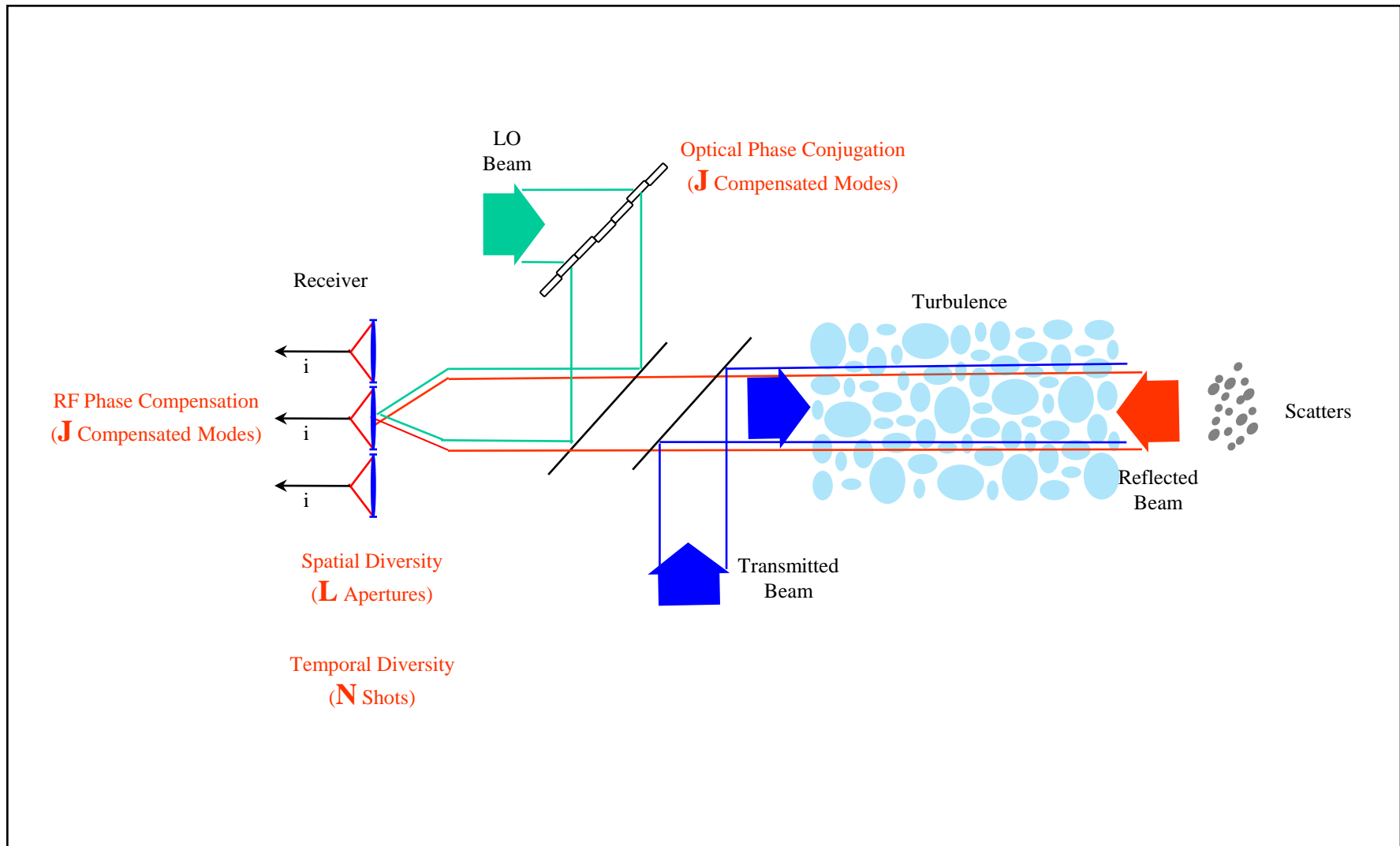
# Atmospheric Turbulence Effects



# Target Speckle Effects



# Compensation Techniques on Coherent Systems

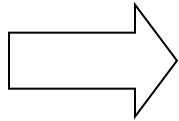


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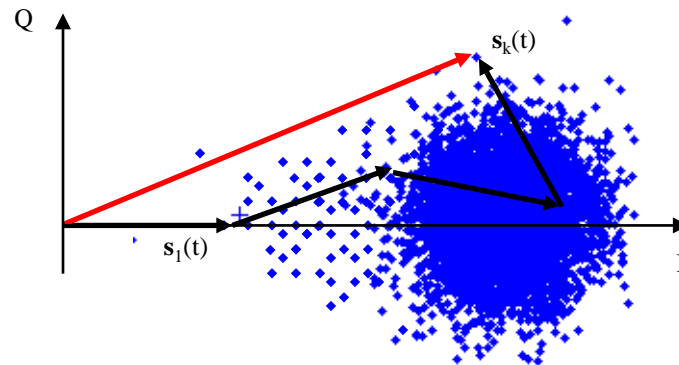
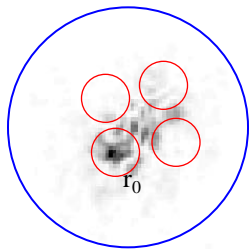
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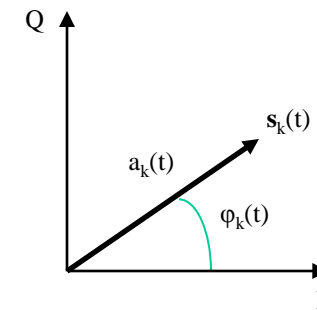
# Turbulence Fading

- Analyzing the receiver performance requires knowledge of the envelope statistics of the downconverted electrical signal. We find that the **SNR  $\gamma$  is described by a noncentral chi-square distribution** with two degrees of freedom

$$p_T(\gamma) = \frac{1+r}{\bar{\gamma}} \exp(-r) \exp\left[-\frac{(1+r)\gamma}{\bar{\gamma}}\right] I_0\left[2\sqrt{\frac{(1+r)r\gamma}{\bar{\gamma}}}\right]$$



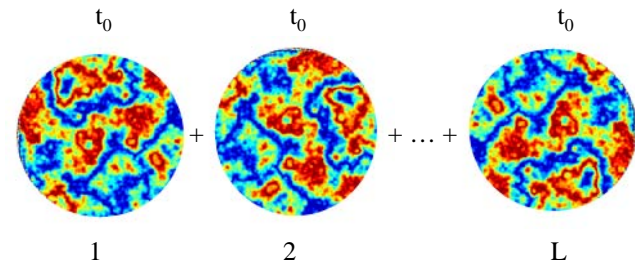
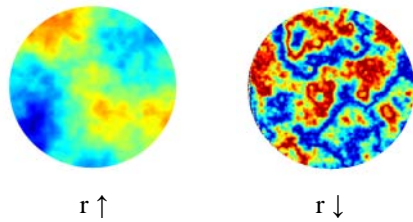
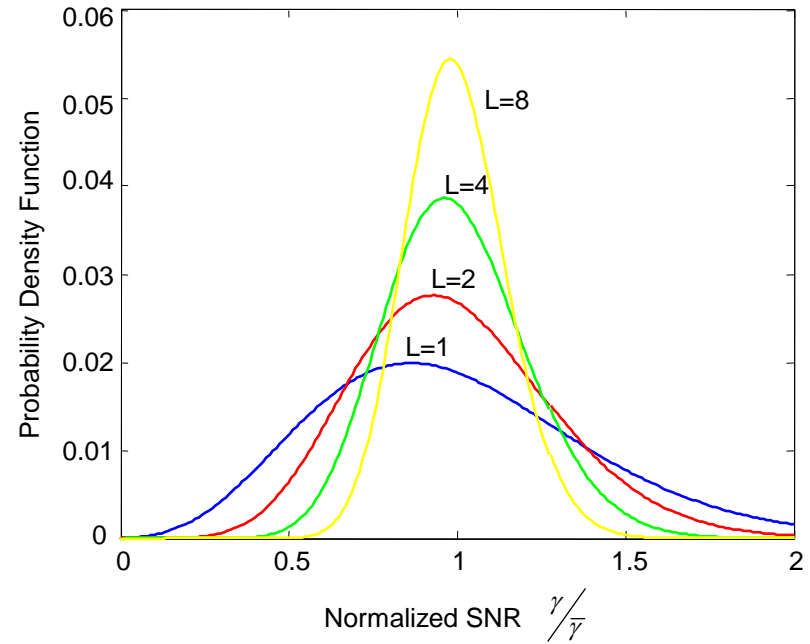
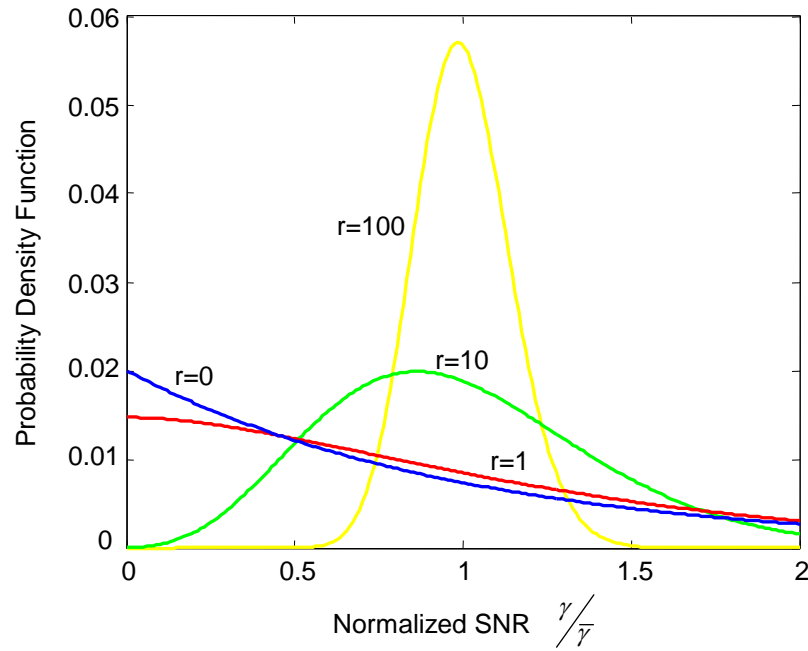
Multiplicative Turbulence Noise



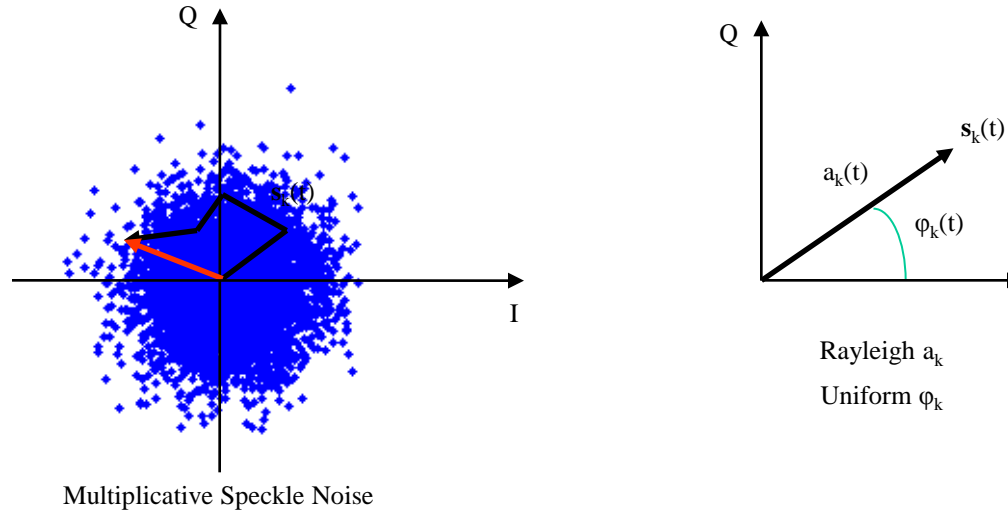
Log-normal  $a_k$

Normal  $\phi_k$

# Turbulence SNR Statistics



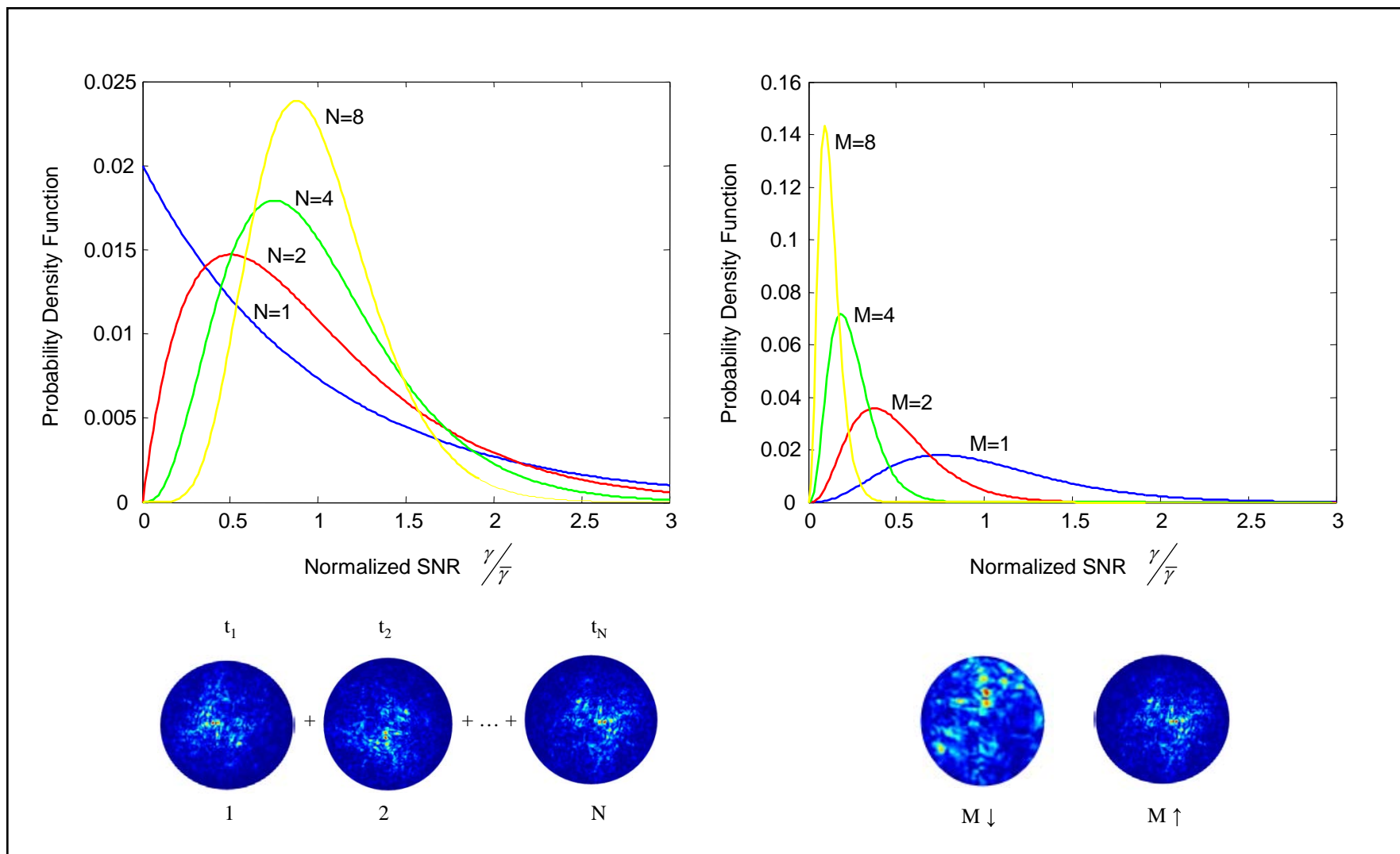
# Speckle Fading



- The SNR  $\gamma$  is described by a **Gamma distribution** with shape parameter  $N$  (accumulation shots) and scale parameter  $\bar{\gamma}/M$  (degeneracy parameter)

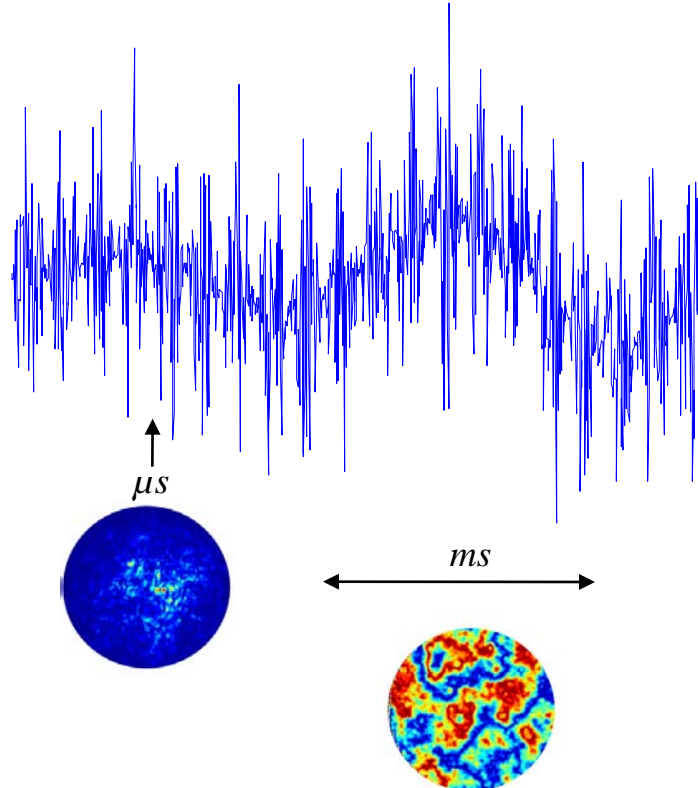
$$p_s(\gamma) = \left(\frac{NM}{\bar{\gamma}}\right)^N \frac{\gamma^{N-1}}{\Gamma(N)} \exp\left(-NM \frac{\gamma}{\bar{\gamma}}\right)$$

# Speckle SNR Statistics



# Speckle Driven By Turbulence

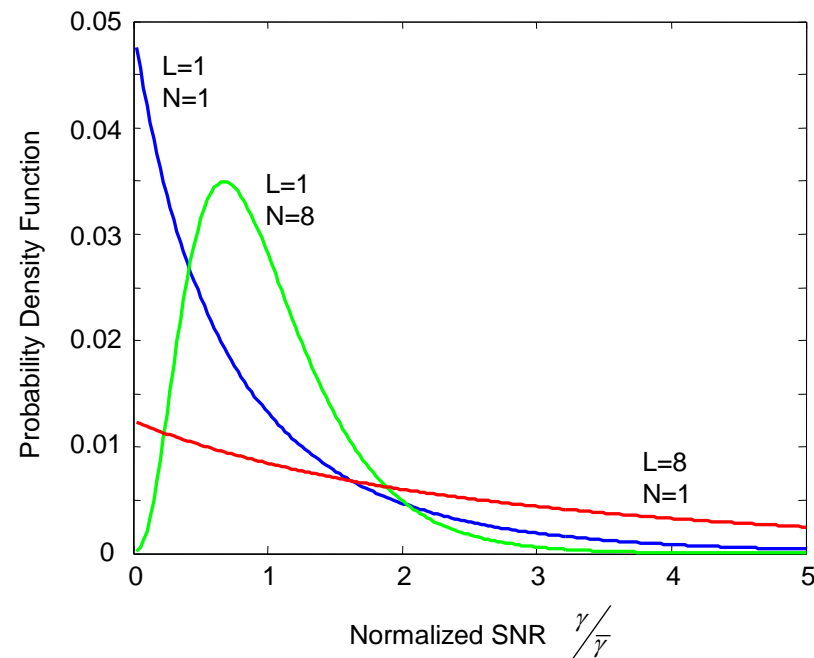
- The speckle process is driven by turbulence. The problem of compound speckle statistics can be analyzed by the application of conditional statistics.



$$p_{\gamma}(\gamma) = \int_0^{\infty} p_S(\gamma|v) p_T(v) d\gamma$$

# Coherent Lidar Signal Statistics

- We suggest a continuous PDF from the family of K distributions, the **gamma transform of a non-central chi-squared distribution**, to model the smearing due to speckle of the SNR in a heterodyne lidar receiver affected by atmospheric turbulence.



# Outline

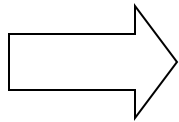
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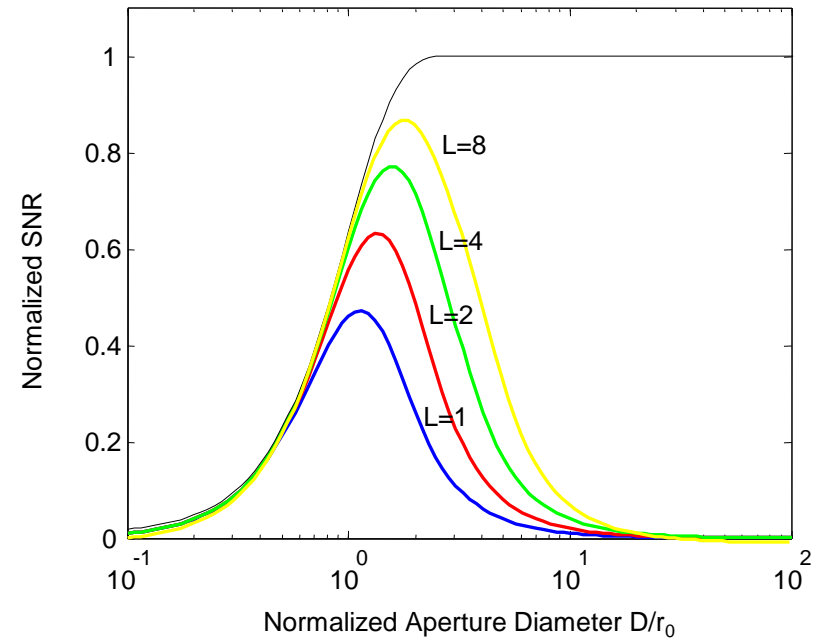
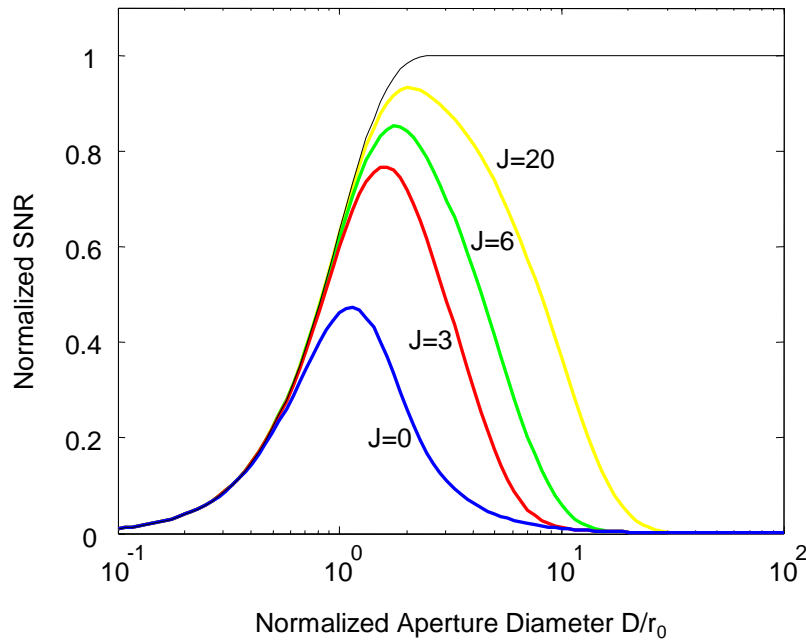
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Final Remarks and Research Opportunities

# Mean SNR (Photocounts)

- For a shot-noise limited signal is the detected number of photons

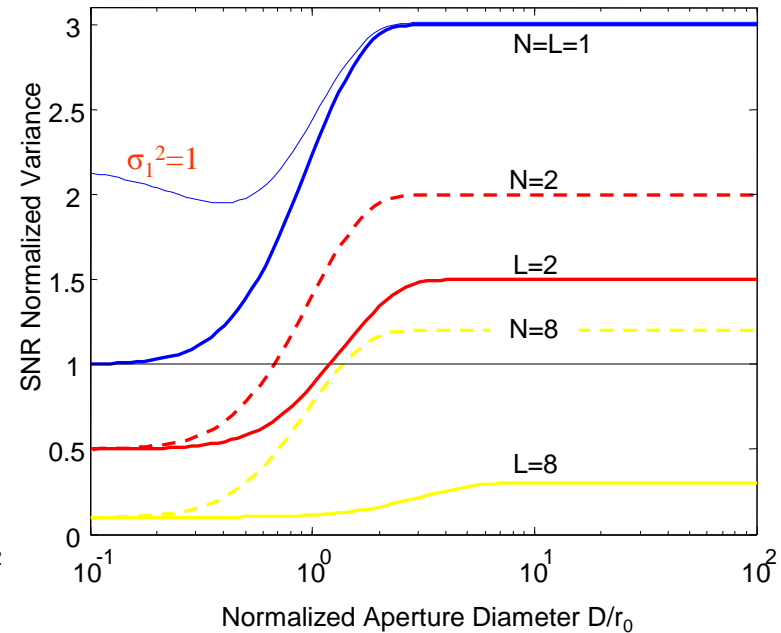
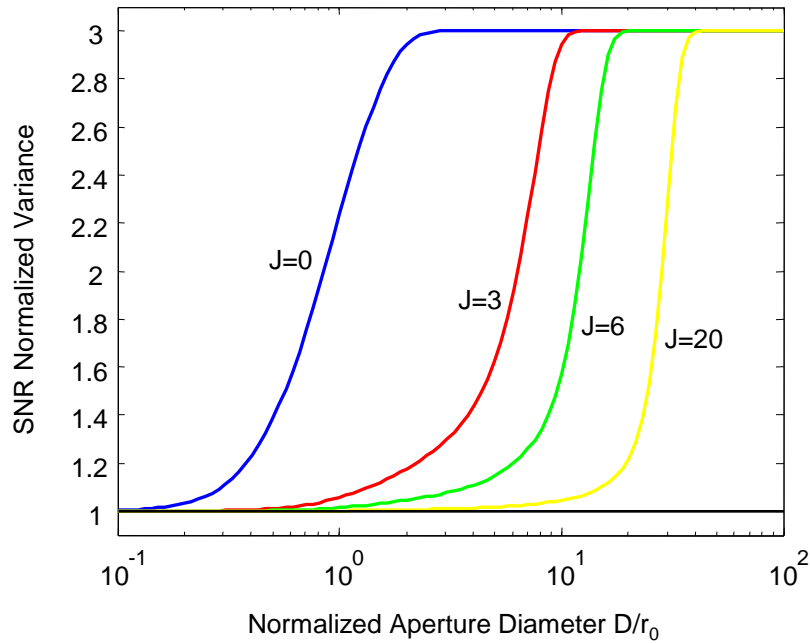
$$\langle \gamma \rangle = \int_0^{\infty} \gamma p_{\gamma}(\gamma) d\gamma$$



# Amount of Fading

- In the context of diversity combining, the mean  $\gamma$  does not capture all diversity. **Diversity also reduces fading-induced fluctuations**

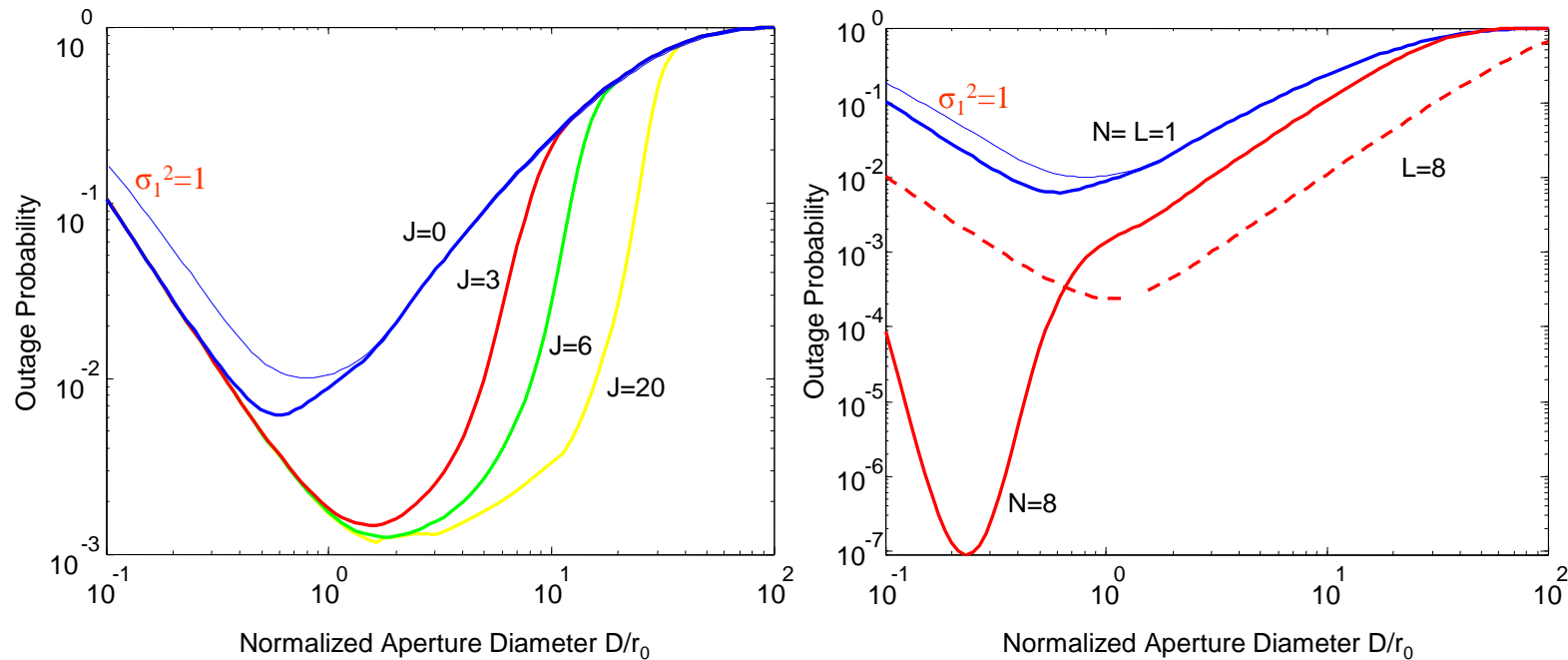
$$\langle \gamma^2 \rangle = \int_0^{\infty} \gamma^2 p_{\gamma}(\gamma) d\gamma$$



# Outage (Fade) Probability

- Another standard performance criterion of diversity systems is the probability that the output SNR (Photons)  $\gamma$  falls below a certain specified threshold

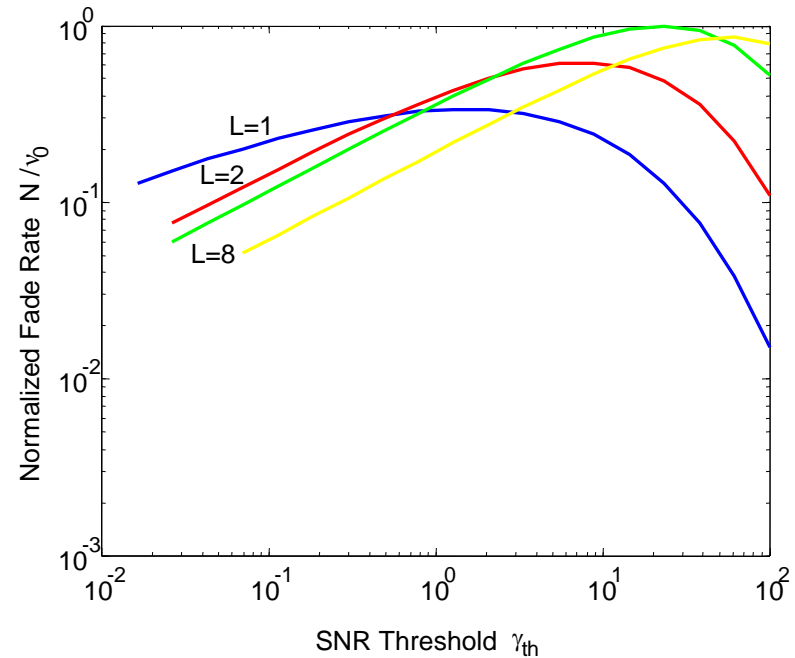
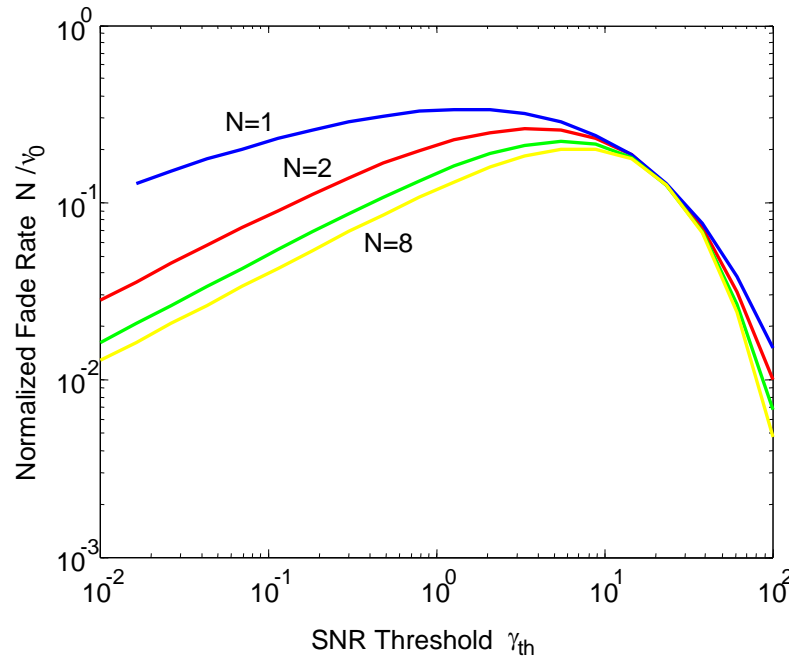
$$P_{out}(\gamma_{th}) = \int_0^{\gamma_{th}} p_{\gamma}(\gamma) d\gamma$$



# Level Crossing Rate

- The average outage (fade) duration and the frequency of outages are important performance criteria for the proper selection of transmission PRF, pulse length

$$N(\gamma_{th}) = p_{\gamma}(\gamma_{th}) \int_0^{\infty} \gamma' p_{\gamma'}(\gamma' | \gamma_{th}) d\gamma'$$



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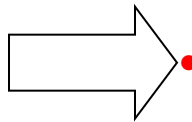
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# Final Remarks

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- Atmospheric turbulence coupled with target speckle deteriorates coherent laser radar performance
- Spatial and temporal diversity methods, along with phase correction techniques, can be applied to mitigate signal deterioration
- Measures of performance are required to estimate the effectiveness of the compensation methods
- The speckle reflected from atmospheric scatters is a compounded effect of the atmospherically induced SNR fluctuations and the speckle fluctuations
- Our model helps to explore the various possibilities that exist to deploy compensation techniques