

Calculation of the CO₂ storage term in an urban environment: results and guidelines from Central London

Alex Bjorkegren¹, Sue Grimmond^{2,1}, Simone Kotthaus^{2,1}

1: King's College London

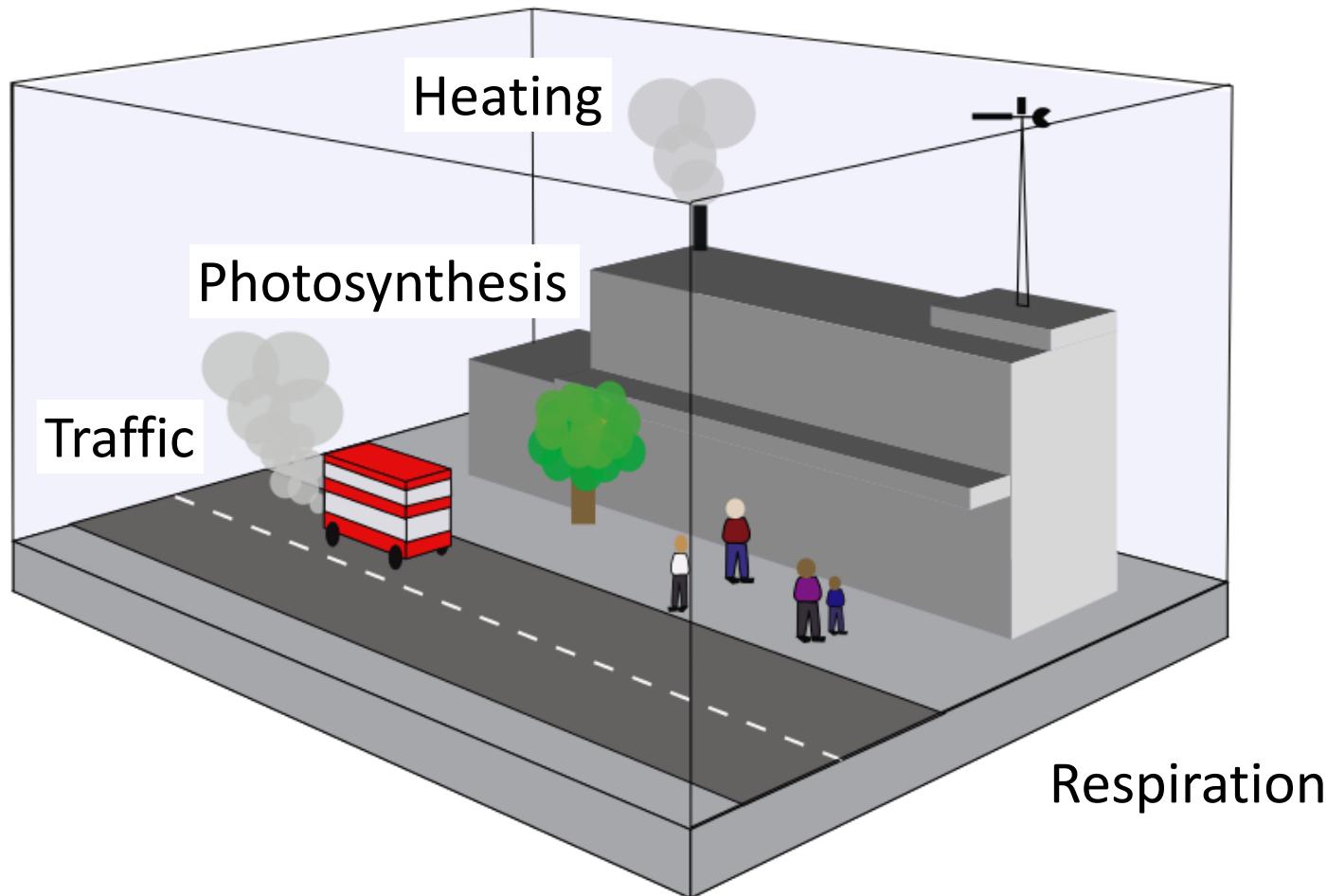
2: University of Reading

Acknowledgements: NERC ClearLo (Clean Air for London) Project

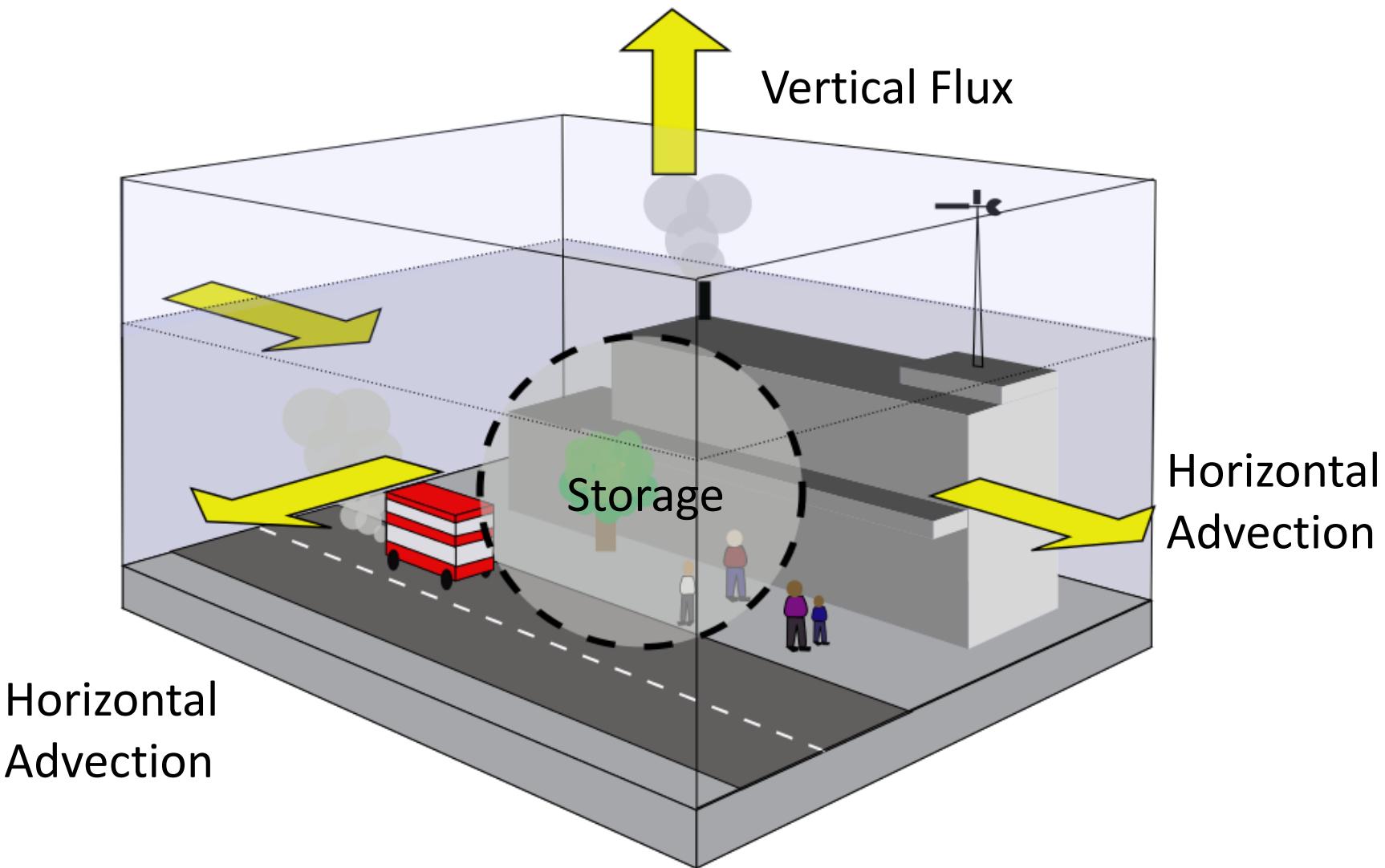
Contact: alex.bjorkegren@kcl.ac.uk



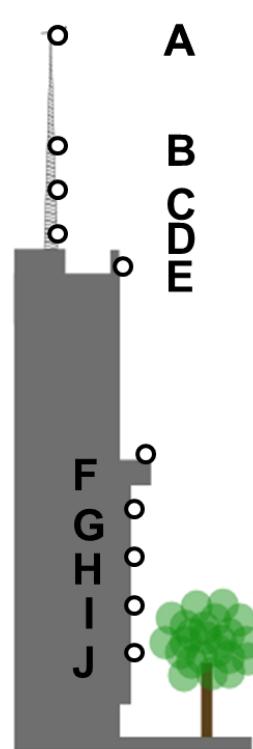
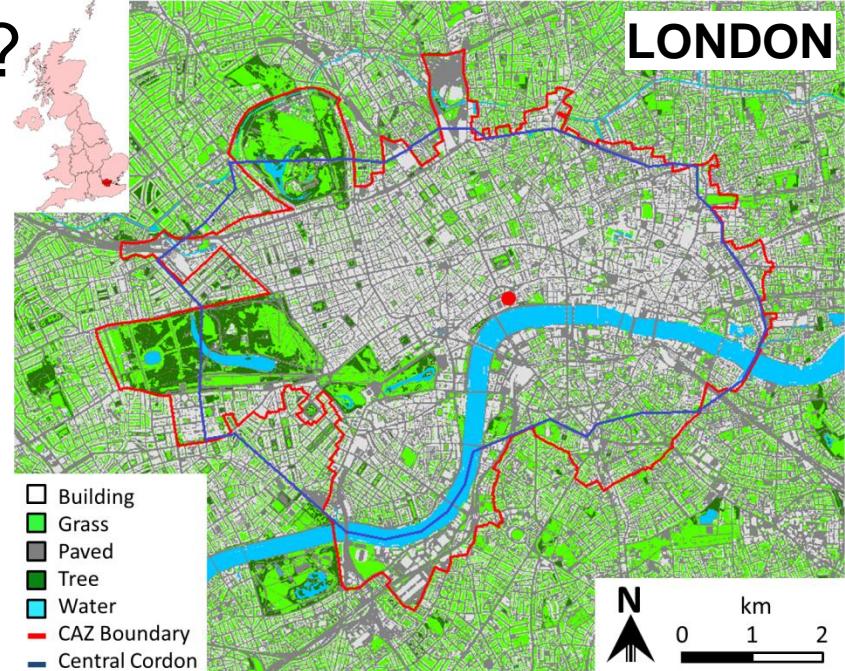
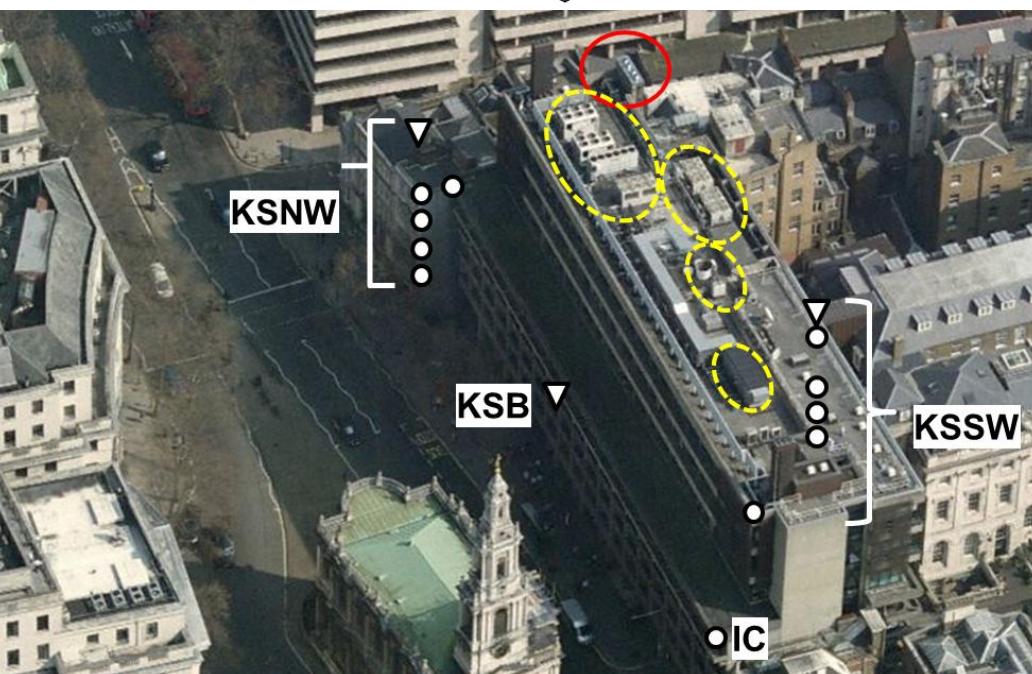
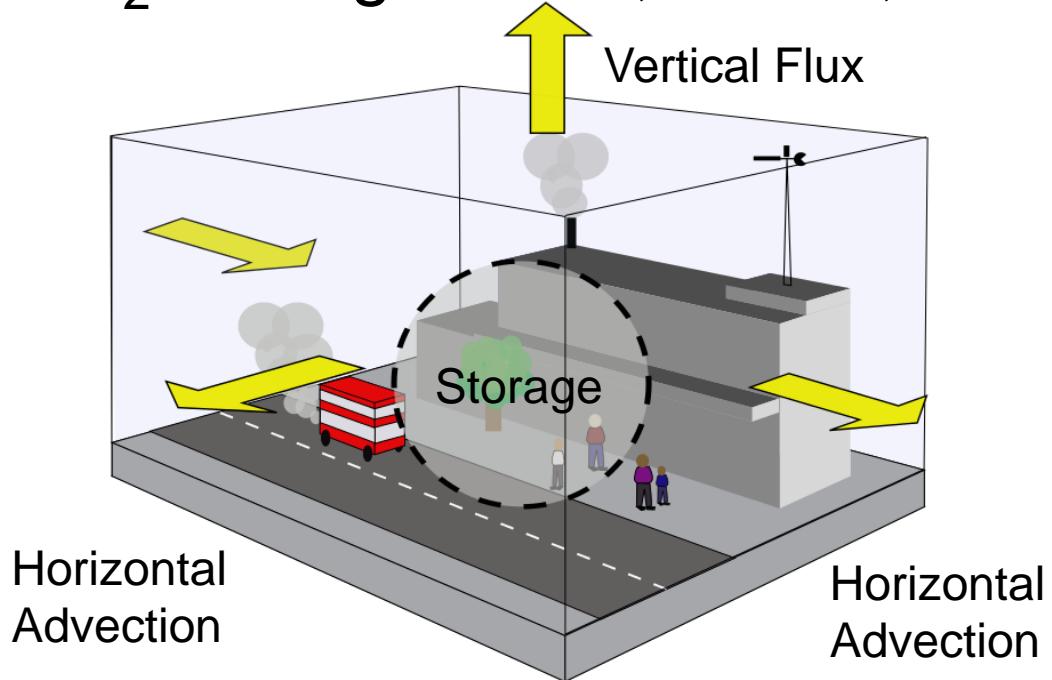
Net Emissions = Heating + Traffic + Respiration - Photosynthesis



~~Net Emissions = Flux + Storage + Advection~~



CO₂ Storage: what, where, how?



$$\Delta C_S = \int_0^{z_h} \frac{\partial \bar{c}}{\partial t} dz$$

$$\approx \sum_{i=1}^h \left[\frac{\Delta c(z_i)}{\Delta t} \right] \Delta z_i$$

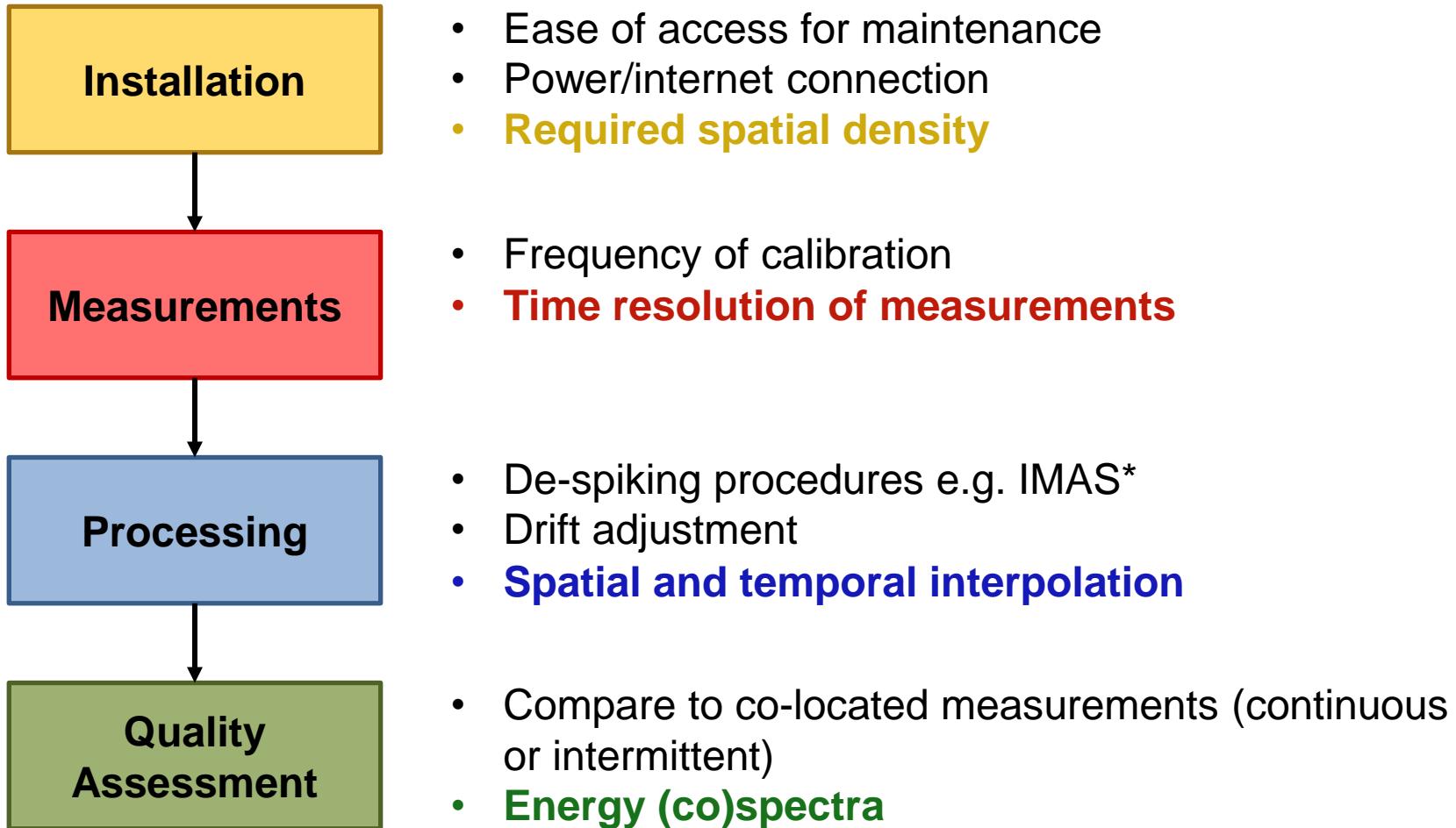
Δz_i

$\Delta c(z_i)$

10:55

10:45

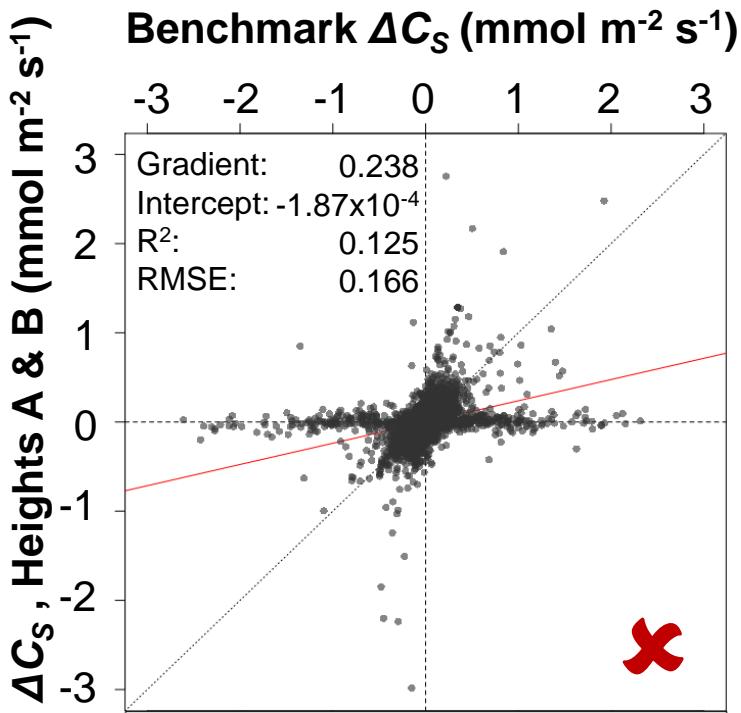
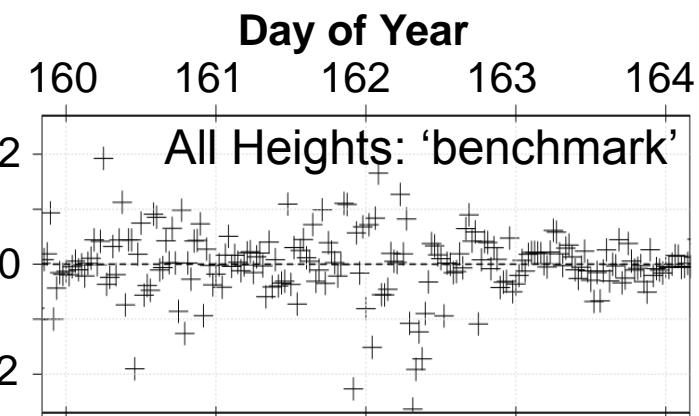
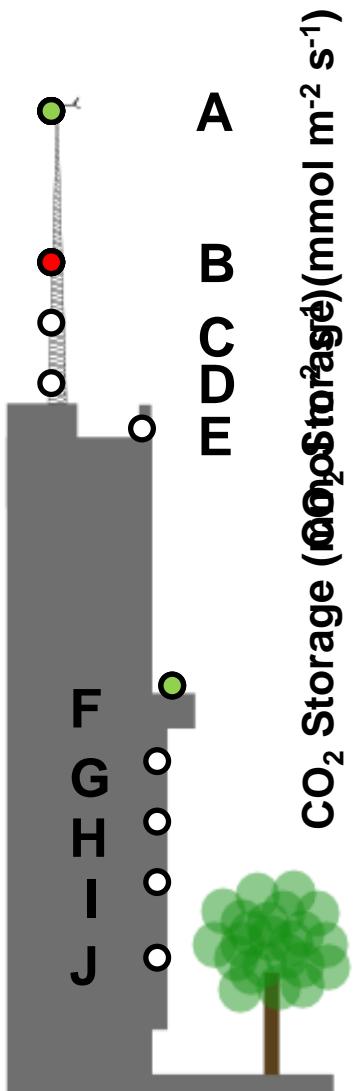
Calculating CO₂ storage: workflow



* Kotthaus and Grimmond (2012)

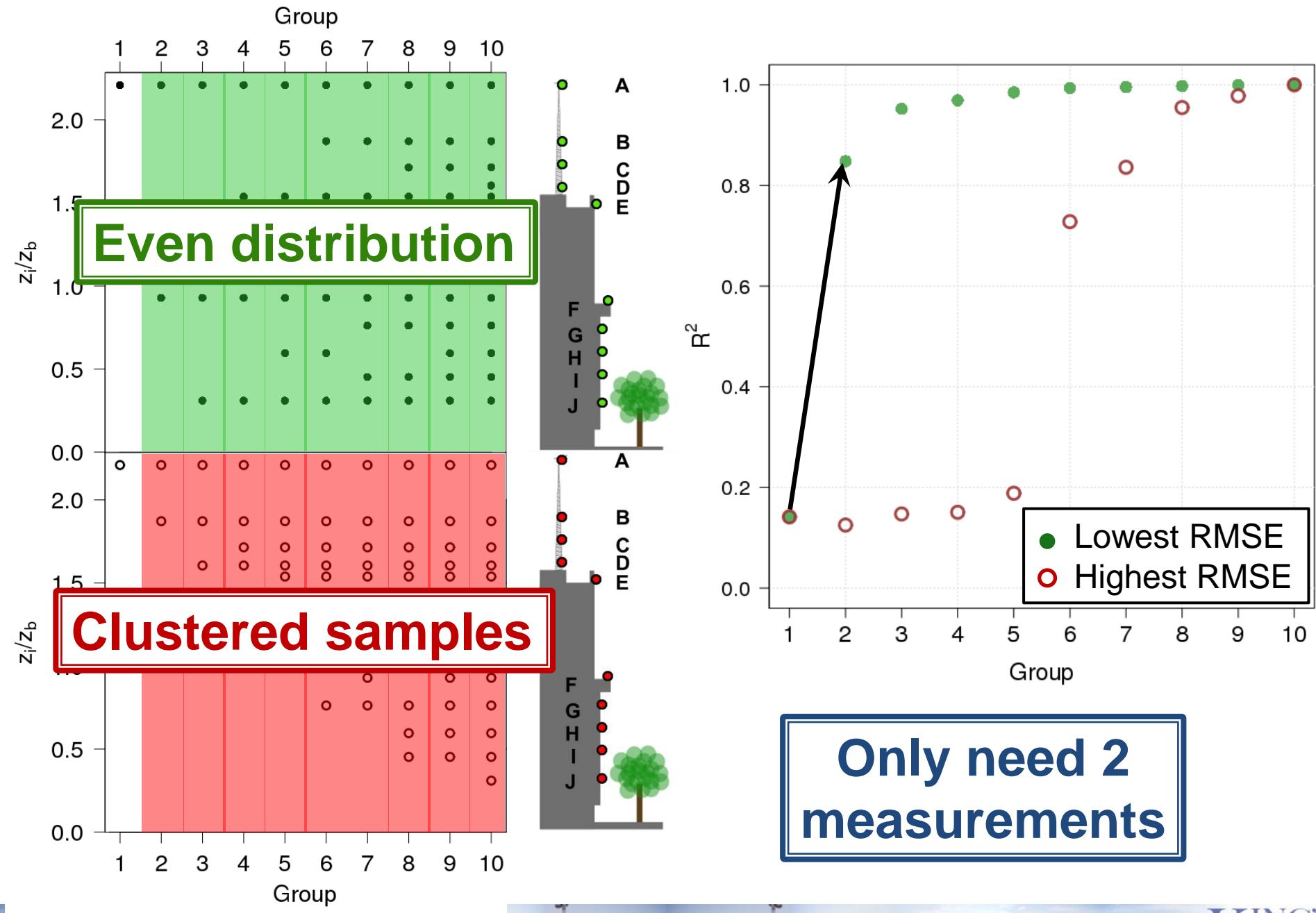


CO_2 Storage: Spatial Resolution of Measurements



Data collected by Li840
2012/150 – 2013/153

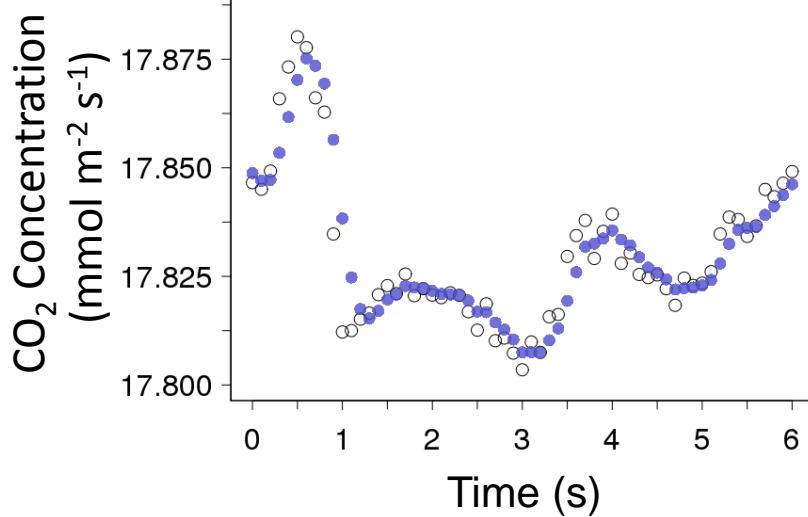
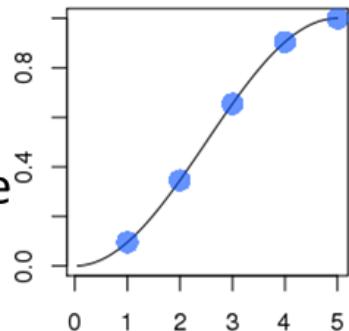
Installation



Time resolution of measurements

Sensor response time

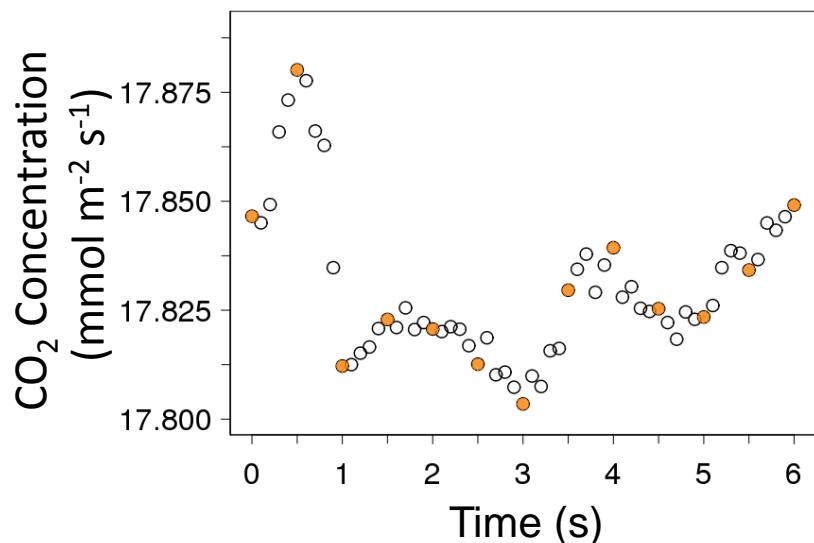
Smoothed by modified cosine



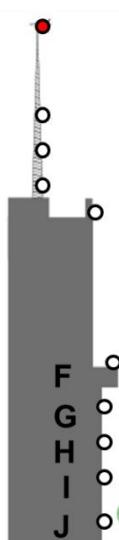
Installation

Measurements

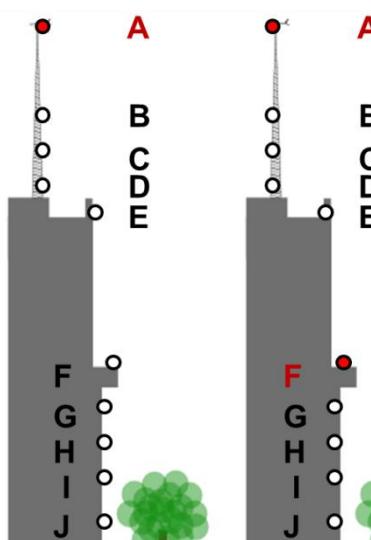
Sensor sampling interval



ΔC_S , Single



ΔC_S , Profile



LI7500



20 Hz



LI840

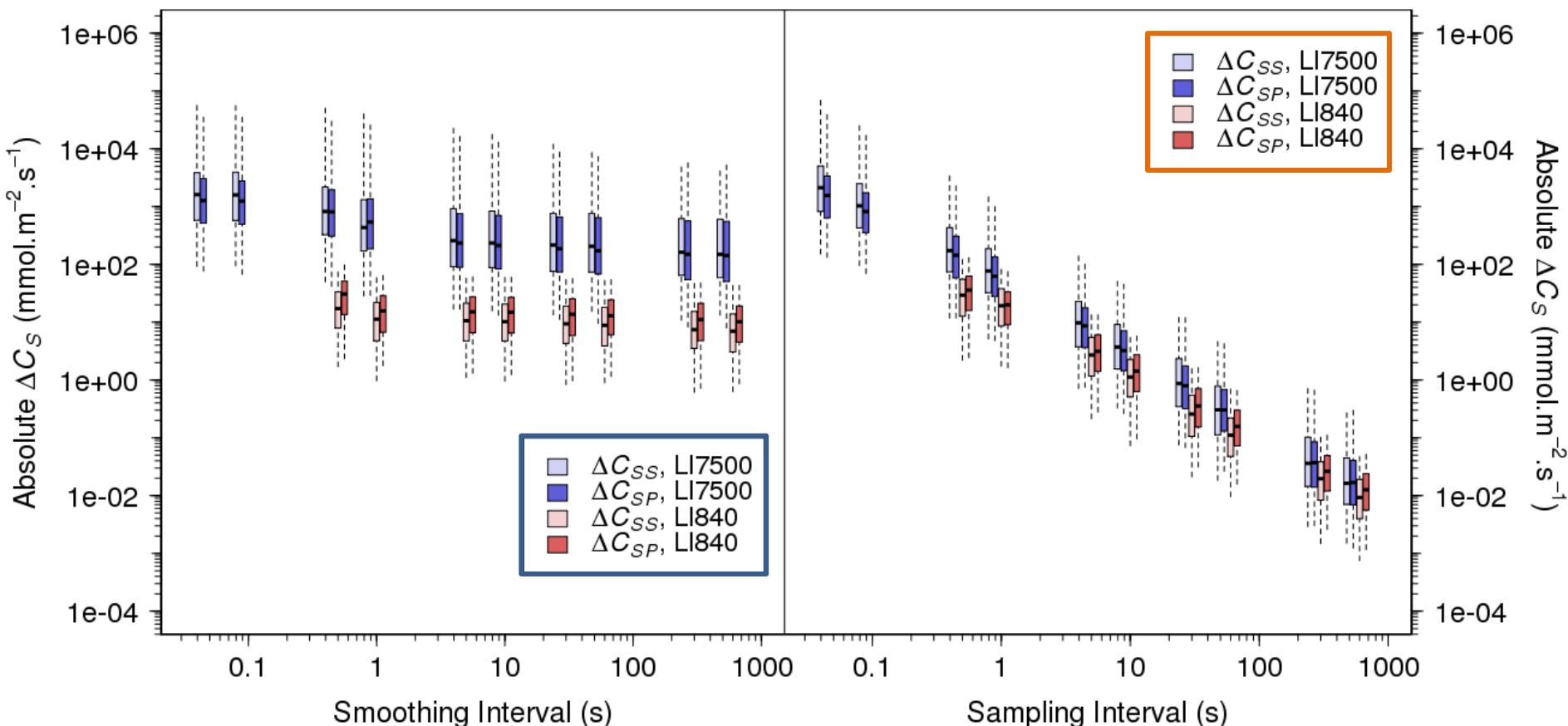
2 Hz

Time resolution of measurements

LI7500 and LI840, Heights A and F, 2014/013 – 2014/043

ΔC_{SS} : data from single height

ΔC_{SP} : data from vertical profile



- Aim for response time < 0.1 s
- Little difference between response times > 1 s

$$\log_{10}(|\Delta C_S|) = a \log_{10}(t_s) + b$$

Installation

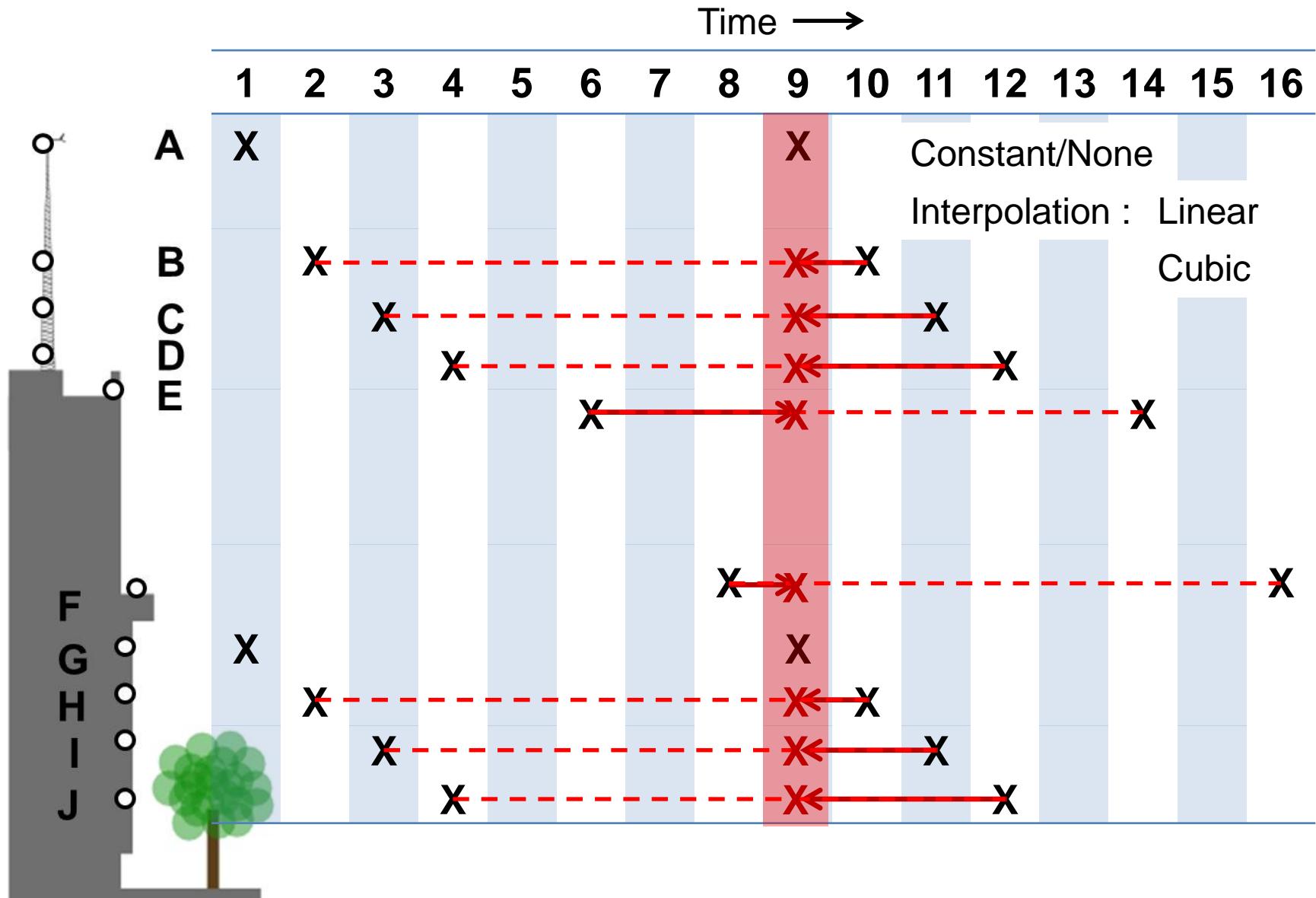
Measurements

Processing

Quality Assessment

KING'S
College
LONDON

Interpolation in time



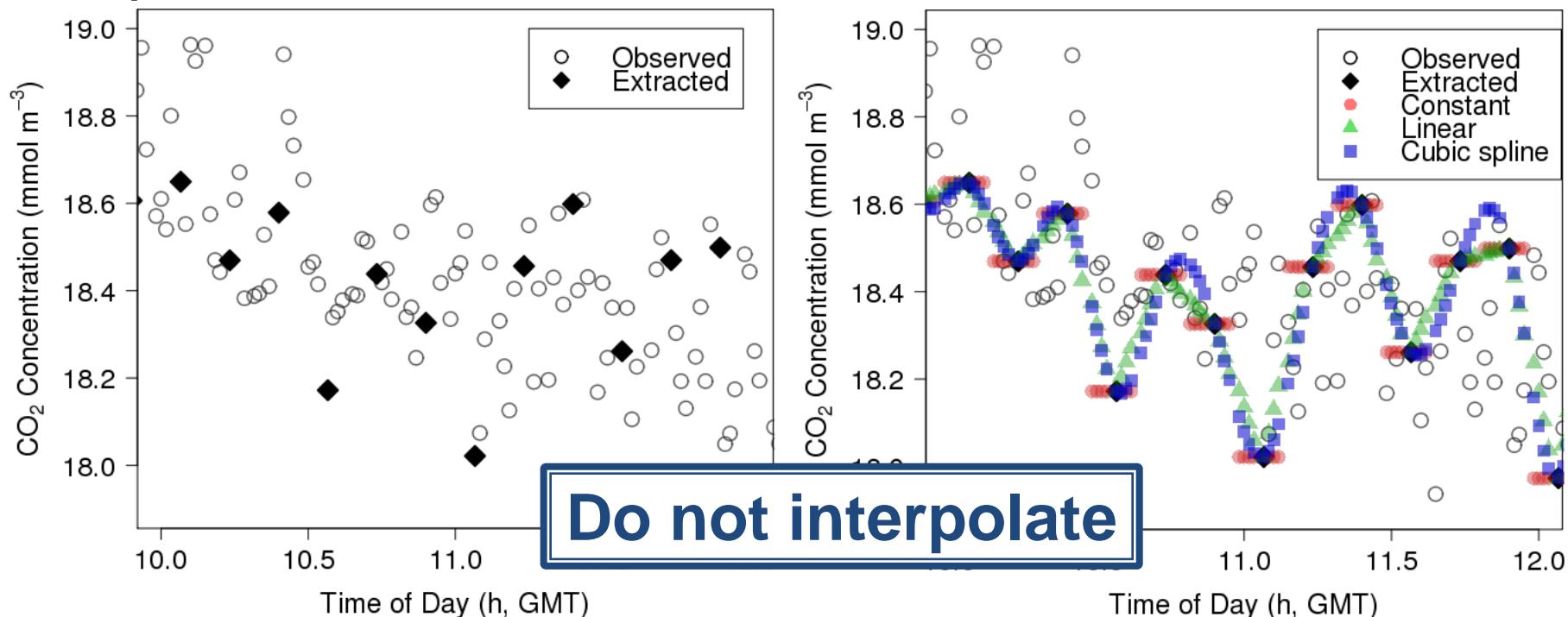
Installation

Measurements

Processing

Quality Assessment

Interpolation in time: 2013/160 – 2013/365



	Interpolation Method	R ²	Slope	Intercept	RMSE	DoF x10 ³
CO ₂ Concentration (mmol m ⁻³)	None	0.987	0.993	0.131	0.151	181
	Linear	0.989	0.992	0.146	0.140	210
	Cubic	0.987	0.992	0.136	0.151	210
CO ₂ Storage (mmol m ⁻² s ⁻¹)	None	0	0	0.022	7.73	26
	Linear	0.030	0.945	-0.002	5.34	209
	Cubic	0.011	0.601	-0.001	5.39	209

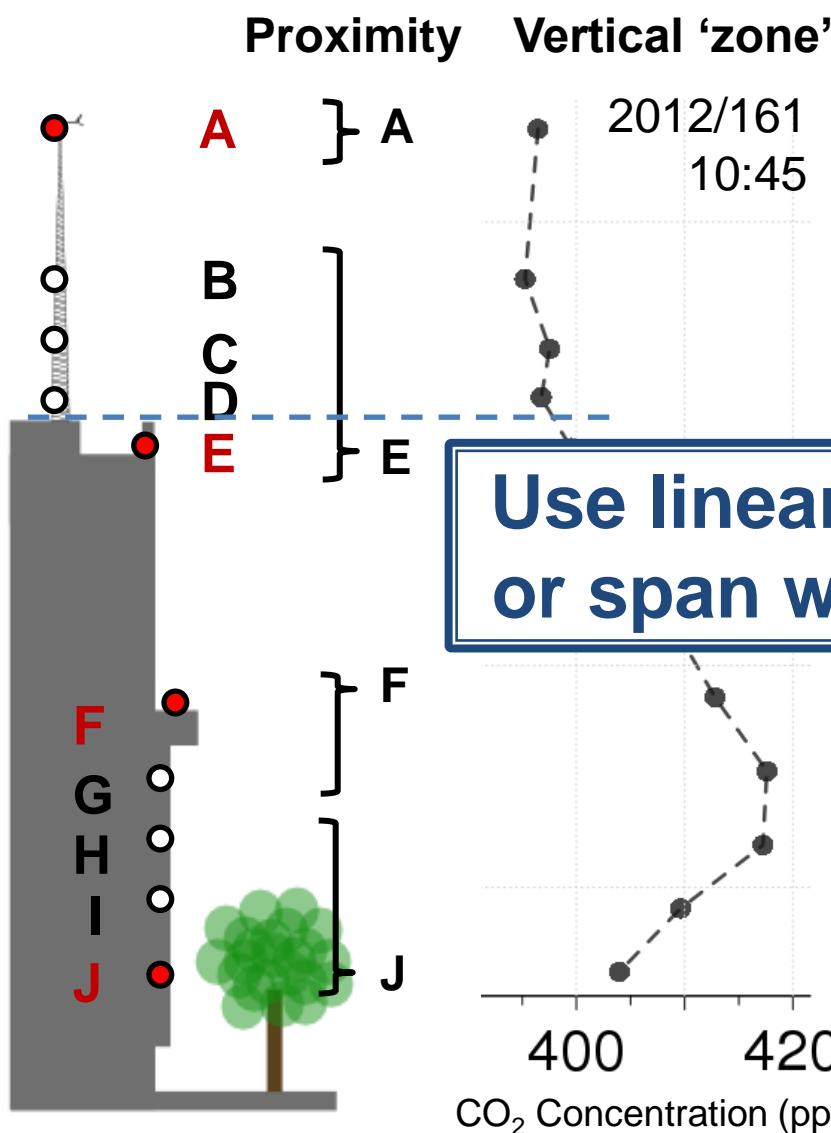
Installation

Measurements

Processing

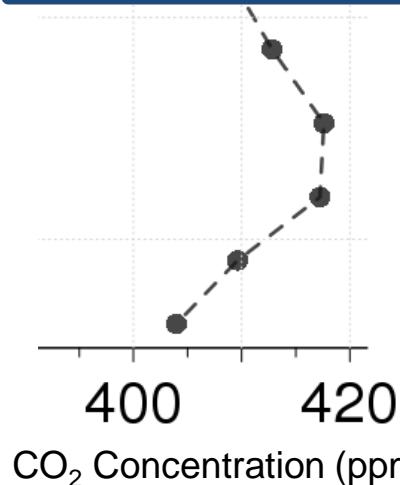
Quality Assessment

Interpolation in Space: 2013/160 – 2013/365



Interpolation Method	Sample Location	R^2	Intercept (ppm)	Slope	RMSE (ppm)	DoF $\times 10^3$
None (proximity)	B (E)	0.82	64.3	0.84	10.4	41
	C (E)	0.82	50.9	0.87	10.9	41
	D (E)	0.85	50.3	0.87	10.0	41
	G (F)	0.86	3.2	1.00	10.7	38
	H (J)	0.91	28.9	0.93	7.9	38
	I (J)	0.90	30.0	0.93	8.4	38

Use linear interpolation
or span weight by zone



Installation

Measurements

Processing

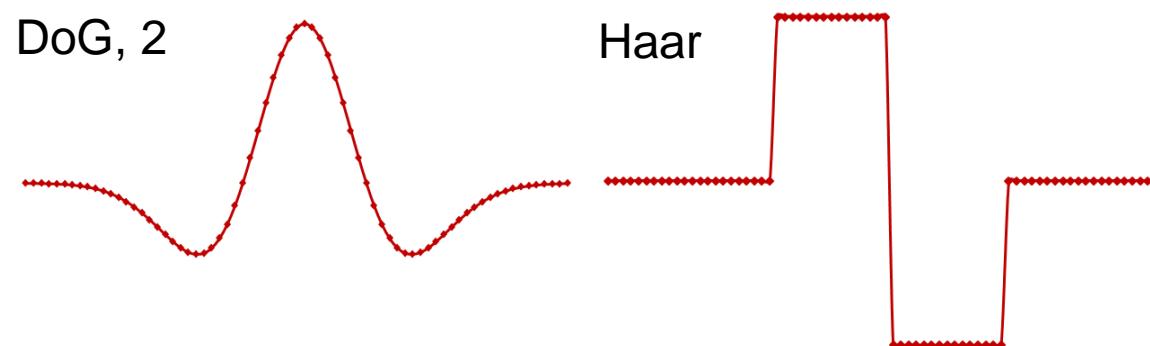
Quality Assessment

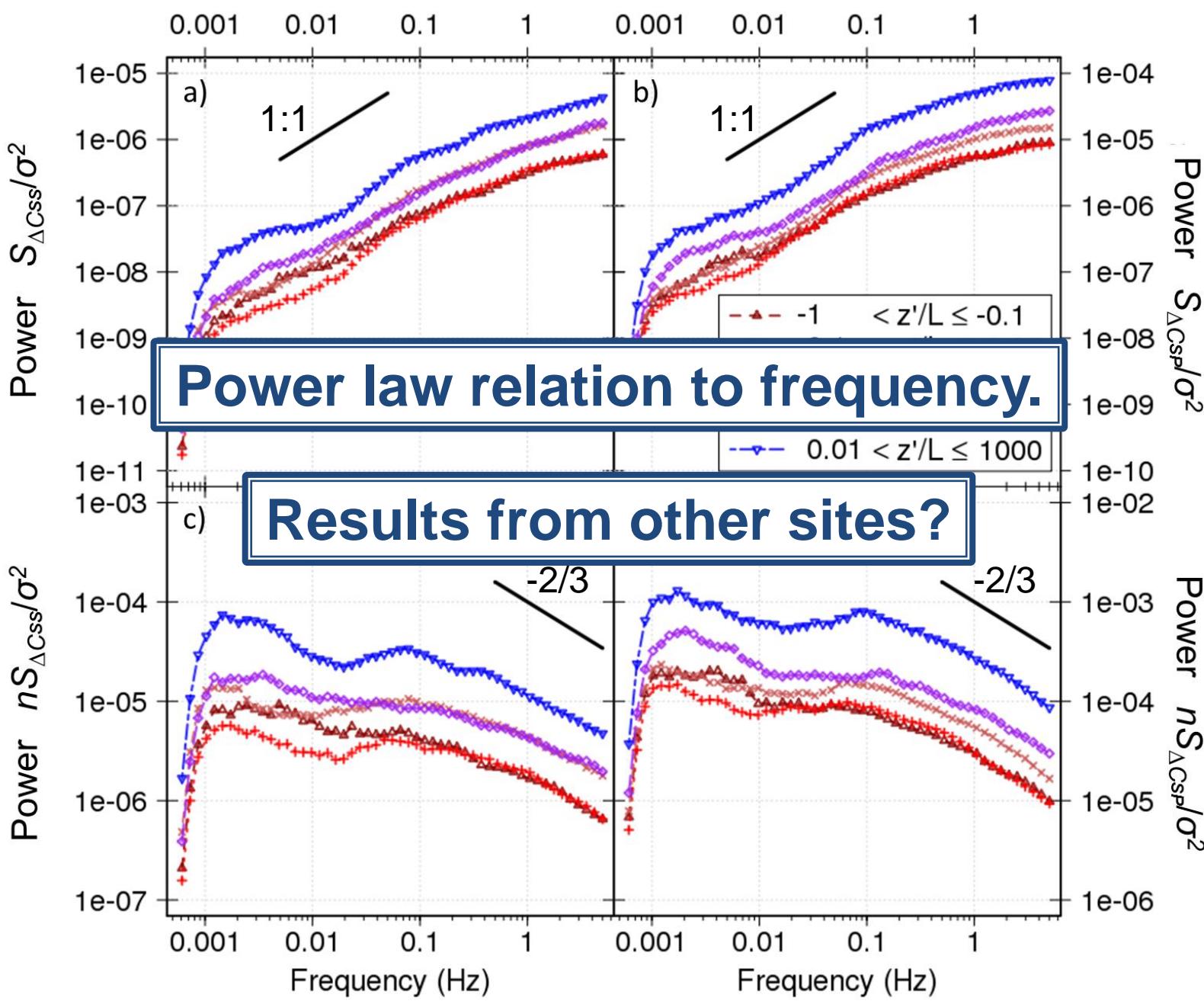
Choice of method for frequency analysis

Criteria	Fourier Analysis	Lomb-Scargle Periodogram	Wavelet Analysis
Automatable	✓	✓	✓
Tolerant to gaps/errors	✗	✓	~
Quick to run	✓	✗	✓

Admissibility Conditions

- Mean of 0
- Localised in both time and frequency space





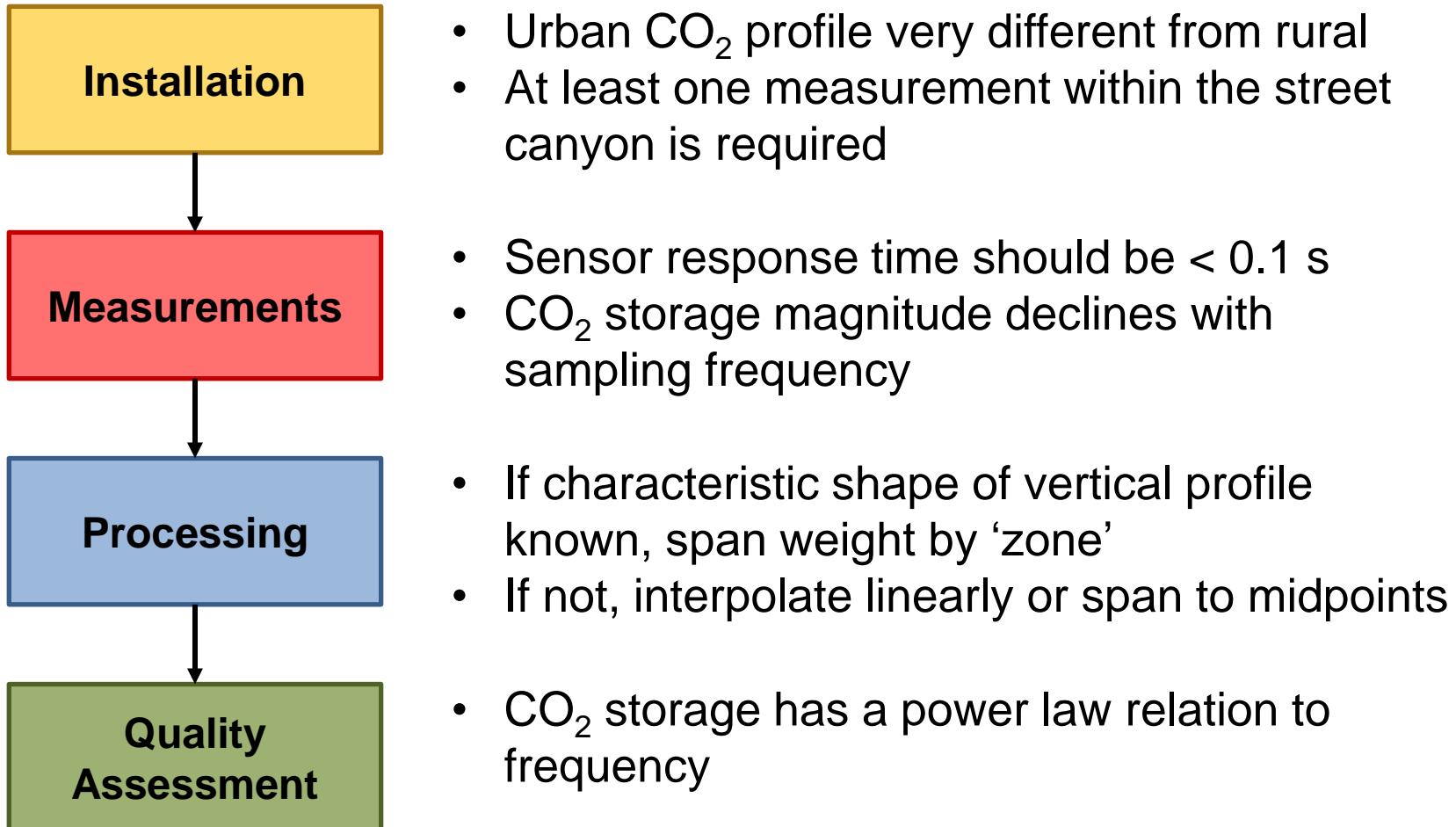
Installation

Measurements

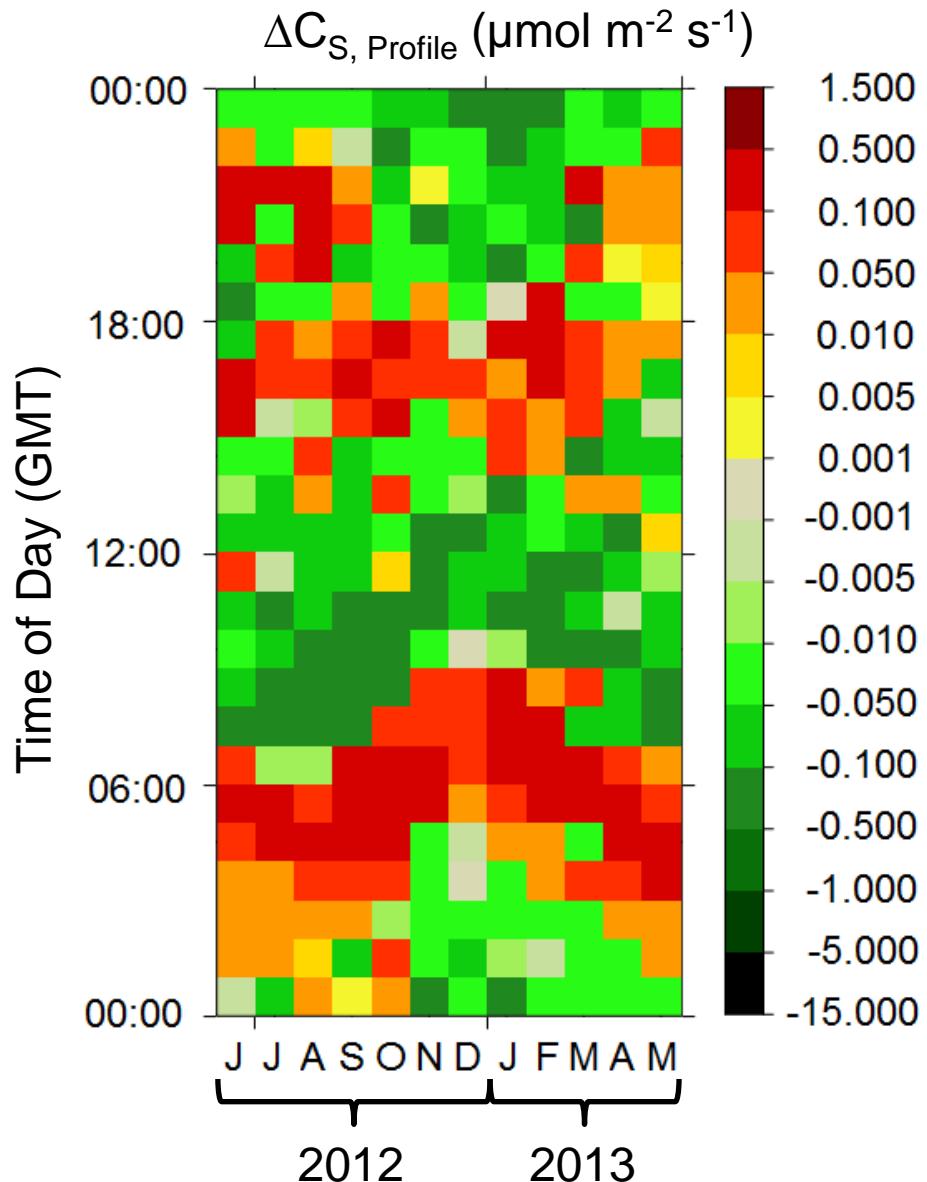
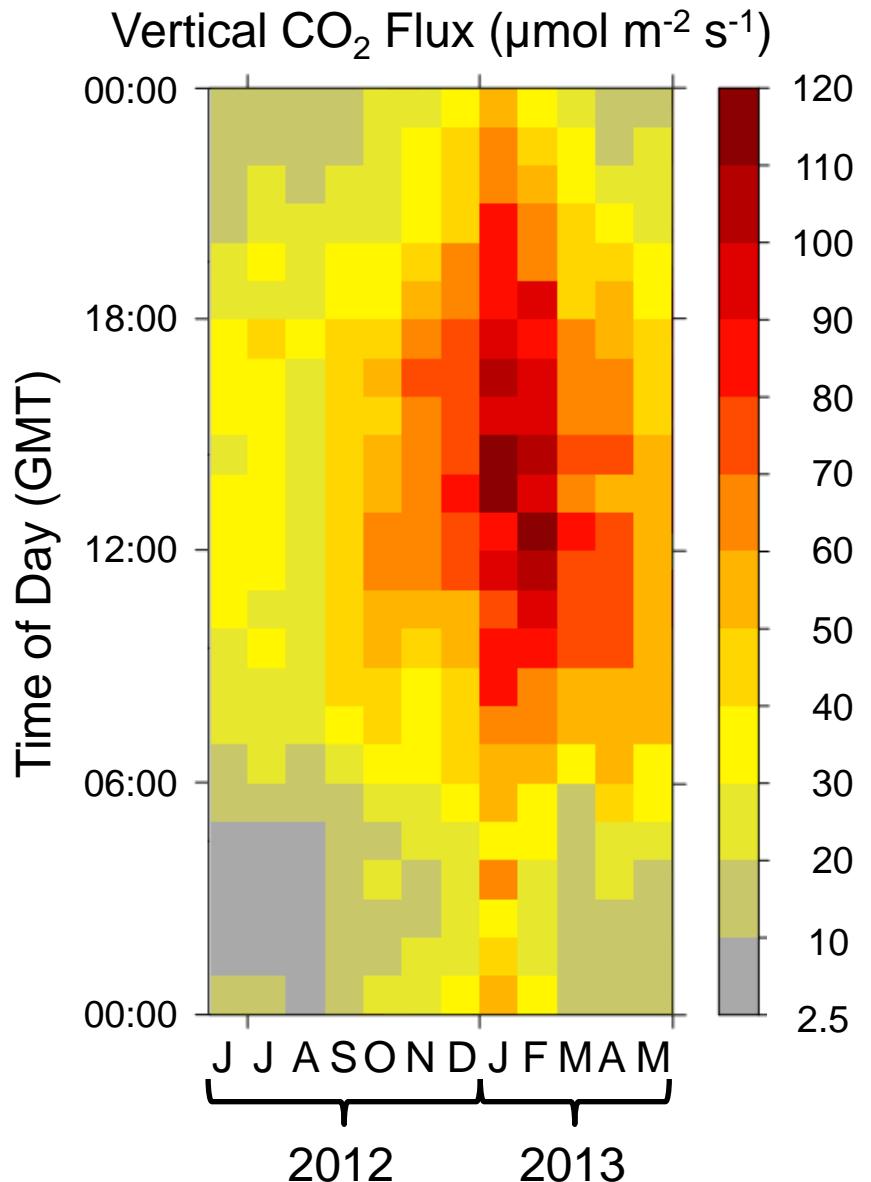
Processing

Quality Assessment

Conclusions

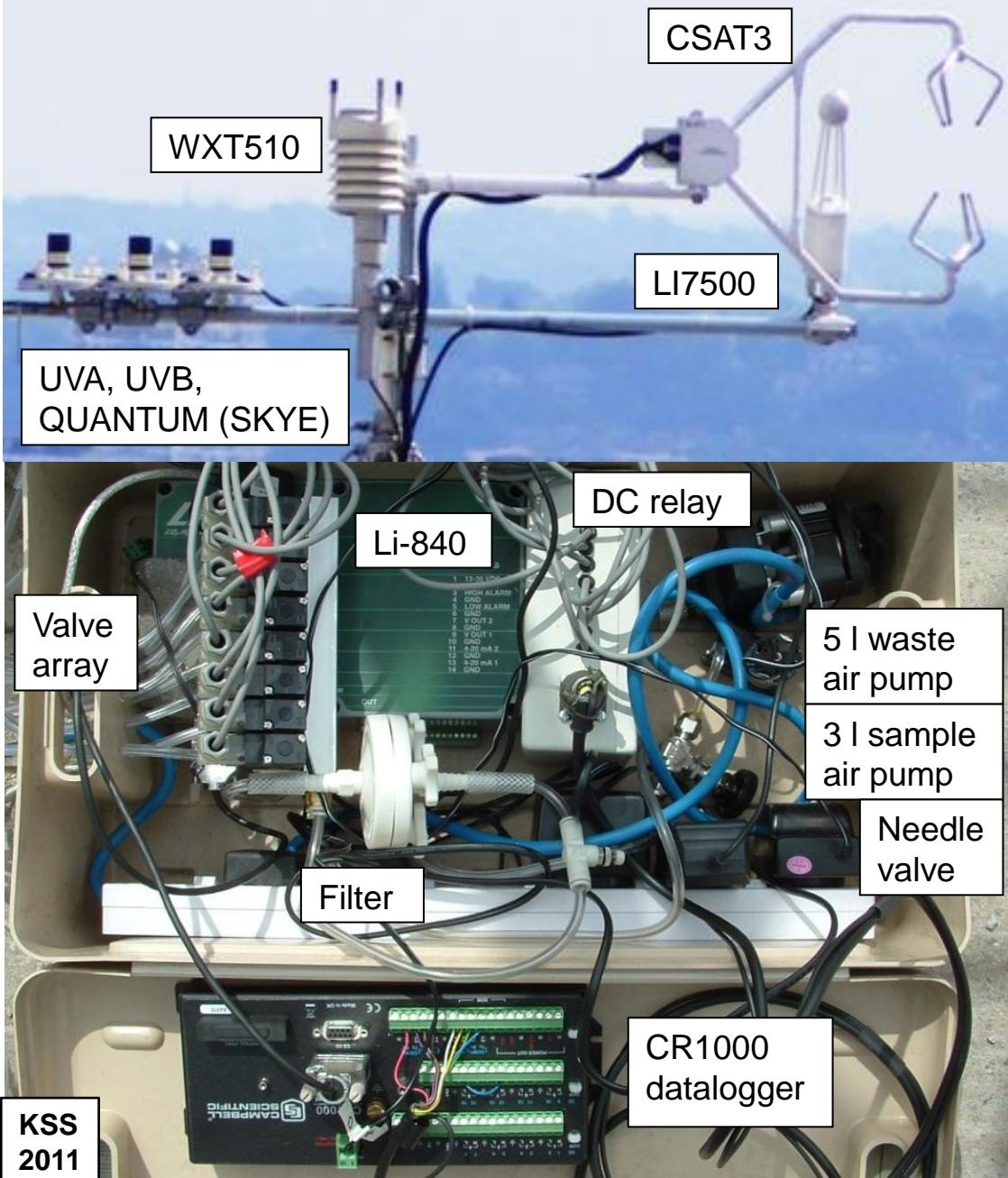
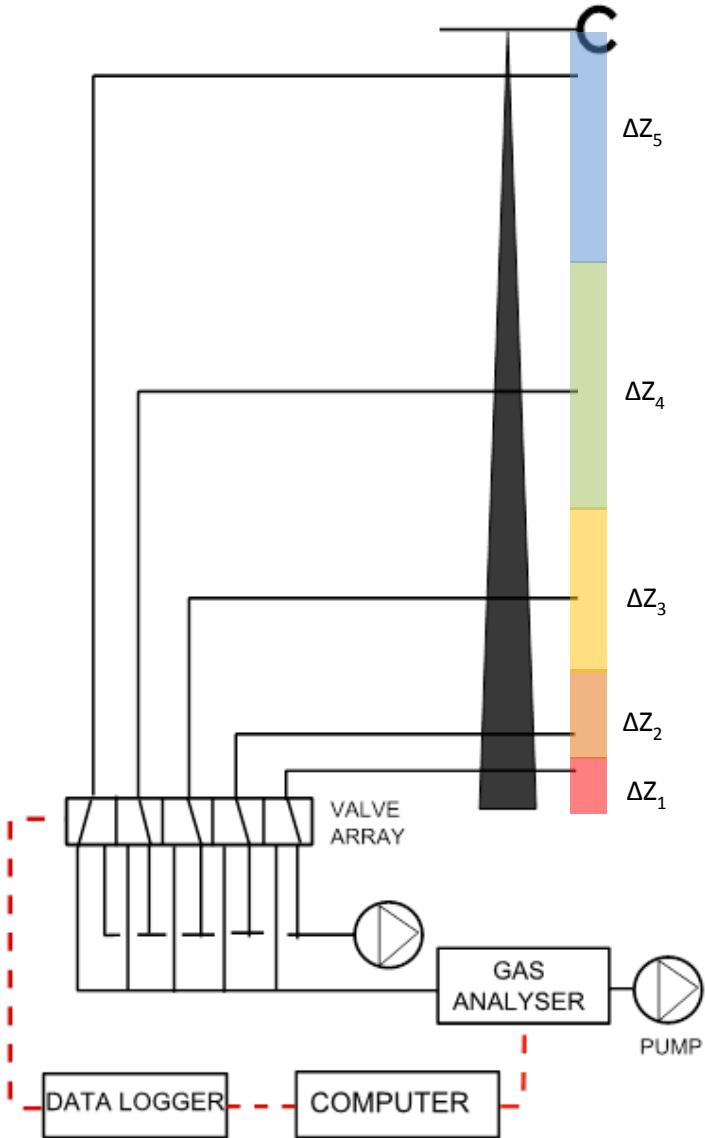


Results: Vertical flux and CO₂ storage June 2012 to May 2013

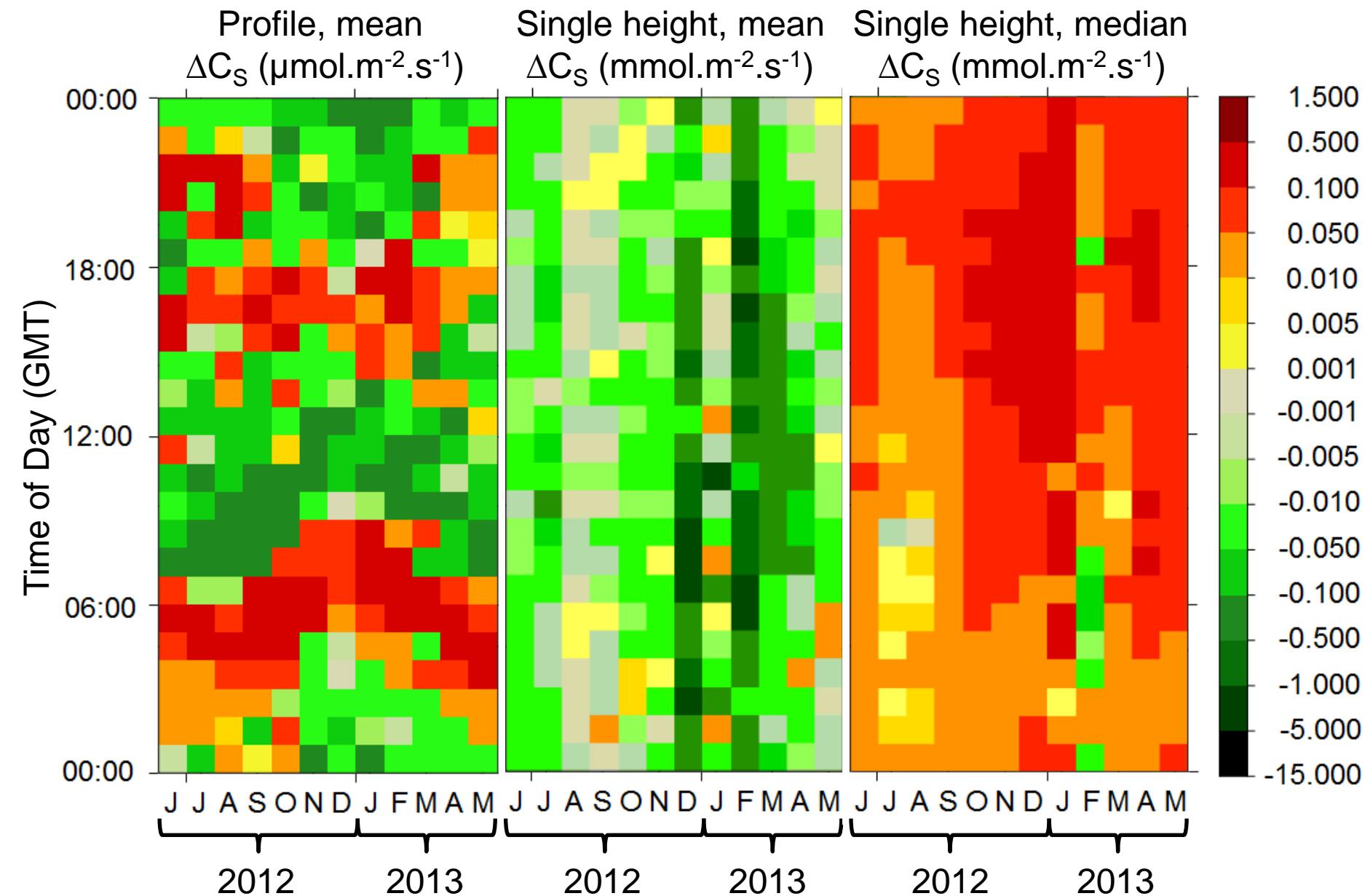


References: Kotthaus, S. and Grimmond, C.S.B. (2012) Identification of micro-scale anthropogenic CO₂, heat and moisture sources – processing eddy covariance fluxes for a dense urban environment. *Atmospheric Environment*, 57, 301-316.

Equipment



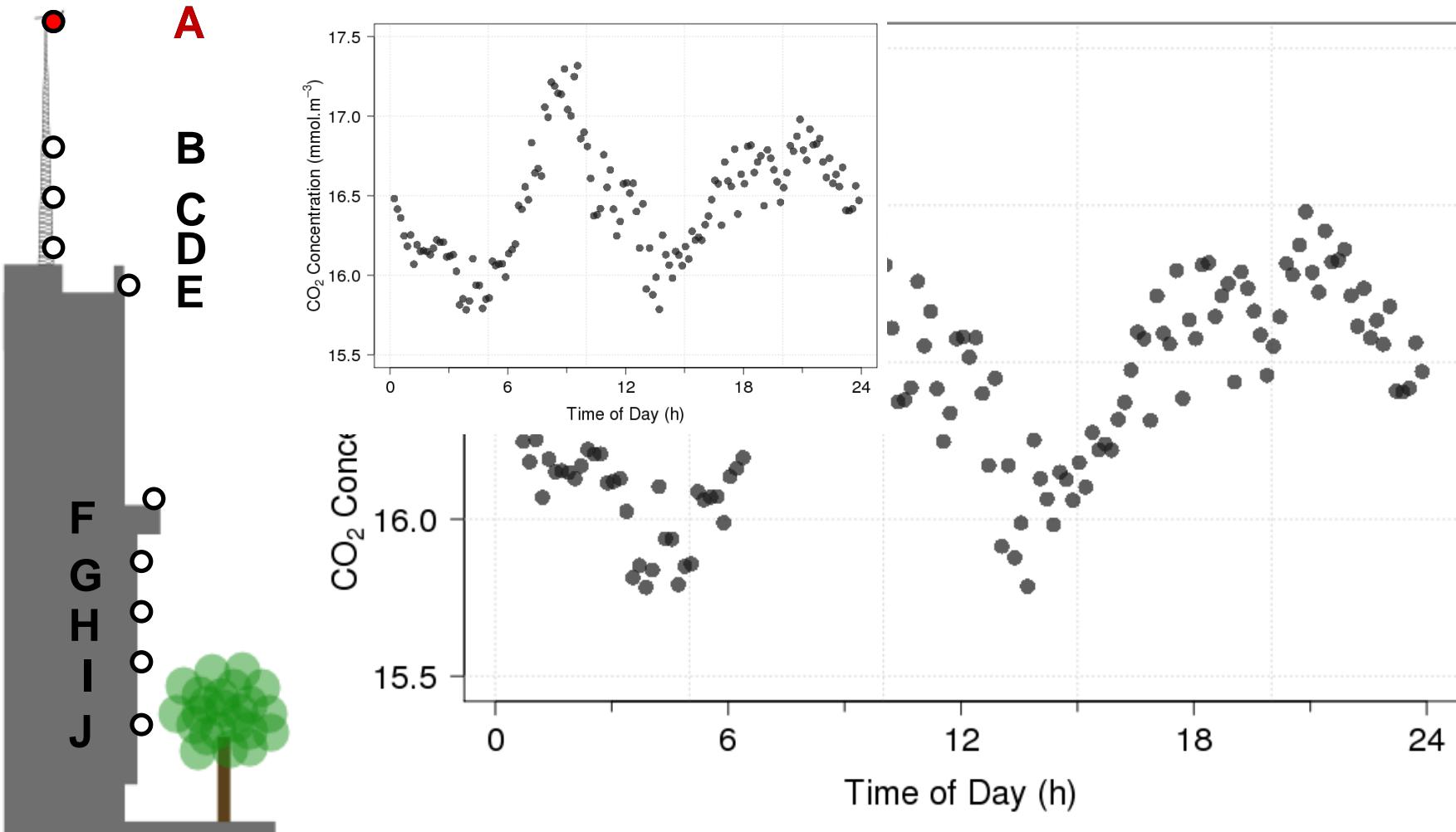
CO₂ Storage: 2012/159-2013/150



CO₂ Storage

$$\Delta C_S = \int_0^{z_h} \frac{\partial \bar{c}}{\partial t} dz \approx \sum_{i=1}^h \left[\frac{\Delta c(z_i)}{\Delta t} \right] \Delta z_i$$

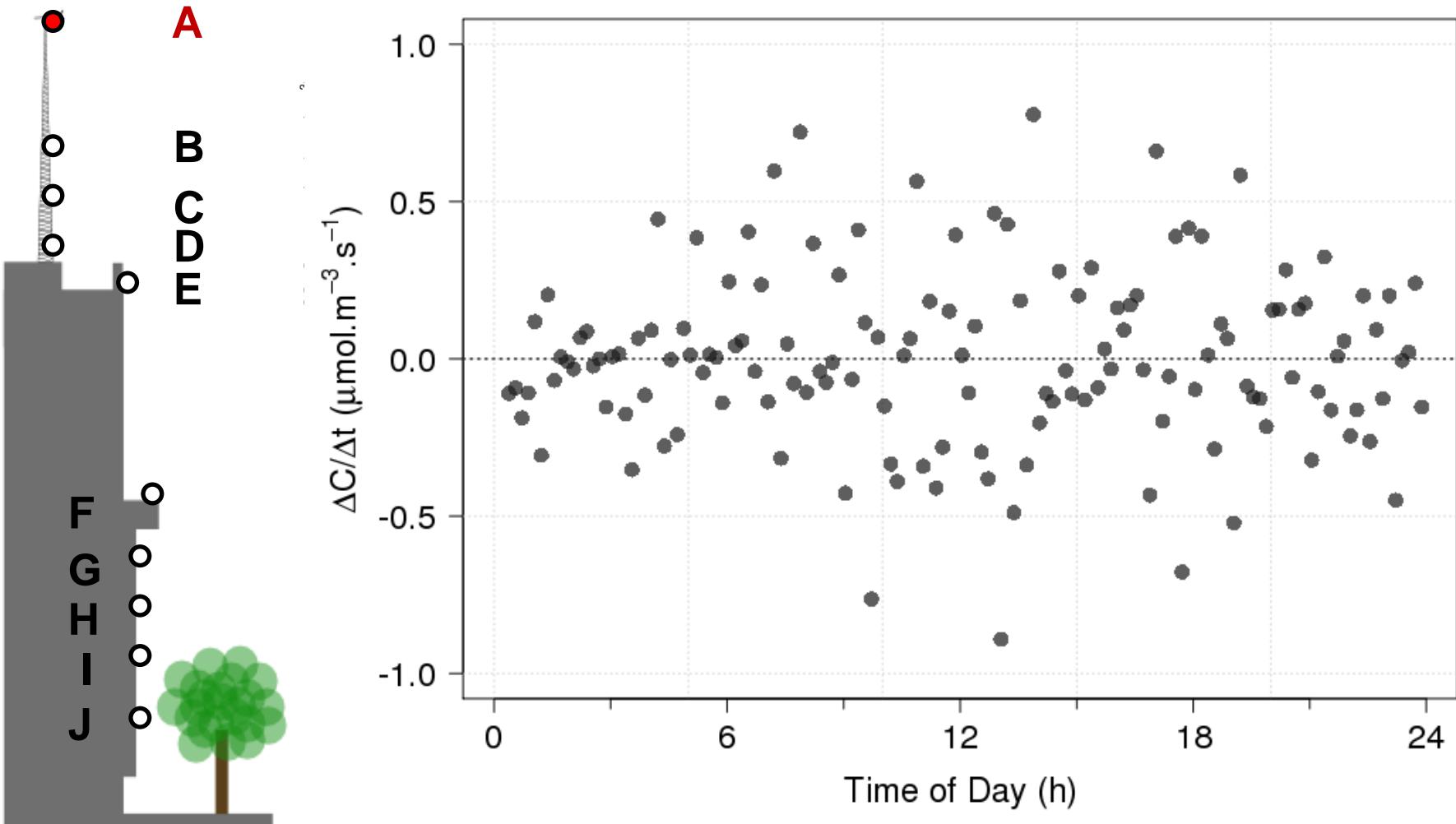
Monday 3rd December 2012 (2012/338)



CO₂ Storage

Monday 3rd December 2012 (2012/338)

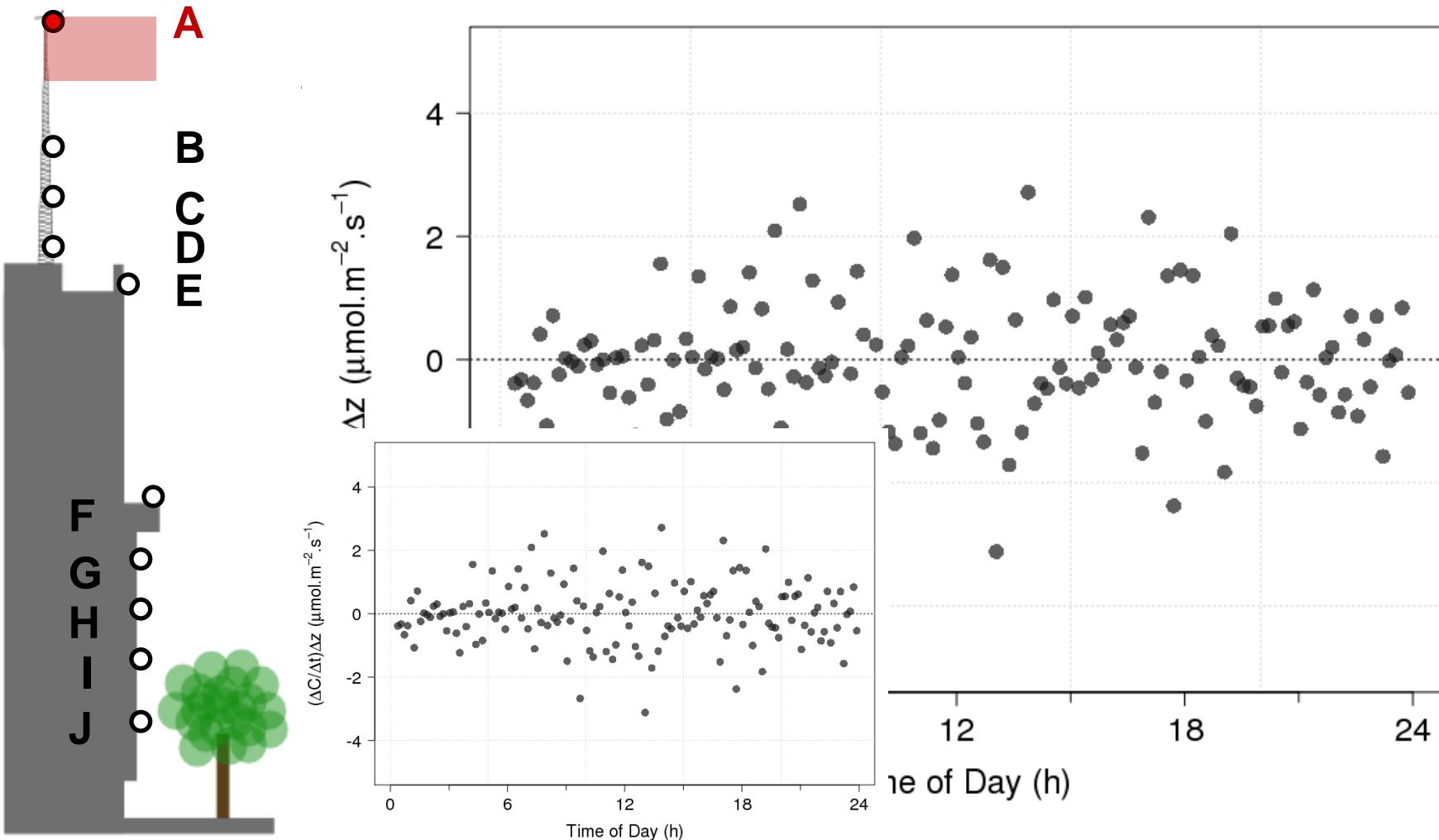
$$\Delta C_S = \int_0^{z_h} \frac{\partial \bar{c}}{\partial t} dz \approx \sum_{i=1}^h \left[\frac{\Delta c(z_i)}{\Delta t} \right] \Delta z_i$$



CO₂ Storage

$$\Delta C_S = \int_0^{z_h} \frac{\partial \bar{c}}{\partial t} dz \approx \sum_{i=1}^h \left[\frac{\Delta c(z_i)}{\Delta t} \right] \Delta z_i$$

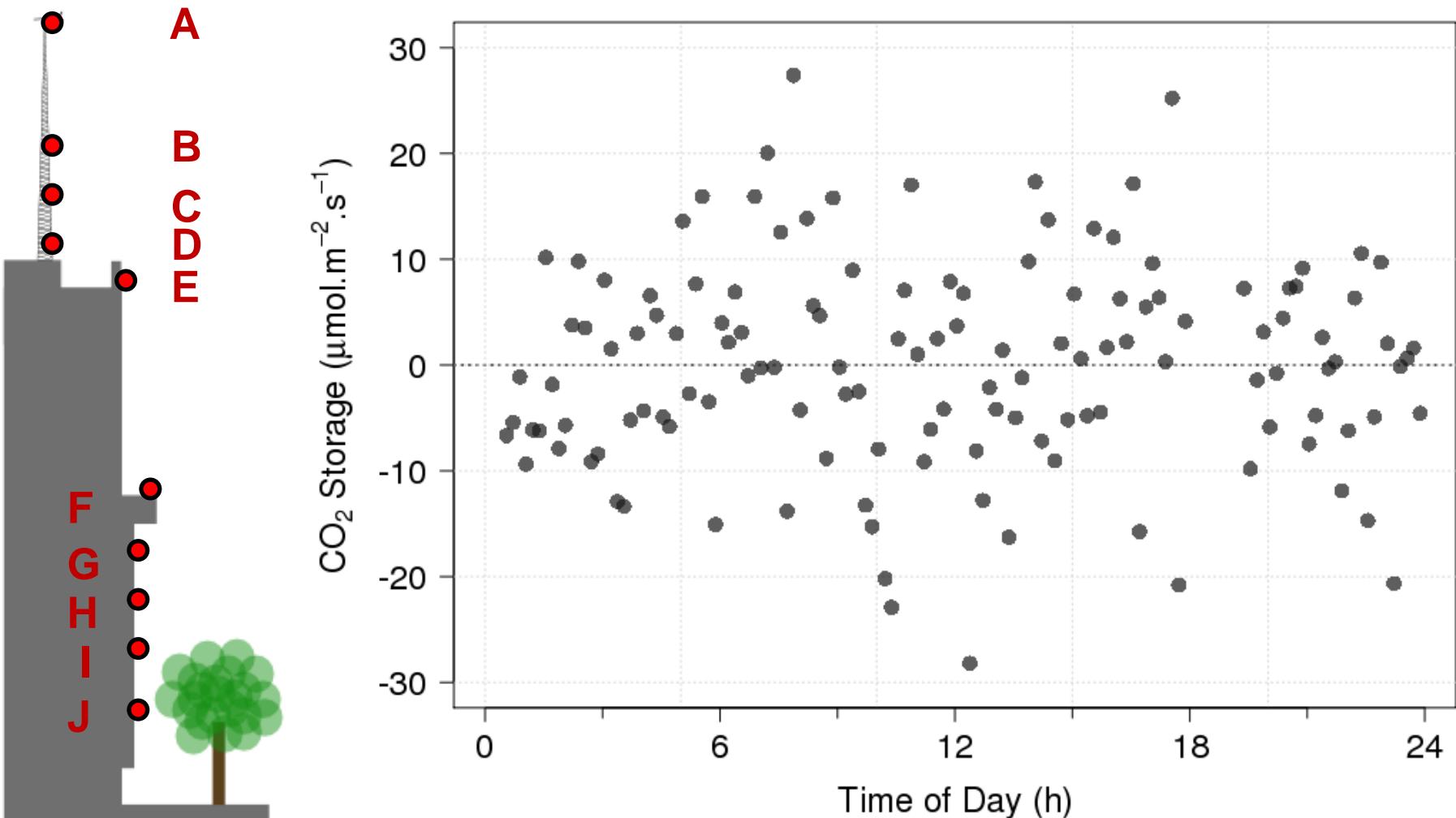
Monday 3rd December 2012 (2012/338)

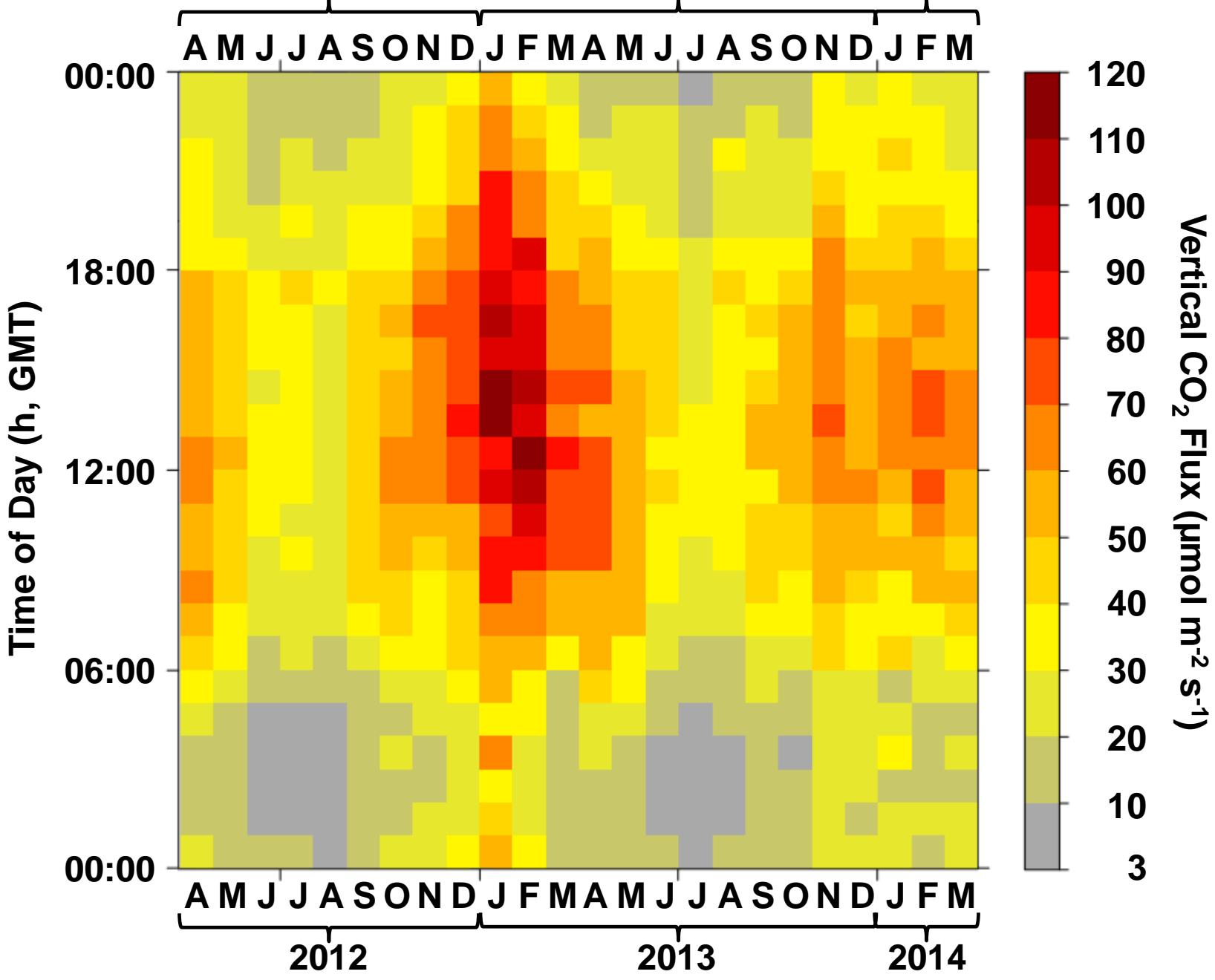


CO₂ Storage

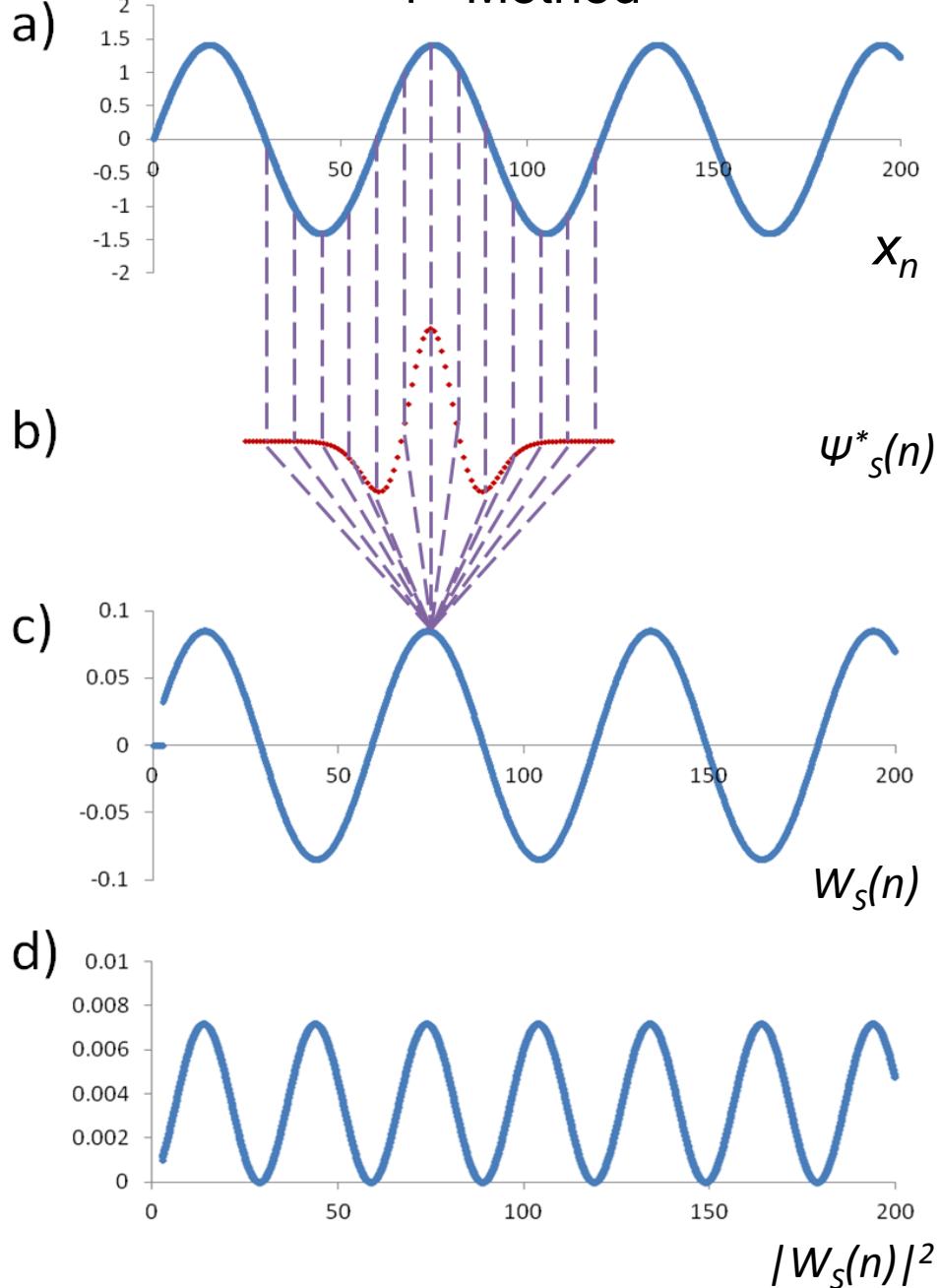
$$\Delta C_S = \int_0^{z_h} \frac{\partial \bar{c}}{\partial t} dz \approx \sum_{i=1}^h \left[\frac{\Delta c(z_i)}{\Delta t} \right] \Delta z_i$$

Monday 3rd December 2012 (2012/338)





Wavelet Transform



2nd Method

$$W_s(n) = x_n \otimes \psi_s(n)$$

$$= x_n \times \psi_s^*(n)$$

Convolution theorem:

$$\mathcal{F}\{f \otimes g\} = \mathcal{F}\{f\} \cdot \mathcal{F}\{g\}$$

$$f \otimes g = \mathcal{F}^{-1}\{\mathcal{F}\{f\} \cdot \mathcal{F}\{g\}\}$$

$$\hat{x}_k = \frac{1}{N} \sum_{n=0}^{N-1} x_n e^{-2\pi i kn / N}$$

$$W_n(s) = \sum_{k=0}^{N-1} \hat{x}_k \hat{\psi}^*(sw_k) e^{i w_k n \delta t}$$

Torrence and Compo, 1998

